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Comparison of Dynamic Height Measurements From an Inverted Echo Sounder and an Island Tide Gauge in the Central Pacific

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An inverted echo sounder (IES) and deep pressure sensor were deployed within 70 km of a shallow pressure sensor at Palmyra Island (6°N, 162°W) in the central Pacific. These instruments provided yearlong records of acoustic travel time, deep pressure and sea level. Two independent time series of dynamic height are derived from travel time and sea surface elevation, respectively. The spectra of these time series are similar, and at the spectral peaks the coherence between them exceeds 99.9% confidence levels, indicating that travel time can be used to record dynamic height fluctuations. This investigation provides a frequency dependent calibration for the IES in this region. At the energetic low frequencies (periods ~ 1 month), this calibration agrees with a calibration by the standard method using conductivity-temperature-depth (CTD) casts. At higher frequencies (periods of ~ 3 days), using the CTD-derived calibration may underestimate the amplitude of some processes by as much as 30%.

1. INTRODUCTION

From mid-February 1985 to mid-February 1986, as part of the Tropical Ocean and Global Atmosphere (TOGA) program, three inverted echo sounders (IES) [Chaplin and Watts, 1984] were deployed near 6°, 8°, and 10°N along 162.5°W in the central Pacific, as a northward extension of a Line Islands array of near-surface pressure recorders (Figure 1). The southernmost IES with temperature and deep pressure sensors was moored at 5°55'N, 162°43'W (4324-m depth), 70 km west of the northernmost shallow pressure gauge at 5°53'N, 162°05'W (4-m depth), in the lagoon at Palmyra Island.

The IES measures the round trip acoustic travel time from the seafloor to the sea surface. Because the speed of sound varies with temperature and salinity, travel time has been used as a measure of various baroclinic parameters, in particular dynamic height. Previous studies using IESs have linked travel time with dynamic height using the qualitative arguments of Watts and Rossby [1977] and the linear empirical calibrations found, for example, in the Gulf Stream [Watts and Johns, 1982] and in the eastern and central equatorial Pacific [Miller *et al.*, 1985; Chiswell *et al.*, 1986].

These empirical calibrations are usually made by regressing dynamic height with synthesized travel time, both computed from a regional set of conductivity-temperature-depth (CTD) casts, which are not necessarily coincident with an actual IES deployment. The regressions often have a high correlation [e.g., Watts and Rossby, 1977], and the slope of the least squares fit is used as a calibration for the IES. These slopes, however, are controlled mainly by the large-amplitude signals, which generally occur at low frequencies. There is no assurance that the same calibration applies to less energetic, generally higher-frequency signals; and from a set of CTD casts it is

not possible to study these high-frequency signals, since they are aliased in the infrequent and irregular sampling.

The temporally coincident and nearly spatially coincident travel-time, deep-pressure, and shallow-pressure time series made near 6°N provide an opportunity to compare dynamic height derived from travel time with that derived independently from sea surface elevation. This paper presents such a comparison to determine how well the IES measures dynamic height at periods from 2 days to 4 months. The 1-year time series of measurements allows us to calibrate the IES as a function of frequency, and we investigate how this calibration compares with one obtained directly from a set of CTD casts.

In the next section we briefly review the arguments relating travel time to dynamic height. Then in section 3 we present a calibration made from CTD casts taken as part of the North Pacific Experiment (NORPAX) Hawaii-to-Tahiti Shuttle. Section 4 develops a model for the interrelationship of travel time, deep pressure, and shallow pressure. The comparison between IES-derived and sea level-derived dynamic height is given in section 5. Section 6 presents the conclusions.

2. TRAVEL TIME AND ITS INTERPRETATION

The IES is moored near the ocean bottom and regularly transmits and detects sound pulses to measure the round trip acoustic travel time, τ , from the seafloor to the sea surface. Watts and Rossby [1977] note that since the speed of sound, c , varies approximately linearly with density ρ , the integral for τ ,

$$\tau = 2 \int_{-\eta}^{z_2} 1/c \, dz$$

is similar to that for dynamic height D ,

$$D_{p_1/p_2} = 10^3 \int_{p_1}^{p_2} 1/\rho \, dp$$

where η = sea level, z = depth (positive downward), and p = pressure. SI units are used here (depth in meters, density in kilograms per cubic meter, etc.), except for pressure and dynamic height, which are in decibars and dynamic meters (1 dyn m = 10 m² s⁻²), respectively. Watts and Rossby [1977]

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Fig. 1. Central Pacific Ocean showing the location of the Line Islands array, IESs (solid circles) along 162.5°W. IESs at 6° and 8°N were equipped with deep bottom pressure gauges. A shallow subsurface pressure gauge was located at Palmyra Island. Also shown is the NORPAX Hawaii-to-Tahiti Shuttle cruise track. CTD casts were made every degree between 4°S and 12°N along 150°, 153°, and 158°W; the casts used in this study were those taken near 6°N.

thus suggest that travel time may be a good linear indicator of dynamic height. Since c and ρ depend on temperature and salinity differently, however, the relationship between τ and D depends on the T - S properties of the water column. An IES calibration thus varies regionally and may depend on the process leading to the variability in τ and D (e.g., variability limited to the upper water column may need a different calibration from that extending throughout the entire column).

3. CTD-DERIVED CALIBRATION

The CTD casts used in the present study were taken as part of the NORPAX Hawaii-to-Tahiti Shuttle Experiment [Wyrski *et al.*, 1981; Wyrski and Kilonsky, 1984]; sites were spaced 1° apart along three meridional legs (150°, 153°, and 158°W) between Hawaii and Tahiti (Figure 1). Casts were taken at each site approximately once a month between February 1979 and June 1980, usually to 1000 dbar.

The plot of dynamic height anomaly relative to 1000 dbar, $\Delta D_{0/1000}$, as a function of synthesized travel time to the same level, $\tau_{0/1000}$, for all NORPAX CTD casts taken between 5.5°N and 6.5°N (Figure 2) shows the typical linear relationship ($r^2 = 0.94$) found in these regressions. The slope, m , of $-82.1 \text{ dyn m s}^{-1}$ is thus the "calibration" between $\Delta D_{0/1000}$ and $\tau_{0/1000}$.

The number of deep CTD casts near 6°N, 162°W (being limited, at present, to those made at the IES sites during this project) is insufficient to provide a full-water column calibration, and the extension of the 1000-dbar calibration to the bottom ($\sim 4300 \text{ m}$) cannot be made without some prior knowledge of how m varies as the lower reference level deepens. Because CTD casts in the tropics rarely extend beyond 1000 dbar, this knowledge is limited. However L. Miller (personal communication, 1986), in a study of thermistor and CTD data collected near the equator at 110°W, finds that the magnitude of m drops by about 20% as the lower reference level deepens from 1000 dbar to below 3500 dbar (Figure 3). Thus if the same is true here, the full-water column calibration (i.e., $\Delta D_{0/4300}$ versus $\tau_{0/4300}$) should be about -66 dyn m s^{-1} .

4. RELATING TRAVEL TIME TO SEA SURFACE ELEVATION AND DYNAMIC HEIGHT

Figure 4 illustrates the model used here. On the basis of the discussion in section 2, we make the initial assumption that variations in travel time τ_{ref} , above some reference pressure level p_{ref} close to the seafloor, are linearly proportional to variations in the dynamic height anomaly ΔD of the sea surface relative to that deep level. We also assume that the calibration may be frequency dependent and approach the problem in the frequency domain. Thus at some frequency $f > 0$,

$$\tilde{\tau}_{\text{ref}}(f) = \frac{1}{m(f)} \Delta \tilde{D}(f) \quad (1)$$

where m is called the calibration slope for consistency with Chiswell *et al.* [1986], and the tilde denotes the Fourier transform.

Since p_{ref} is close to the seafloor, the average density ρ_b , and

Fig. 2. Dynamic height anomaly relative to 1000 dbar, $\Delta D_{0/1000}$, as a function of synthesized travel time to the same level, $\tau_{0/1000}$, from all NORPAX CTD casts taken between 5.5° and 6.5°N. Slope m and r^2 from the linear regression are also given.

Fig. 3. IES calibration slope m ($\Delta D_{0/p_{ref}}$ versus $\tau_{0/p_{ref}}$), as a function of the lower reference pressure level, p_{ref} , for the equator at 110°W ; solid circles are from CTD casts; open circles show combined thermistor data from D. Halpern and R. Weisberg, with T - S curve derived from Mangum and Hayes [1983] (from L. Miller, personal communication, 1986).

the average speed of sound, c_b , below p_{ref} are assumed constant in time. The total travel time to the bottom, τ , is then

$$\tilde{\tau}(f) = \frac{1}{m(f)} \Delta \tilde{D}(f) + \frac{2}{c_b} \tilde{H}_2(f) \quad (2)$$

where H_2 is the geometric distance between the seafloor and the reference pressure level. H_2 is constant only if the ocean is baroclinically compensated; in general it varies according to

$$H_2(t) = \eta(t) + H_3 - H_1(t) \quad (3)$$

where η is sea level, H_1 is the geometric distance between the reference pressure level and the sea surface, and H_3 is the mean depth. Since H_3 is a constant, the Fourier transform of (3) is

$$\tilde{H}_2(f) = \tilde{\eta}(f) - \tilde{H}_1(f) \quad (4)$$

From the definition of dynamic height [Neumann and Pierson, 1966], H_1 is given by

$$H_1 = \frac{10}{g} D = \frac{10}{g} (\Delta D + D_{std})$$

where g is the acceleration due to gravity, ΔD is the dynamic height anomaly and D_{std} is the standard-ocean (0° , 35%) dynamic height. Because D_{std} is constant,

$$\tilde{H}_1(f) = \frac{10}{g} \Delta \tilde{D}(f) \quad (5)$$

Substituting (4) and (5) into (2) yields

$$\tilde{\tau}(f) = \left(\frac{1}{m(f)} - \frac{20}{gc_b} \right) \Delta \tilde{D}(f) + \frac{2}{c_b} \tilde{\eta}(f) \quad (6)$$

A similar equation can be obtained for pressure. The pressure at the bottom, p , is (in decibars)

$$p = p_{ref} + 10^{-4} \rho_b g H_2$$

so that

$$\tilde{p}(f) = 10^{-4} \rho_b g \tilde{H}_2(f) \quad (7)$$

Substituting (4) and (5) into (7) gives

$$\tilde{p}(f) = 10^{-4} \rho_b g \tilde{\eta}(f) - 10^{-3} \rho_b \Delta \tilde{D}(f) \quad (8)$$

Equations (8) and (6) can be recast as

$$\alpha \tilde{p}(f) = \tilde{\eta}(f) - \beta \Delta \tilde{D}(f) \quad (9)$$

$$\tilde{\tau}(f) = \gamma \tilde{\eta}(f) - \delta(f) \Delta \tilde{D}(f)$$

Equations (9) can be rearranged to express the dynamic height field in terms of two linear combinations of τ , η , and p :

$$\begin{aligned} \Delta \tilde{D}(f) &= [\tilde{\eta}(f) - \alpha \tilde{p}(f)] / \beta \\ \delta(f) \Delta \tilde{D}(f) &= \gamma \tilde{\eta}(f) - \tilde{\tau}(f) \end{aligned} \quad (10)$$

where

$$\alpha = \frac{10^4}{\rho_b g} \quad \beta = \frac{10}{g} \quad \gamma = \frac{2}{c_b} \quad \delta(f) = -\left(\frac{1}{m(f)} - \frac{20}{gc_b} \right)$$

Equations (10) can be regarded analogous to a linear response system [Jenkins and Watts, 1968] with $\gamma\eta - \tau$ as the response to ΔD or $(\eta - \alpha p)/\beta$ with a transfer function $\delta(f)$, so that in the time domain, $\gamma\eta - \tau$ is the convolution of ΔD with the inverse Fourier transform of δ .

This model has implicitly assumed negligible atmospheric pressure effects. Appendix A presents the modifications required to incorporate atmospheric pressure fluctuations in the model, for regions where this is necessary.

5. INTERCOMPARISON

Since atmospheric pressure was not available for Palmyra Island, sea level was computed from the measured shallow pressure, assuming that atmospheric pressure fluctuations were relatively small. This assumption was confirmed by at-

Fig. 4. Schematic diagram of relationships between dynamic height, travel times, sea level, and pressures (see text).

Fig. 5. Band-passed (-40 -dB points at 36 hours and 856 days) time series of travel time τ , sea level η , and bottom pressure p , taken from the 6°N IES and Palmyra Island sites.

mospheric pressure measurements at Christmas Island (see Appendix A).

The time series of τ , η , and p and of the resulting series $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$ are shown in Figures 5 and 6 (data analysis details are given in Appendix B). A failure of the Paroscientific Digiquartz sensor in the Palmyra Island pressure gauge caused a gradual long-term drift in the sea level record. For this reason, the time series are shown as band-passed time series (upper and lower -40 dB points at 36 hours and 856 days, respectively). The records of $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$ (Figure 6) are visually well correlated, with the dominant 35 to 40-day waves appearing quite similar.

To compare the contributions of each term in $\gamma\eta - \tau$ and $(\eta - \alpha p)/\beta$, we have plotted, in Figure 7, the spectra of τ/γ , η , and αp . The spectra show that $\gamma\eta$ contributes only about 1% of the variance of $\gamma\eta - \tau$ and that the deep pressure p influences $(\eta - \alpha p)/\beta$ strongly only at 2-week period (principally Mf tide, which here appears broadened by the spectral analysis), and (to a lesser degree) at 5-day period. Otherwise, p generally contributes about 10% to the variance of $(\eta - \alpha p)/\beta$.

Fig. 7. Spectra of τ/γ , η , and αp . Vertical guidelines are drawn at indicated periods (in days) for comparison with other figures. The 95% confidence limits are drawn for the number of degrees of freedom as indicated.

The spectra of $\gamma\eta - \tau$ and $(\eta - \alpha p)/\beta$, shown in Figure 8, illustrate the elimination of the barotropic signal in (10), by the absence of Mf tidal peaks at 13.7 days despite their strong presence in the p and η records (Figure 7). The two spectra in Figure 8 are very similar: both show peaks with magnitudes comparable to the 95% confidence interval at 40, 10, 5, 4, and 3 days, indicating strong baroclinic signals at these periods.

The coherence squared between $\gamma\eta - \tau$ and $(\eta - \alpha p)/\beta$ (Figure 9) is almost always greater than the 95% significance level and exceeds the 99.9% significance value in bands coinciding with spectral peaks. However, it is not 1.0, indicating that some of the variance is uncorrelated between the two variables. Apart from inadequacies in the assumption of a linear dependence of τ on ΔD , this could be caused by the 70-km separation of the IES and shallow pressure gauge (i.e., this "noise" is attributable to short-wavelength processes and island effects).

Fig. 6. Band-passed (-40 -dB points at 36 hours and 856 days) time series of $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$.

Fig. 8. Spectra of $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$. Spectral units are $(\text{dyn m})^2 \text{cpd}^{-1}$ and $\text{s}^2 \text{cpd}^{-1}$, respectively; the spectrum of $\gamma\eta - \tau$ has been raised by 3 decades to facilitate comparison of the two spectra. Vertical guidelines and 95% confidence limits are as in Figure 7.

Since η was measured in an island lagoon 70 km from the deep-sea measurements of τ and p , neither $\gamma\eta - \tau$ nor $(\eta - \alpha p)/\beta$ will precisely represent the true values at the IES site. Consequently, both $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$ have some noise associated with them, and our analysis is that of a linear response system with noisy measurements of both “input” and “output” signals (see Appendix B).

The calibration slope m , computed from δ , is plotted in Figure 10 at frequencies corresponding to peaks in the coherence squared. The indicated limits on m are computed from Monte Carlo simulations of the expected fifth and ninety-fifth percentile values of the distribution of δ .

At periods of near 40 days, m is $-65 \pm 9 \text{ dyn m s}^{-1}$, in excellent agreement with the depth-extended CTD-derived calibration of -66 dyn m s^{-1} (section 2). These 40-day oscillations are seen in Figure 5 to have the largest amplitude, with about the same peak-to-peak range in dynamic height as the range in the CTD data ($\sim 0.3 \text{ dyn m}$, Figure 2). This suggests

Fig. 9. Coherence squared between $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$. Vertical guidelines are as in Figure 7; horizontal lines are levels of 95 and 99.9% significance.

Fig. 10. IES calibration slope m , derived from equation (10) at periods where peaks occur in the coherence squared. Error bars are expected fifth and ninety-fifth percentile values based on Monte Carlo simulations of a linear response system with noise at both input and output. The solid horizontal line is the depth-extended CTD-derived calibration slope, -66 dyn m s^{-1} ; dashed lines are 2 standard deviations from this estimate.

that the predominant contribution to the CTD-derived calibration may well have been similar 40-day variability, and this would explain the good agreement at low frequency between the two methods.

There is some evidence that m changes with frequency. The general trend is for the magnitude of m to increase with increasing frequency. At periods of 10, 3, and 2 days, m is significantly greater than the CTD-derived value, at most about 50% greater. The trend is not monotonic, however: at 4- and 5-day periods, m does not differ significantly from the CTD-derived value.

This apparent frequency dependence of m suggests that oscillations in different frequency bands do have different vertical structure. The 40-day period waves are presumably examples of the 20- to 80-day period oscillations observed by *Mitchum and Lukas* [1987], who attribute them to baroclinic instabilities in the equatorial current system having synoptic spatial scale [*Legeckis*, 1977]. Our data agree with previous observations that these “synoptic” oscillations have largest amplitude in October and November [*Lukas*, 1982]. The 10-day waves are probably equatorially trapped Rossby-gravity waves similar to those seen in the eastern equatorial Pacific by *Chiswell et al.* [1987], whereas the 5-, 4-, 3- and 2-day waves fall in the equatorially trapped inertia-gravity wave band and are probably different meridional modes of these waves.

6. SUMMARY AND CONCLUSIONS

Until now, the justification for using inverted echo sounders to measure baroclinic processes has relied heavily on temporally discrete CTD or expendable bathythermograph observations, and the assumption that the resulting calibration is applicable at all frequencies. Here (for the first time) we make a direct comparison of dynamic height derived from travel time with that derived independently from sea surface elevation and bottom pressure.

We have presumed that the differences between $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$ arise predominantly through inadequacies of the assumption that τ and ΔD are linearly related as in (1). But

noise in the measurements of η , τ , and p (some of it from topographic and physical separation effects; see Appendix B) also contributes to these differences.

The variable $(\eta - \alpha p)/\beta$ removes the barotropic component from the sea surface signal and is a precise measure of dynamic height (to the extent that η accurately represents the open ocean sea level), since its derivation requires only the assumption that the near-bottom density is constant in time; the coefficients α and β depend only on ρ_b and g and are easily determined. The variable $\gamma\eta - \tau$ incorporates a correction for sea level changes to the assumption that τ follows ΔD , but this correction is small (the variance of η is generally 2 decades lower than that of τ/γ). Thus $\gamma\eta - \tau$ and $(\eta - \alpha p)/\beta$ are practically independent measurements. Consequently, two factors confirm that $\gamma\eta - \tau$ can be used to measure ΔD : the very similar nature of the spectra of $\gamma\eta - \tau$ and $(\eta - \alpha p)/\beta$ (Figure 8) and the greater than 99.9% confidence in the coherence between the two variables at the spectral peaks (Figure 9).

It is clear that in certain bands, sea level is affected significantly by barotropic processes; these bands are not limited to those where one might a priori expect dominantly barotropic signals (e.g., at the *Mf* tidal period). A comparison of Figures 7 and 8 shows that near 5- and 4-day periods the spectrum of τ/γ is closer to the dynamic height spectrum (i.e., $(\eta - \alpha p)/\beta$) than is the spectrum of η . In these bands, then, even with the inherent uncertainty in IES calibration, acoustic travel time provides a better measure of dynamic height than does sea level.

This paper has presented a method for comparing dynamic height measured from acoustic travel time with that obtained from island sea level. In principle, varying mixtures of vertical modes could produce a frequency dependent IES calibration, $m(f)$, but this does not appear to have occurred to a significant extent during this deployment. At long periods, m derived from the IES-pressure gauge comparison agrees well with the CTD-derived slope extended to 4000 m (though the applicability of the extension is otherwise uncertain). There is some evidence that m depends on the processes leading to the variability, with higher-frequency dynamics having steeper calibration slopes; however, it appears that using the low-frequency value would underestimate the amplitude of these processes by at most 30%.

APPENDIX A: INCLUSION OF ATMOSPHERIC PRESSURE

Atmospheric pressure was not measured at Palmyra Island. However, it was measured at Christmas (Kiritimati) Island (2°N, 157°30'W), about 700 km to the southeast of Palmyra Island, coincident with the IES observations (except for the first month and for 25 days in August and September 1985 (P. Freitag, personal communication, 1986). Over large distances in the tropics, atmospheric pressure fluctuations are similar at periods of days [Brier and Simpson, 1969] to weeks [Madden and Julian, 1972], so that Christmas Island pressure may be used in the following order of magnitude estimate to show that ignoring atmospheric pressure has negligible effect for our deployment.

The bottom pressure p_b is the sum of the hydrostatic pressure p and atmospheric pressure p_a . Dropping the frequency dependence for simplicity,

$$p_b = p + p_a$$

Similarly, the measured shallow pressure p_s includes atmospheric variations

$$p_s = 10^{-4} \rho_s g \eta + p_a$$

or

$$\eta = \frac{(p_s - p_a)}{10^{-4} \rho_s g} \quad (\text{A1})$$

where ρ_s is the density near the surface.

Equations (9) then become

$$\begin{aligned} \alpha p_b &= \eta - \beta \Delta D + \alpha p_a \\ \tau &= \gamma \eta - \delta D \end{aligned}$$

Rearranging terms, substituting for η from (A1), and writing $\varepsilon = \rho_b/\rho_s - 1$, gives

$$\begin{aligned} \Delta D &= \left[\frac{p_s}{10^{-4} \rho_s g} - \alpha(p_b + \varepsilon p_a) \right] / \beta \\ \delta \Delta D &= \gamma \frac{(p_s - p_a)}{10^{-4} \rho_s g} - \tau \end{aligned} \quad (\text{A2})$$

Since atmospheric pressure was ignored earlier, η in (10) is the same as $p_s/(10^{-4} \rho_s g)$ in (A2). The differences between (10) and (A2) are thus the replacement of p_b by $(p_b + \varepsilon p_a)$ and the replacement of p_s by $p_s - p_a$.

Christmas Island atmospheric pressure fluctuations had a peak-to-peak range of 0.07 dbar, compared with about 0.3 dbar in the shallow pressures and 0.1 dbar in the deep pressures at 6°N (see Figure 5). A CTD cast made at the IES deployment shows $\rho_s = 1.022 \times 10^3 \text{ kg m}^{-3}$ and $\rho_b = 1.044 \times 10^3 \text{ kg m}^{-3}$, so that $\varepsilon = 0.022$. Thus, fluctuations in εp_a are about 2 orders of magnitude less than those of p_b , already small compared with p_s (section 5). Similarly, since the amplitude of $\gamma\eta$ is an order of magnitude less than that of τ and since p_a has only one-fifth the fluctuation amplitude of p_s , replacing p_s with $p_s - p_a$ has little overall effect.

This argument demonstrates that the influence of p_a on the total variance of dynamic height is negligible; however, at some individual frequency the effect could be significant. Consequently, spectra of ΔD and $\delta \Delta D$ were computed according to (A2) but were visually indistinguishable from the spectra computed according to (10), when plotted as in Figure 8.

APPENDIX B: DATA ANALYSIS

The 6°N data were first treated for the removal of tides by the response analysis method of Munk and Cartwright [1966]. The deep pressure record was corrected for the small temperature sensitivity of the pressure sensor and then detrended with an exponential trend in accordance with Watts and Kontoyannis [1986]. The series were then band-pass filtered by subtracting very low pass filtered series from low-pass filtered series using a Gaussian filter. The resulting filter has its upper and lower -40-dB points at 36 hours and 856 days. At 5.5-, 4-, 3-, and 1-day periods, the filter reduces by -3, -6, -10, and -90 dB, respectively. The lower -3-dB point is at 80 days; at 365-day periods the filter reduces by -25 dB.

Spectra were computed using the weighted overlapped-segment averaging method [Welch, 1967] combined with band averaging at the higher frequencies. This allows higher resolution at low frequencies and improved statistics at high frequencies. The spectra shown in Figures 7 and 8 are "recolored" to compensate for the effects of filtering. Expressions for the number of degrees of freedom and 95% confidence limits

were obtained from Koopmans [1974], Welch [1967], and Thompson [1979].

Equations (10) can be regarded analogous to a linear response system [Jenkins and Watts, 1968] with $(\eta - \alpha p)/\beta$ as the input, $\gamma\eta - \tau$ as the output, and $\delta(f)$ as the transfer function. However, neither $\gamma\eta - \tau$ nor $(\eta - \alpha p)/\beta$ is physically a direct response to the other (the link is the assumption that τ and ΔD are linearly related). Our measurements of η were made in an island lagoon 70 km from our measurements of p and τ . These measurements consequently contain noise associated with the separation and, in the case of η , noise from topographic effects (such as wind setup in the lagoon). Our analysis is thus that of a system having noise in the measured input x ,

$$x = (\eta - \alpha p)/\beta + e_x$$

and in the measured output y ,

$$y = \gamma\eta - \tau + e_y$$

where e_x and e_y are uncorrelated with $(\eta - \alpha p)/\beta$ and $\gamma\eta - \tau$. The best estimate of the transfer function δ is then given by

$$\delta = \sqrt{(S_y/S_x)} \quad (\text{B1})$$

where S_x and S_y are the measured spectra of x and y , respectively.

The limits on m shown in Figure 10 were estimated from Monte Carlo simulations of the limits on δ computed for our processing. In these simulations a linear response system was set up with a known transfer function. Both input and output were contaminated with Gaussian white noise with the same signal-to-noise ratio, and the transfer function was computed according to equation B1. These simulations show that equation B1 correctly computes δ and that the limits on δ depend on the amount of noise present. This noise was estimated from the observed coherence between x and y assuming equal signal-to-noise ratios for each variable.

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