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Global Evaluation of Particulate Organic Carbon Flux Parameterizations and Implications for Atmospheric pCO₂

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Key words: Biological pump, POC flux, ballast hypothesis, Martin curve

Key points:
- Three parameterizations for particulate organic carbon (POC) export are compared to global data.
- POC fluxes estimated from the Martin curve and the ballast hypothesis capture observations equally well at all depths.
- Globally, data constrain Martin’s b to a range from 0.70 to 0.98. This range could modify atmospheric pCO₂ by only tens of ppm.
Abstract

The shunt of photosynthetically derived particulate organic carbon (POC) from the euphotic zone and remineralization at depth comprises the basic mechanism of the “biological carbon pump.” POC raining through the “twilight zone” (euphotic depth to 1 km) and “midnight zone” (1 km to 4 km) is remineralized back to inorganic form through respiration by heterotrophs and bacteria. Accurately modeling POC flux is critical for understanding the “biological pump” and its impacts on air-sea CO₂ exchange and, ultimately, long-term ocean carbon sequestration. Yet, the parameterizations of POC flux commonly used in simulations have not been tested quantitatively against global datasets using the same modeling framework. Here, we use a single one-dimensional physical-biogeochemical modeling framework to assess the skill of three common POC flux parameterizations in capturing POC flux observations from moored sediment traps and thorium-234 depletion. The exponential decay, Martin curve, and ballast model are compared to data from 11 biogeochemical provinces distributed across the globe. In each province, the model captures satellite-based estimates of surface primary production within uncertainties. Goodness-of-fit is measured by how well the simulation captures the observations, quantified by bias and the root-mean-squared-error and displayed using “target diagrams.” Comparisons are presented separately for the twilight zone and midnight zone. We find the parameterization based on the ballast hypothesis shows no improvement over a globally or regionally parameterized Martin curve. For all provinces taken together, Martin’s $b$ that best fits the data is [0.70, 0.98]; this finding reduces by at least a factor of 3 previous estimates of potential impacts on atmospheric pCO₂ of uncertainty in POC export to a more modest range [-16 ppm, +12 ppm].
1. Introduction

The biologically-mediated removal of organic carbon from surface waters against a dissolved inorganic carbon (DIC) gradient and its subsequent remineralization at depth is termed the “biological pump” \cite{Broecker1982, DeLaRocha2006}, which can be separated into a “carbonate pump” and a “soft-tissue pump” \cite{Volk1985} as well as a “microbial pump” \cite{Jiao2010a}. The percentage of net primary production (NPP) exported from the euphotic zone as particulate organic carbon (POC) is at least 5%, with some estimates higher than 40\% \cite{Martin1987, Buesseler1998, Schlitzer2000, Boyd2007, Buesseler2009, Henson2011}. Much of this material is respired, primarily by bacteria and zooplankton, within the “twilight zone” (euphotic depth to 1000 m) \cite{Steinberg2008}; only ~3\% of exported NPP reaches the 1000 m depth horizon \cite{DeLaRocha2007a}. On timescales of days to weeks the flux of POC is controlled by sinking speed and degradation rate. If in steady state, POC flux should be balanced by the input of limiting nutrients to the euphotic zone \cite{Passow2012, Giering2017a}. POC flux to depth is the hallmark of the biological pump, and is critical to setting surface ocean pCO$_2$ \cite{Parekh2006, Kwon2009, Kwon2011, Devries2012a}. The pCO$_2$ gradient across the air-sea interface determines the direction of carbon flux across the surface. By converting DIC to organic carbon, biological activity reduces surface ocean pCO$_2$ and promotes CO$_2$ uptake by the ocean. The downward POC flux then sequesters carbon at depth. Changes in the efficiency of the biological pump, measured as the ratio of exported POC to primary
production has the potential to alter ocean carbon storage and atmospheric CO$_2$

[Marinov et al., 2008a, 2008b; Kwon et al., 2009; Henson et al. 2011]. Parekh et al. (2006) estimate the atmospheric pCO$_2$ would be 150-200 $\mu$atm greater than the current value if not for the biological control on the vertical DIC gradient. Kwon et al. [2011] separate the sensitivity of atmospheric CO$_2$ to changes in the carbonate pump versus the soft-tissue pump. They find that for a globally-averaged respired carbon increase of 10 $\mu$mol kg$^{-1}$, the carbonate pump increases atmospheric CO$_2$ by about 3.4% while the soft-tissue pump decreases atmospheric CO$_2$ by 5.3%, thus there is a net 2% reduction in atmospheric CO$_2$ when both pumps are accounted for.

Projections using earth system models show a sizeable uncertainty across various models with respect to the biological pump’s response to 21st century climate change [Bopp et al., 2013; Laufkötter et al., 2015; Hauck et al., 2015; Krumhardt et al. 2016]. Accurate estimation the sensitivity of the biological pump to future climate change is critical to economic evaluations of the impacts of climate change on ecosystem services [Barange et al., 2017]. Parameterizations used in earth system models would ideally capture both the mean POC attenuation and the variability found in available observations, and do so in a mechanistically-realistic manner, in order to reliably predict future change in the strength and efficiency of the biological pump.

Early parameterizations of POC flux relate export either at a reference depth [Martin et al., 1987] or the euphotic zone primary production [Suess, 1980; Betzer et al., 1984; Pace et al., 1987] to the vertical POC flux through an empirically-derived relationship. Although these parameterizations lack mechanistic realism, the Martin et al. [1987] power law parameterization, in some cases with adjustment to different
ocean regions [Henson et al. 2012; Guidi et al. 2015], has been used widely to predict carbon flux >2000m [François et al., 2002; Honjo et al., 2008]. Alternative to a power law parameterization, an exponential curve has been used to describe attenuation through an empirical fit to observations [Lutz et al., 2002; Boyd and Trull, 2007; Marsay et al., 2015]. Parameterizations assuming first-order kinetics and a constant sinking speed have been used in biogeochemical models [Walsh et al., 1988; Banse, 1990; Dutkiewicz et al., 2005; DeVries and Weber, 2017], which implies an exponential decay of POC. More mechanistic parameterizations, such as those based on the “ballast hypothesis” [Armstrong et al., 2002] assume minerals associated with POC increase the POC flux at depth, have been proposed.

To directly compare the various choices available for POC parameterization, a global dataset with consistent treatment and a consistent model framework is required. The choice of seasonal normalization in datasets [Lutz et al., 2002; Lutz et al., 2007; Honjo et al., 2008] can impact statistical fits, and simulated POC fluxes are dependent both on the POC flux parameterization, and also on the simulated surface ocean productivity. In a previous model-data comparison, Howard et al. [2006] used a three-dimensional ocean model in which surface NPP responds to the POC parameterization. They find that the ballast model captures observations more accurately than the Martin curve, and that the geochemical distribution in the deep ocean is sensitive to the parameterization used. However, there has not yet been a comparison across all three common parameterizations in which the modeling framework is identical, including identical surface NPP and POC production to drive the vertical fluxes estimated by each parameterization.
In this study, we compare three common POC flux parameterizations using a single one-dimensional numerical modeling framework in which NPP is not responsive to the parameterization used; i.e. each parameterization is driven by the same surface POC source. This model is applied in 11 Longhurst [2006] provinces for which adequate POC flux data are available (Figure 1). We quantitatively evaluate, using a suite of statistical tests, the exponential decay model, Martin curve, and the ballast hypothesis against the recently released global POC flux dataset [Mouw et al., 2016a] that consists of POC flux observations from sediment traps supplemented with thorium-234 depletion observations (2% of the data) spanning years 1976 to 2012.

2. Methodology

2.1 Model Description

The Massachusetts Institute of Technology general circulation model (MITgcm) [Marshall et al., 1997a, 1997b] is configured as a one-dimensional column with 77 vertical layers. Depths increase from a resolution of 10m in the surface to 650m in the deepest layer. K-profile parameterization (KPP) simulates vertical mixing [Large et al., 1994]. The model uses a nutrient-restoring scheme with a relaxation time scale of 30 days to approximate advection and diffusive processes that are not directly simulated. Nutrients are restored towards the climatology appropriate for each province in the euphotic zone when the simulated nutrient concentration falls below the climatological value, while nutrients below the euphotic zone are constantly restored towards climatology. Sediments are not included in the model, and thus detritus slowly accumulates in the bottom grid cell; the bottom grid cell is ignored in analyses.
The model is initialized with physical and biogeochemical observations and forced at
the surface with monthly climatological meteorological and radiative fields
appropriate for each province. Temperature, salinity, and nutrients are prescribed by
World Ocean Atlas 2013 [Boyer et al., 2013]. Alkalinity and DIC are prescribed
using GLObal Ocean Data Analysis Project (GLODAP) atlas [Key et al., 2004].
Photosynthetically active radiation (PAR) is prescribed using Sea-viewing WIde
Field-of-view Sensor (SeaWIFS) data [Frouin et al., 2002]. Surface dust deposition
is provided by Mahowald et al. [2005]. Surface wind stress is prescribed using
National Center for Environmental Prediction (NCEP) reanalysis 1 [Kalnay et al.,
1996].

The ecosystem model embedded in MITgcm is that of Dutkiewicz et al. [2005]. The
model includes two phytoplankton functional groups (diatoms and small
phytoplankton) and one zooplankton class. Phytoplankton growth can be light and
nutrient limited. Mortality rate and maximum growth rates of diatoms and small
phytoplankton are tuned for each province (supplementary Table S1) to best fit
satellite-based estimates of primary productivity (Table 1). The remineralization rate
\((k)\) is set to 1/10 d\(^{-1}\) for POC and 1/150 d\(^{-1}\) for biogenic silica (opal). The dissolution
rate for particulate inorganic carbon (PIC) is 1/300 d\(^{-1}\). The sinking speed \((w)\) for
POC, PIC, and opal are fixed constants: POC and opal sink at a rate of 10 m d\(^{-1}\) while
PIC sinks at 15 m d\(^{-1}\). These POC sinking speeds lie within the range of other
models, 2.5 m d\(^{-1}\) [Yool et al., 2010], 8 m d\(^{-1}\) [Dutkiewicz et al., 2005], 11-85 m d\(^{-1}\)
[DeVries and Weber., 2017]. The POC remineralization rate and sinking speed used
here imply a remineralization length scale \((\lambda = wk^{-1})\) of 100 m, similar to the Lima
et al. [2014] value of 130 m and within the range assumed by Moore et al. [2004].
This remineralization length scale is within the 50-200 m range that Mouw et al. [2016b] found for most provinces, and the 69-265m range derived from the optimization of DeVries and Weber [2016].

The model assumes 7% of phytoplankton are calcifiers, and therefore produce PIC. Production of POC, PIC, and opal are due to mortality of phytoplankton and zooplankton, as well zooplankton grazing on phytoplankton. The tendency of POC, PIC, and opal production are shown below:

\[
\frac{d[X_{prod}(z)]}{dt} = P_{X_{prod}}^p(z) + Z_{X_{prod}}^p(z) \tag{1}
\]

where \(X=\text{POC, PIC, or opal}\). \(P_{X_{prod}}^p(z)\) represents production of \(X\) (mgX m\(^{-2}\) d\(^{-1}\)) at depth \((z, m)\) by phytoplankton (P) and \(Z_{X_{prod}}^p(z)\) represents production of \(X\) (mgX m\(^{-2}\) d\(^{-1}\)) at depth \((z, m)\) by zooplankton (Z).

A 10-year simulation is run after a 10-year model spin up. The model uses a time step of 200 seconds with an 8-day averaging period. This averaging period is chosen to coincide with the time step of the vertically integrated production model (VGPM) [Behrenfeld and Falkowski, 1997] which is used for comparison to modeled NPP. VGPM satellite-based NPP estimates are obtained from http://www.science.oregonstate.edu/ocean.productivity/ and the modeled NPP is calculated as the integrated productivity in the euphotic zone.

### 2.3 Exponential Decay Model

The exponential decay model assumes that all the POC is labile with a constant sinking speed, expressed in equation (2) [Banse, 1990].
\[
F(z) = w_{poc}[POC(z)] \quad (2)
\]

where \(F(z)\) is the POC flux (mgC m\(^{-2}\) d\(^{-1}\)) at depth \((z, \text{m})\), \(w_{poc}\) is the sinking speed of labile POC (m d\(^{-1}\)), and \([POC(z)]\) is the volume concentration of labile POC (mgC m\(^{-3}\)) at depth. The tendency of POC to sink and remineralize is expressed in the following form:

\[
\frac{d[POC(z)]}{dt} = w_{poc} \frac{d[POC(z)]}{dz} - k_{poc}[POC(z)] \quad (3)
\]

where the first term represents vertically sinking POC while the second term represents a first-order remineralization scheme where POC is instantly remineralized at each depth level \((z)\) with \(k_{poc}\) being the remineralization rate. An expression for the flux of labile POC is derived by applying equation (2) to a steady state version of equation (3): \(F(z) = F(z_o)EXP[(z - z_o)/\lambda]\), where \(F(z_o)\) is the flux at reference depth \(z_o\) and \(\lambda = \frac{w_{poc}}{k_{poc}}\) is the remineralization length scale (e-folding length scale).

Table 2 provides definitions of all equation parameters.

The ecosystem model of Dutkiewicz et al. [2005] treats particulate organic matter as exponentially decaying throughout the water column and assumes all POC is labile. The full tendency of POC is defined in equation (4):

\[
\frac{d[POC(z)]}{dt} = \frac{d[POC^{prod}(z)]}{dt} + w_{poc} \frac{d[POC(z)]}{dz} - f_T k_{poc}[POC(z)] \quad (4)
\]

where the first term is the tendency of POC production (equation (1)) and the last two terms represent sinking and remineralization (equation (3)). Temperature dependence on remineralization rate is taken into account through an Arrhenius function: \(f_T = A * EXP[T_{AE} (T^{-1} - T_{ref}^{-1})]\), where \(A, T_{AE},\) and \(T_{ref}\) are constants and \(T\) is the local temperature (supplementary Table S2). POC flux at each level is calculated using
equation (2). This framework will be termed the “exponential decay model” for POC flux.

2.4 Martin Curve

Using data obtained from free-floating sediment traps, Martin et al. [1987] describe POC flux attenuation using a normalized power function of the following form, commonly referred to as the “Martin curve”:

\[ F(z) = F(100) \left( \frac{z}{100} \right)^{-b} \] (5)

where \( F(100) \) is the POC flux at 100m and \( b \) is the flux attenuation coefficient. The Martin curve is equivalent to a decreasing remineralization rate with depth or an increasing sinking speed with depth [Lam et al., 2011]. Villa-Alfageme et al. [2016] observed an increase in sinking speed with depth, possibly due to the gradual loss of slow-sinking particles with depth. Small values of \( b \) imply a higher transfer efficiency where more carbon remineralizes at deeper depths. Transfer efficiency is defined as the fraction of exported organic matter that reaches a given depth below the depth of export, with 100 m below the depth of export being where transfer efficiency is typically estimated [Buesseler and Boyd, 2009]. Transfer efficiency and \( b \) are inversely related: large values of \( b \) imply a small transfer efficiency with more carbon remineralizing at shallower depths. Martin et al. [1987] calculated a global \( b \) value of 0.858 using observations from nine locations in the Northeast Pacific.

Regional variations in the \( b \) parameter have been found to improve the statistical fits at the scale of ocean provinces [Henson et al., 2012; Guidi et al., 2015] and across ocean basins [Berelson, 2001; Schlitzer, 2002], implying regional variability in the flux attenuation and transfer efficiency. Marsay et al. [2015] showed the \( b \) parameter, and hence the flux attenuation, correlates with temperature. This pattern is plausibly
explained by a slowdown of microbial utilization of carbon as temperature decreases
[Pomeroy and Diebel, 1986; Pomeroy et al., 1991]. Changes in $b$, when applied
globally in a biogeochemical model, have been shown to significantly impact
atmospheric CO$_2$ concentrations [Kwon et al., 2009].

In this study, POC fluxes at depth based on the Martin curve are calculated offline
from surface production in MITgcm. In keeping with the original intent of the Martin
curve, we use equation (5) to calculate the flux at each depth level ($z$) using an export
depth of 100 m and export flux, $F(z_{100})$, from the exponential decay model runs.
Due to nutrient restoring below the euphotic zone, feedback of shallow
remineralization on surface production is negligible; thus, this approach is robust.
Runs with both the Martin et al. [1987] global $b$ value of 0.858 as well as the Guidi et
al. [2015] and Henson et al. [2012] regional $b$ values are performed for comparison.

2.5 Ballast Hypothesis

The ballast hypothesis proposed by Armstrong et al. [2002] asserts that “ballast”
minerals (PIC, opal, and dust), qualitatively associated with POC, increase the deep
ocean POC flux. Using observations from the equatorial Pacific, Armstrong et al.
[2002] observed that the ratio of organic carbon flux to total mass flux was nearly
constant below 1800 m and concluded ballast minerals are intimately related to the
POC flux. Mechanistically, the role of ballast minerals is not entirely clear. It has
been proposed that they act to increase the sinking speed and/or protect POC from
microbial respiration and zooplankton grazing. Thus, POC that is associated with
ballast minerals induces a higher transfer efficiency, delivering more POC to depth.
The ballast hypothesis asserts that sinking POC is a composed of “free” and ballast
mineral associated fractions (supplementary Figure S1). The free fraction has a
remineralization length scale as labile POC while POC qualitatively associated with
ballast minerals is partitioned between a “soft” and “hard” subclass, which represent
external and internal protection mechanisms, respectively [Armstrong et al., 2002].
External protection constitutes physical removal from hydrolyzing enzymes by
adsorption of POC into mineral micropores and increasing sinking speed [Mayer,
1994]; POC associated with the soft fraction has the same remineralization profile as
its associated ballast mineral. Internal protection occurs when POC is encased in PIC
or opal, sheltering it from degradation until the mineral has dissolved [Armstrong et
al., 2002; and references therein]. For this reason, the hard fraction has a very deep
remineralization length scale, representing refractory POC. However, Iversen and
Robert [2015] concluded that ballast minerals act only to increase sinking speed and
do not provide any protection to organic matter.

Klaas and Archer [2002] used a global dataset of sediment trap observations in the
midnight zone to distinguish three forms of ballast with the following carrying
capacities (grams of organic carbon per gram of ballast): PIC (0.094), opal (0.025),
and dust (0.035). Additionally, Klaas and Archer [2002] observed 80% of the POC
flux to the seafloor was associated with PIC, suggesting it is a more efficient ballast
mineral compared to opal and dust. There are three reasons why the carrying capacity
of PIC has been suggested to be greater than that of opal and lithogenic dust:
1. PIC sinks ~50% faster than opal for an equivalent particle radius [Sarmiento
and Gruber, 2006], since the density of PIC (2.71 g cm\(^{-3}\)) is ~30% greater than
the density of opal (2.1 g cm\(^{-3}\)) [Klaas and Archer, 2002].
2. Opal production and export is not as spatially uniform as PIC production and export [Sarmiento and Gruber, 2006]. The ratio of opal flux to carbon flux also varies regionally [Ragueneau et al., 2000 Figure 5].

3. Lithogenic fluxes are generally too small to significantly impact the transfer efficiency of organic carbon [François et al., 2002]. However, some studies find evidence that does not support PIC having a higher carrying capacity compared to opal or dust [De La Rocha et al., 2008] or show regional variability in the carrying capacity of each ballast mineral [Wilson et al., 2012; Pabortsava et al., 2017].

Published parameterizations for the ballast hypothesis have important differences: Moore et al. [2004] and Armstrong et al. [2002] include PIC, opal, and lithogenic material (dust) as ballast minerals while Yool et al. [2010] and Dunne et al. [2013] omit ballasting from dust. The reader is referred to Moore et al. [2004] and Lima et al. [2014] for a detailed description of the implementation of the ballast hypothesis in a three-dimensional ocean model with dust.

For this study, the ecosystem model of Dutkiewicz et al. [2005] is augmented to include ballasting from PIC, opal, and dust in a manner similar to that of Moore et al. [2004] and Lima et al. [2014]. The implementation of the ballast hypothesis is based on Armstrong et al. [2002] and assumes a portion of the POC production is associated with PIC and opal production and surface dust deposition. Flux of POC is calculated by multiplying the sinking speed by the concentration of POC associated with each mineral (equation (6)):
\[ F(z) = w_{poc}[POC(z)] + w_{pic}[POC_{pic}(z)] + w_{opal}[POC_{opal}(z)] + w_{dust}[POC_{dust}(z)] \]  

where \( w_X \) is the sinking speed of X=POC, PIC, opal, or dust, \([POC_Y(z)]\) is the concentration of POC associated with Y=PIC, opal, or dust, and \([POC(z)]\) is the concentration of free or labile POC. The tendency of POC associated with ballast mineral Y is separated into a hard and soft subclass (equation (7)):

\[
\frac{d[POC_Y(z)]}{dt} = \frac{d[POC_{Y\text{soft}}(z)]}{dt} + \frac{d[POC_{Y\text{hard}}(z)]}{dt} \tag{7}
\]

POC in the soft subclass decays exponentially with a remineralization rate as its associated ballast mineral while POC in the hard subclass decays exponentially with a very long remineralization rate; POC in each subclass has the same sinking speed as its associated ballast mineral. Each term in \( \frac{d[POC_{pic}(z)]}{dt} \) is defined in Table 3 and each term in \( \frac{d[POC_{opal}(z)]}{dt} \) is defined in Table 4. The source of dust in the model is from surface deposition \( (dust^{dep}, \text{mgDust m}^{-2} \text{d}^{-1}) \). POC associated with dust solely occurs in the surface grid cell \( (\Delta z_{surf}, m) \) and is separated into a hard and soft subclass which decay exponentially. Each term in the tendency equation for POC associated with dust \( \left(\frac{d[POC_{dust}(z)]}{dt}\right) \) is defined in Table 5. The tendency of free POC production is calculated by subtracting ballast associated POC from the total POC production:

\[
\frac{d[POC_{free}(z)]}{dt} = \frac{d[POC_{prod}(z)]}{dt} - \left[ \omega_{PIC} \left( \frac{d[PIC_{prod}(z)]}{dt} \right) + \omega_{opal} \left( \frac{d[opal_{prod}(z)]}{dt} \right) + \omega_{dust} \left( \frac{d[dust^{dep}, m]}{dt} \right) \right] + \omega_{opal} \left( \frac{d[opal_{prod}(z)]}{dt} \right) + \omega_{dust} \left( \frac{d[dust^{dep}, m]}{dt} \right)
\]

where \( \frac{d[X_{prod}(z)]}{dt} \) is the production of X=PIC or opal by phytoplankton and zooplankton (equation (1)) and \( \omega_Y \) is the POC carrying capacity for Y=PIC, opal, or dust. Each term in the tendency equation for free POC \( \left(\frac{d[POC(z)]}{dt}\right) \) is defined in Table 6.
2.6 Analysis

An 8-day climatology of POC flux within each province is created using the Mouw et al. [2016a] data compilation of in situ sediment trap and thorium-234 based measurements. PIC and opal fluxes are not analyzed due to insufficient spatial and temporal resolution in the field data. Dates are converted to day of year and aligned in time using the midpoint of the deployment. POC flux observations within each biogeochemical province as defined by Longhurst [2006] (provided by VLIZ [2009]) are aggregated and grouped by depth and day of year into 8-day segments.

Observations are then aggregated to the model vertical grid in order to quantitatively compare to model output. In order to be considered in our comparison, observations must be available at depths greater than 1000 m and the model must capture the surface ocean production in a manner consistent with satellite retrievals. Coastal provinces are omitted.

Model performance is assessed by investigating the model-data misfit, defined as

\[ \Delta(i) = \log[M(i)] - \log[O(i)] \]

where \( M(i) \) and \( O(i) \) represent the \( i \)th model prediction and \( i \)th observed value respectively. Each observation is log base 10 transformed to alleviate skewedness from large values. The water column is partitioned into the twilight zone (100-1000m) and midnight zone (1000-4000m), with each analyzed separately. For consideration of variability, the full range of variability for the model and observations across each zone is compared. A set of six summary statistics are used as univariate measures of model performance [Stow et al., 2009]:
1. Correlation: 
\[ r = \frac{\sum_{i=1}^{N} \left[ \log[M(i)] - \log[M(i)] \right] \left[ \log[O(i)] - \log[O(i)] \right]}{\left( \sum_{i=1}^{N} [M(i) - \bar{M}]^2 \sum_{i=1}^{N} [O(i) - \bar{O}]^2 \right)^{\frac{1}{2}}} \]

2. Root Mean Squared Difference: 
\[ \text{RMSD} = \left[ \frac{1}{N} \sum_{i=1}^{N} \Delta(i)^2 \right]^\frac{1}{2} \]

3. Bias: 
\[ B = \overline{\log[M(i)]} - \overline{\log[O(i)]} \]

4. Average Absolute Error: 
\[ \text{AAE} = \frac{\sum_{i=1}^{N} \left| \log[M(i)] - \log[O(i)] \right|}{N} \]

5. Model Efficiency: 
\[ ME = 1 - \frac{\sum_{i=1}^{N} \left( \log[M(i)] - \log[O(i)] \right)^2}{\sum_{i=1}^{N} \left( \log[O(i)] - \bar{O} \right)^2} = 1 - \left( \frac{\text{RMSD}}{s_O} \right)^2 \]

6. Reliability Index: 
\[ RI = 10^{\text{RMSD}} \]

The correlation (r) is a measure between -1 and 1 quantifying the degree to which the simulation and observations linearly vary. The correlation only expresses how well the simulation and observations vary together and does not account for systematic biases; a correlation of 1 does not preclude a mean offset between the simulation and observations. Additionally, this value is related to the coefficient of determination (r²), which expresses the variance explained by a linear regression.

Root mean squared difference (RMSD), bias (B), and average absolute error (AAE) are all measures of the discrepancy between the simulated and observed mean. Values near zero imply “good” model performance and large values imply “poor” model performance using these metrics. The modeling efficiency (ME) can be used as a transition value between good and poor model performance [Nash and Sutcliffe, 1970]. A skillful model by this metric has an ME value near one. Modeling efficiency is related to RMSD: 
\[ ME = 1 - \left( \frac{\text{RMSD}}{s_O} \right)^2 \]

where \( s_O \) is the observed variance. The reliability index (RI) quantifies the average factor by which the model differs from observations. For example, an RI of 2 implies the model predictions need to be multiplied by 2 in order to reconstruct the observations.
Model performance is visualized using normalized “target diagrams” [Jolliff et al., 2009]. Target diagrams visualize bias and variability together (Figure 2a), giving them an advantage over the commonly used “Taylor diagram” [Taylor, 2001], which summarizes only the variability. Normalized target diagrams are based on the following quadratic relationship:

\[
\left( \frac{\text{RMSD}}{s_0} \right)^2 = \left( \frac{B}{s_0} \right)^2 + \left( \frac{u\text{RMSD}}{s_0} \right)^2 \tag{8}
\]

where \( u\text{RMSD} = \frac{1}{N} \sum_{i=1}^{N} [\Delta(i) - B]^2 \) is the unbiased RMSD (or variance of the model-data misfit), which measures the degree to which the model captures the observed variance, bias (B) is a measure of how well the simulated mean captures the observed mean, and \( s_0 \) is the observed variance. Target diagrams provide a novel way of visualizing B and uRMSD on a single plot: bias (B) on the y-axis and unbiased RMSD (uRMSD) on the x-axis. The radial distance, \( \left( \frac{\text{RMSD}}{s_0} \right)^2 \), is related to the modeling efficiency (ME): \( \left( \frac{\text{RMSD}}{s_0} \right)^2 = 1 - ME \). ME is negative when the radial distance is greater than one and modeling efficiency is positive when the radial distance is less than one. Therefore, ME is visualized by plotting a circle with a radius of one on a normalized target diagram; skillful models are within the circle. Under- or over-estimation of the variability is quantified by multiplying uRMSD by the sign of the observed variance (\( s_0 \)) subtracted from the modeled variance (\( s_M \)). Equation (9) shows the relationship used to construct target diagrams presented in this manuscript, which is equivalent to equation (8):

\[
(1 - ME) = B^2 + u\text{RMSD}^2 \tag{9}
\]
where $B^* = \frac{B}{s_o}$ and $uRMSD^* = \frac{uRMSD}{s_o} \cdot \text{sign}(s_M - s_O)$. Normalized target diagrams allow the display of multiple models on a single plot. They also visualize how well each model captures the observed mean and variance along with the modeling efficiency (ME). Target diagrams have previously been used to assess satellite derived NPP estimates [Friedrichs et al., 2009; Saba et al., 2010; Saba et al., 2011; Lee et al., 2015], surface chlorophyll [Hofmann, 2008; Lazzari et al., 2012], and physical variables such as temperature and salinity [Hofmann, 2008; Pairaud et al., 2011].

The final component of our analysis is to determine the range of Martin’s $b$ that is globally consistent with POC flux observations; and then to use this range to constrain previous estimates of the potential sensitivity of atmospheric pCO$_2$ to uncertainty in the biological pump [Kwon et al. 2009]. The normalized bias ($B^*$), the vertical axis in normalized target diagrams, is our metric for best fit. As discussed in detail in section 3, the three parameterizations are better able to capture the observed mean POC flux rather than POC flux variability, motivating the choice of $B^*$ as a metric. For this analysis, the model is run for each province with a range of $b$ values from 0.40 to 1.40 (with increments of 0.01), the range of $b$ from Kwon et al. [2009]. $B^*$ is calculated using observations only in the midnight zone, and in both the midnight and twilight zones. A particular value of $b$ “accurately” captures the observed mean if the $B^*$ for that model is within the range [-1,1] (supplementary Figure S2). The best-fit global $b$ range is taken as the interquartile range of all province-specific $b$ values. Atmospheric pCO$_2$ as a function of $b$ is taken from the global 3-D biogeochemical modeling study of Kwon et al. [2009]. In their most realistic model formulation (“nutrient restoring”, Supplementary Text T1), biological productivity changed in
response to export change and a constant rain ratio (PIC/POC) of 0.08 was used. For our analysis, their results are digitized and interpolated with a cubic spline [Kwon et al., 2009, their Figure 3c]. The change in atmospheric pCO$_2$ (referred to pCO$_2$ with $b=0.858$) is then inferred from this curve for the range of $b$ values that we find to best fit POC flux observations.

3. Results

Four biogeochemical provinces out of eleven are selected to be presented in the main text since they span a range of latitudes (Figure 1). Simulated POC fluxes for each parameterization in the selected provinces are shown alongside observations in Figure 3; all provinces are presented in supplementary Figures S3-S16, and considered in the discussion and conclusions. Two provinces, Eastern Pacific subarctic gyres (PSAE) and North Atlantic drift (NADR), were selected for focus because of their expected collocation with the study regions for the Exports Processes in the Ocean from RemoTe Sensing (EXPORTS) field campaign that is presently being planned [Siegel et al., 2016]. These sites also cover a range of ecosystem states. The simulated mean annual primary production in each province captures the climatological range of mean annual primary production, calculated using VGPM (Table 1). Although the model does not fully capture the observed seasonality across some provinces (supplementary Figure S17), it does capture the annual primary production, indicating the model is a useful tool to study mean annual export, as done here.

3.1 Twilight Zone

For each province, the Martin curve, exponential model, and ballast hypothesis have similar reliability indexes in the twilight zone (Figure 4), illustrating that these
parameterizations capture observations equally well within the twilight zone. This corroborates Buesseler and Boyd [2009], who show that the Martin curve and exponential model capture observations at shallow depths. The exponential decay model has a tendency to underestimate the flux deep in the twilight zone in some provinces such as the Pacific Equatorial Divergence (PEQD) (Figure 3). The exponential model assumes a constant sinking speed and remineralization rate (i.e. constant remineralization length scale) throughout the water column, which often results in fluxes that decrease too quickly with depth [Armstrong et al., 2002; Lutz et al., 2002]. The amount of variability in the modeled flux varies between provinces, much due to variability in primary production.

The interquartile ranges for the three parameterizations overlap for each of the univariate statistics (Figure 5), quantitatively supporting that these parameterizations are equally good at capturing observations in the twilight zone. However, the parameterizations tend to underestimate the observed variability in the twilight zone, evident through negative uRMSD* values (Figure 6). Depending on the location, the models either show a slight positive or negative bias (Figure 5, Figure 6). Overall, all the models perform well in the twilight zone and are more skillful than simply setting the POC flux to be the observed average (Figure 6).

3.2 Midnight Zone

The Martin curve and ballast hypothesis each capture observations well in the midnight zone, while the exponential model underestimates the observed flux at these depths (Figure 3; Figure 4). The exponential model underestimates the flux at depth since a constant remineralization length scale does not allow for slowdown of
remineralization with depth or increasing sinking speed with depth. The global
Martin curve slightly underestimates the observed flux in some provinces, such as
PEQD (Figure 3), resulting from either too low POC fluxes out of the euphotic zone
or the use of a $b$ parameter that is too large.

In the midnight zone, the interquartile range for summary statistics overlap for both
the Martin curve and ballast hypothesis (Figure 5); however, not for the exponential
model. Each summary statistic suggests the exponential model performs poorly in the
midnight zone compared to the Martin curve and ballast hypothesis:

1. Correlation interquartile range nearly symmetric about zero.
2. Large RMSD, AAE compared to Martin curve and ballast hypothesis.
3. Large negative bias compared to Martin curve and ballast hypothesis.
4. Large negative ME, suggesting poor model performance.

The exponential model for the midnight zone generally lies far from the origin in the
fourth quadrant in the target diagram (Figure 6), consistent with its underestimate of
the observed mean and overestimate of variability. However, if only one depth level
is resolved in the midnight zone then the normalized target diagram suggests the
exponential model reasonably captures the variability while underestimating the mean
(e.g. PSAE). For all provinces, the Martin curve and ballast hypothesis both have a
radial distance near unity on the normalized target diagram (Figure 6), suggesting
these models are equally skillful.

3.3 Regional Attenuation Parameter

Regional Martin curves, using attenuation parameters from Henson et al. [2012] and
Guidi et al. [2015], qualitatively agree with each other and with the global $b$ estimates
Regional $b$ parameters can lead to an improved fit in the midnight zone in specific provinces. For example, the Guidi et al. [2015] regional $b$ parameter reduces the bias in PEQD relative to the Martin et al. [1987] global $b$ value (Figure 2). This is further supported by the reliability index (RI) in the midnight zone decreasing from 2.24 using Martin et al. [1987] global $b$ value to 1.97 using the Guidi et al. [2015] regional $b$ parameter (Figure 8). However, when all 11 provinces are considered, the interquartile range for each summary statistic overlaps (Figure 5), which suggests on a global scale regional $b$ values produce no statistically significant improvement over the Martin et al. [1987] global $b$ value.

4. Discussion

We use a consistent modeling framework to compare estimates of vertical POC flux from three common parameterizations to a globally distributed dataset. We find that the Martin curve and the ballast hypothesis capture observations equally well at all depths. The exponential model is as skillful as the Martin curve and the ballast hypothesis in the twilight zone (100-1000m), but not as skillful in the midnight zone (1000-4000m).

Vertical attenuation of POC flux is ultimately controlled by particle sinking speed and remineralization rate, each of which can change as the particle descends through the water column. Potential processes influencing sinking speed and remineralization rate include: mineral ballasting [Armstrong et al., 2002; François et al., 2002], temperature [Laws et al., 2000; Marsay et al., 2015; DeVries and Weber, 2017], oxygen concentration [Devol and Hartnett, 2001; Van Mooy et al., 2002; Keil et al., 2016; Sanders et al., 2016; DeVries and Weber, 2017], and particle aggregation [Burd
and Jackson, 2009]. Some of these processes have been explicitly parameterized into the “stochastic, Lagrangian aggregate model of sinking particles (SLAMS)”, which was able to reproduce sediment trap observed POC fluxes and some of its regional variation [Jokulsdottir and Archer, 2016]. The relative and global importance of these processes is unclear [Burd et al., 2016] and their influence on sinking speed is still an active area of research. For example, Mari et al., [2017] show transparent exopolymer particles (TEP) accumulates in the surface microlayer and needs to be ballasted to overcome its low density in order to promote aggregation, which brings into question the classic view that TEP increases POC flux by promoting aggregation through its role as a “biological glue.” Attenuation of POC flux is also effected by surface processes that modify the character and lability of the POC that is exported. For example, episodic events [Lebrato et al., 2012; Smith et al, 2014], community structure [Guidi et al., 2009; Guidi et al., 2016], and zooplankton processes [Giering et al., 2014; Cavan et al., 2015; Cavan et al., 2017; Steinberg and Landry, 2017] are all likely important.

That we find that this implementation of the ballast hypothesis captures observations in the twilight zone and midnight zone no better than the global and regional Martin curves does not invalidate the ballast hypothesis. It simply indicates that the interaction of ballast minerals with POC, as parameterized using standard approaches, is not necessary to model POC flux in a manner that is statistically consistent with observations from water column. A major issue here is, of course, the limited coverage of these data in space and time [Mouw et al. 2016a,b; Siegel et al. 2016; Burd et al. 2016]. The ballast hypothesis is based on a long-known correlation between the flux of POC and the flux of ballast minerals [Deuser et al., 1981] which
has been used to suggest ballast minerals are responsible for the flux of POC at depth, either by increasing the sinking speed or protecting organic matter from oxidation [Armstrong et al., 2002; François et al., 2002; Klaas and Archer, 2002]. The organic matter content of sinking particles in the midnight zone is observed to be approximately 5% by weight [Armstrong et al., 2002]. An alternative view of this correlation is that sinking POC scavenges neutrally-buoyant minerals [Passow, 2004], which has been corroborated with a laboratory study [Passow and De La Rocha, 2006]. Additionally, Passow and De la Rocha, [2006] observed the POC to dry weight percent concentration to be 2-3%, which is similar to the 5% observed by Armstrong et al. [2002] in deep sediment traps, suggesting this may be the carrying capacity of suspended minerals for POC. Many studies support the claim that ballast minerals increase the sinking speed of aggregates [De La Rocha and Passow, 2007; Ploug et al., 2008; Iversen and Ploug, 2010]. However, the literature provides both supporting [Arnarson and Keil, 2005; Engel et al., 2009; Le Moigne et al., 2013] and opposing [Ingalls et al., 2006; Ploug et al., 2008; Iversen and Robert, 2015] mechanistic evidence with respect to the degree to which ballast minerals protect organic matter from oxidation.

4.1 **Modeling Recommendations**

Each parameterization investigated in this study may be useful in modeling studies, but should be selected with consideration of the time and depth scales of interest. All three parameterizations capture mean observations within the twilight zone and therefore would be suitable for studies investigating the surface ocean on annual to decadal time scales, i.e. where accurately capturing the deep ocean is not crucial. However, for studies of the carbon cycle on centennial to millennial time scales,
including assessments of long-term ocean carbon sequestration, carbon supply to the deep ocean should be important. In this case, the Martin curve and the ballast hypothesis capture observations at depth equally well on the mean and therefore would both be suitable.

We find that the empirical Martin curve has a predictive power comparable to the mechanistic ballast hypothesis, despite the fact that it lacks a mechanistic foundation. Though regional variability in the $b$ parameter may improve the realism of the Martin curve [Henson et al. 2012; Guidi et al., 2015], it is still not mechanistic. The exponential decay model’s first-order kinetics are mechanistic to a degree, but this approach excludes suggested mechanisms such as increasing sinking speed and remineralization length scale with depth [Villa-Alfageme et al., 2016]. The ballast hypothesis is more mechanistic by allowing for refractory POC and allowing ballast associated POC to sink faster with a longer remineralization length scale. However, sinking speed and remineralization length scale of POC and ballast minerals still do not increase with depth. Even though the ballast hypothesis is more mechanistic than the exponential model and the Martin curve, it does not explain the observed variability in POC flux at depth, which highlights a need for more complete quantification of export mechanisms (see section 4). If simplicity is desired, our recommendation would be to use the Martin curve in ecosystem models, but this evaluation indicates that the ballast hypothesis would be an equally good choice.

In order to improve simulations of the biological pump, the relative significance of mechanisms driving POC flux attenuation need to be better understood. The primary limitation on this understanding is the lack of observational data with sufficient
spatio-temporal resolution to resolve ecosystem processes in the surface ocean that generate POC and at the same time the processes driving remineralization at depth [Buessler and Boyd, 2009; Siegel et al. 2016; Burd et al. 2016]. Drivers of temporal variability in these mechanisms need also to be elucidated. To better constrain a model on seasonal timescales, having sediment trap data with higher temporal resolution and more sampling depths would be of great utility.

4.2 Impacts on Atmospheric pCO₂

The biological pump plays an important role regulating atmospheric pCO₂ [Parekh et al., 2006; Kwon et al., 2009] and may help explain the drawdown of atmospheric pCO₂ during glacial periods [Sigman and Boyle, 2000; Buchanan et al., 2016] by sequestering carbon in the deep ocean [Yu et al., 2016]. Carbon raining to the “midnight zone” (>1000 m) can be considered sequestered because it will be out of contact with the atmosphere for at least 100 years [Primeau, 2005; Ciais et al., 2013]. Using earth system model experiments, Buchanan et al., [2016] find that the biological pump explains about 58% of the increase in atmospheric pCO₂ from the last glacial maximum to pre-industrial times. The current uncertainty with respect to the biological carbon pump’s role in setting atmospheric pCO₂ has significant implications for our understanding of global climate regulation on time frames ranging from centennial to millennial.

Applying B* as a metric to limit Martin’s b to a range consistent with the observations in each province (section 2.6) reveals that Martin’s global b (=0.858) value is contained within the range of reasonable estimates for each province (Figure 9A). When data in the twilight zone and midnight zone are considered, and all
provinces $b$ values collected, the interquartile range of $b$ values is 0.68 – 1.13 (Figure 9C) while the range is 0.70 – 0.98 when only considering observations solely in the midnight zone (Figure 9D). The midnight zone contains 25-75% of observations in each province (>33% mean, Figure 9B) indicating sufficient data are available for the latter comparison.

Thus, the best-fit global range for $b$ is 0.68 – 1.13 across both the twilight and midnight zone, and 0.70 – 0.98 for only the midnight zone. These ranges are substantially less than 0.4 to 1.4 used in the model of Kwon et al. [2009] to estimate potential impacts on atmospheric pCO$_2$. In their most realistic model configuration, this range of $b$ leads to a range of equilibrium atmospheric pCO$_2$ of almost 100 ppm [-46ppm, +52ppm]. Since only the carbon that reaches the midnight zone is sequestered on the long-term, our data-constrained range of $b$ that is most applicable to the control of atmospheric pCO$_2$ is 0.70 – 0.98. This constrained range leads to change in atmospheric pCO$_2$ from -16 ppm to +12 ppm in the Kwon et al. [2009] model (supplementary Table S3). This indicates that uncertainty in the biological pump, as globally constrained by the available POC flux data, has the potential to vary modern atmospheric pCO$_2$ by approximately 1/3 the range suggested by Kwon et al. [2009], i.e. only a few tens of ppm [-16 ppm, +12 ppm].

5. Conclusions

The Mouw et al. [2016a] dataset is a comprehensive collection of POC flux measurements that allows a regional assessment of the skill of the Martin curve, exponential decay model, and ballast hypothesis parameterizations. When these three
parameterizations are compared to observations throughout the water column in 11 
biogeochemical provinces we find:

1. Twilight zone observations are captured equally well by the all three 
   parameterizations.

2. Midnight zone observations are captured equally well by the Martin curve and 
   ballast hypothesis.

All three parameterizations would be equally good choices for modeling studies 
addressing the upper ocean, but only the ballast hypothesis or Martin curve should be 
selected if export to depths below 1000m is of interest.

Parameterizations using the global $b$ value of Martin et al. [1987] were compared 
with province specific $b$ values of Guidi et al. [2015] and Henson et al. [2012]. 
Province-specific $b$ values can reduce the bias in the midnight zone POC fluxes in 
some regions relative to Martin’s global $b$ value (Figure 2). However, when all 
provinces are considered, the interquartile range for each summery statistic overlaps 
(Figure 5), indicating no global benefit of province-specific $b$ values. Province-
specific $b$ values may still be suitable for studies with a regional focus. For all 
provinces taken together, the range of Martin’s $b$ that best fits data from the midnight 
zone where long-term carbon sequestration occurs is [0.70, 0.98]. Based on previous 
global biogeochemical modeling [Kwon et al., 2009], this limited range of $b$ has the 
capacity to change atmospheric pCO$_2$ by only a few tens of ppm [-16 ppm, +12 ppm]. 

The paucity of high-resolution observations makes it impossible to discern the relative 
importance of various export mechanisms, many of which are discussed in Section 4. 
At a given depth level, the Mouw et al. [2016a] dataset shows variability spanning an
order of magnitude (Figure 3) that cannot yet be mechanistically explained, and thus
cannot yet be accurately modeled. The role of ecosystem structure on export, the
biotic and abiotic transformation of particles to different class sizes, and variability
through space and time are key areas of research [Burd et al., 2016; Mouw et al.,
2016b]. There is also a great need for seasonally resolved observations at a variety of
locations for more complete elucidation and quantification of export mechanisms
[Siegel et al. 2016].

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thank Darren Pilcher for initially setting up the model. Comments from two
anonymous reviews greatly improved the manuscript. Data used to create model
forcing fields are listed in the references and POC flux data is available at
6. References


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VLIZ (2009), Longhurst biogeographical provinces. [Available at http://www.marineregions.org/].


### Tables

<table>
<thead>
<tr>
<th>Province [short name]</th>
<th>VGPM†‡ [g m⁻²]</th>
<th>Simulation† [g m⁻²]</th>
</tr>
</thead>
<tbody>
<tr>
<td>NPSW</td>
<td>96 ± 53</td>
<td>137 ± 1</td>
</tr>
<tr>
<td>PSAW</td>
<td>148 ± 55</td>
<td>113 ± 113</td>
</tr>
<tr>
<td>SPSG</td>
<td>108 ± 29</td>
<td>71 ± 34</td>
</tr>
<tr>
<td>NADR*</td>
<td>251 ± 88</td>
<td>249 ± 100</td>
</tr>
<tr>
<td>NASW</td>
<td>113 ± 23</td>
<td>134 ± 2</td>
</tr>
<tr>
<td>NPPF</td>
<td>202 ± 61</td>
<td>230 ± 140</td>
</tr>
<tr>
<td>PNEC</td>
<td>128 ± 37</td>
<td>118 ± 58</td>
</tr>
<tr>
<td>PEQD*</td>
<td>155 ± 53</td>
<td>114 ± 58</td>
</tr>
<tr>
<td>ANTA</td>
<td>51 ± 31</td>
<td>39 ± 49</td>
</tr>
<tr>
<td>SANT*</td>
<td>100 ± 59</td>
<td>83 ± 88</td>
</tr>
<tr>
<td>PSAE*</td>
<td>148 ± 45</td>
<td>108 ± 99</td>
</tr>
</tbody>
</table>

* indicates province is presented in the main text.
† Uncertainty is one standard deviation.
‡ VGPM is satellite-observed net primary production.
Table 2. Definition of equation parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Units</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>F(z)</td>
<td>mgC m$^{-2}$ d$^{-1}$</td>
<td>POC flux</td>
</tr>
<tr>
<td>[POC(z)]</td>
<td>mgC m$^{-3}$</td>
<td>Volume concentration of labile POC</td>
</tr>
<tr>
<td>[POC$^Y_{hard}$(z)]</td>
<td>mgC m$^{-3}$</td>
<td>Volume concentration of POC associated with Y in the hard subclass</td>
</tr>
<tr>
<td>[POC$^Y_{soft}$(z)]</td>
<td>mgC m$^{-3}$</td>
<td>Volume concentration of POC associated with Y in the soft subclass</td>
</tr>
<tr>
<td>$[X^{prod}(z)]$</td>
<td>mgC m$^{-3}$</td>
<td>Volume concentration of production of X</td>
</tr>
<tr>
<td>$p_X^{prod}(z)$</td>
<td>mgC m$^{-3}$ d$^{-1}$</td>
<td>Production of X at depth z by phytoplankton</td>
</tr>
<tr>
<td>$Z_X^{prod}(z)$</td>
<td>mgC m$^{-3}$ d$^{-1}$</td>
<td>Production of X at depth z by zooplankton</td>
</tr>
<tr>
<td>$w_X$</td>
<td>m d$^{-1}$</td>
<td>Sinking speed of X</td>
</tr>
<tr>
<td>$w_{dust}$</td>
<td>m d$^{-1}$</td>
<td>Sinking speed of dust</td>
</tr>
<tr>
<td>$k_X = \frac{w_X}{\lambda_X}$</td>
<td>d$^{-1}$</td>
<td>Remineralization rate of X</td>
</tr>
<tr>
<td>$k_{Y_{hard}} = \frac{w_Y}{\lambda_{hard}}$</td>
<td>d$^{-1}$</td>
<td>Remineralization rate of hard subclass for Y</td>
</tr>
<tr>
<td>$\lambda_X$</td>
<td>m</td>
<td>Remineralization length scale of X</td>
</tr>
<tr>
<td>$\lambda_{hard}$</td>
<td>m</td>
<td>Remineralization length scale of hard subclass</td>
</tr>
<tr>
<td>$\omega_Y$</td>
<td>gC gY$^{-1}$</td>
<td>POC carrying capacity of Y</td>
</tr>
<tr>
<td>$f_Y^{hard}$</td>
<td>dimensionless</td>
<td>Fraction of Y routed to hard subclass</td>
</tr>
<tr>
<td>$dust^{dep}$</td>
<td>mgDust m$^{-2}$ d$^{-1}$</td>
<td>Surface dust deposition</td>
</tr>
<tr>
<td>$\Delta z_{surf}$</td>
<td>m</td>
<td>Depth of surface grid cell</td>
</tr>
<tr>
<td>$b$</td>
<td>dimensionless</td>
<td>Flux attenuation parameter</td>
</tr>
</tbody>
</table>

X = POC, PIC, or opal
Y = PIC, opal, or dust
Table 3: Tendency equation for POC associated with PIC at depth $z$ \( \left( \frac{d[POC_{PIC}(z)]}{dt} \right) \).

The summation of the parameter column produces the full tendency equation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\omega_{PIC} f_{PIC}^{hard} \left( \frac{d[PIC^{prod}(z)]}{dt} \right)$</td>
<td>Tendency of hard POC associated with PIC</td>
</tr>
<tr>
<td>$\omega_{PIC} (1 - f_{PIC}^{hard}) \left( \frac{d[PIC^{prod}(z)]}{dt} \right)$</td>
<td>Tendency of soft POC associated with PIC</td>
</tr>
<tr>
<td>$w_{PIC} \left( \frac{d[POC_{PIC}^{hard}(z)]}{dz} \right)$</td>
<td>Sinking of hard POC associated with PIC</td>
</tr>
<tr>
<td>$w_{PIC} \left( \frac{d[POC_{PIC}^{soft}(z)]}{dz} \right)$</td>
<td>Sinking of soft POC associated with PIC</td>
</tr>
<tr>
<td>$-k_{PIC}^{hard}[POC_{PIC}^{hard}(z)]$</td>
<td>Remineralization of hard POC associated with PIC</td>
</tr>
<tr>
<td>$-k_{PIC}[POC_{PIC}^{soft}(z)]$</td>
<td>Remineralization of soft POC associated with PIC</td>
</tr>
</tbody>
</table>
**Table 4:** Tendency equation for POC associated with opal at depth $z \left( \frac{d[POC_{\text{opal}}(z)]}{dt} \right)$.

The summation of the parameter column produces the full tendency equation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\omega_{\text{opal}} f_{\text{opal}}^{\text{hard}} \left( \frac{d[\text{opal}^{\text{prod}}(z)]}{dt} \right)$</td>
<td>Tendency of hard POC associated with opal</td>
</tr>
<tr>
<td>$\omega_{\text{opal}} (1 - f_{\text{opal}}^{\text{hard}}) \left( \frac{d[\text{opal}^{\text{prod}}(z)]}{dt} \right)$</td>
<td>Tendency of soft POC associated with opal</td>
</tr>
<tr>
<td>$w_{\text{opal}} \left( \frac{d[POC_{\text{opal}}^{\text{hard}}(z)]}{dz} \right)$</td>
<td>Sinking of hard POC associated with opal</td>
</tr>
<tr>
<td>$w_{\text{opal}} \left( \frac{d[POC_{\text{opal}}^{\text{soft}}(z)]}{dz} \right)$</td>
<td>Sinking of soft POC associated with opal</td>
</tr>
<tr>
<td>$-k_{\text{opal}}^{\text{hard}}[POC_{\text{opal}}^{\text{hard}}(z)]$</td>
<td>Remineralization of hard POC associated with opal</td>
</tr>
<tr>
<td>$-f_T k_{\text{opal}}^{\text{soft}}[POC_{\text{opal}}^{\text{soft}}(z)]$</td>
<td>Remineralization of soft POC associated with opal</td>
</tr>
</tbody>
</table>

$f_T$ is the temperature-dependency function [supplementary Table S3]
Table 5: Tendency equation for POC associated with dust at depth $z$ \( \left( \frac{d[POC_{dust}(z)]}{dt} \right) \).

The summation of the parameter column produces the full tendency equation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\omega_{dust} f_{dust}^{hard} \left( \frac{dust^{dep}}{\Delta z_{surf}} \right)$</td>
<td>Tendency of hard POC associated with dust</td>
</tr>
<tr>
<td>$\omega_{dust} (1 - f_{dust}^{hard}) \left( \frac{dust^{dep}}{\Delta z_{surf}} \right)$</td>
<td>Tendency of soft POC associated with dust</td>
</tr>
<tr>
<td>$w_{dust} \left( \frac{d[POC_{dust}^{hard}(z)]}{dz} \right)$</td>
<td>Sinking of hard POC associated with dust</td>
</tr>
<tr>
<td>$w_{dust} \left( \frac{d[POC_{dust}^{soft}(z)]}{dz} \right)$</td>
<td>Sinking of soft POC associated with dust</td>
</tr>
<tr>
<td>$-k_{dust}^{hard}[POC_{dust}^{hard}(z)]$</td>
<td>Remineralization of hard POC associated with dust</td>
</tr>
<tr>
<td>$-k_{dust}^{soft}[POC_{dust}^{soft}(z)]$</td>
<td>Remineralization of soft POC associated with dust</td>
</tr>
</tbody>
</table>
Table 6: Tendency equation for labile POC at depth $z$ \( \left( \frac{d[POC(z)]}{dt} \right) \) used in the ballast model. The summation of the parameter column produces the full tendency equation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \frac{d[POC^{prod}(z)]}{dt} )</td>
<td>Tendency of POC production by phytoplankton and zooplankton</td>
</tr>
<tr>
<td>(-\omega_{PIC} \left( \frac{d[PIC^{prod}(z)]}{dt} \right) )</td>
<td>Tendency of POC associated with PIC production</td>
</tr>
<tr>
<td>(-\omega_{opal} \left( \frac{d[opal^{prod}(z)]}{dt} \right) )</td>
<td>Tendency of POC associated with opal production</td>
</tr>
<tr>
<td>(-\omega_{dust} \left( \frac{dust_{dep}}{\Delta z_{surf}} \right) )</td>
<td>Tendency of POC associated with dust deposition</td>
</tr>
<tr>
<td>( w_{poc} \left( \frac{d[POC(z)]}{dz} \right) )</td>
<td>Sinking of labile POC</td>
</tr>
<tr>
<td>(-f_T k_{poc}[POC(z)] )</td>
<td>Remineralization of labile POC</td>
</tr>
</tbody>
</table>

\( f_T \) is the temperature-dependency function [supplementary Table S3]
Figure 1. Simulated provinces presented in the paper are shown in dark gray. Light gray provinces are presented in supplementary. Red dots are locations of flux observations from sediment traps and thorium-234 depletion.

Figure 2. Target diagrams displaying average model skill at each region (SANT, PEQD, PSAE, NADR) for the Martin et al. [1987] global b value (Martin), Henson et al. [2012] regional b values (Henson), and Guidi et al. [2015] regional b values (Guidi) in the twilight zone (red) and midnight zone (blue). The black circle is the normalized standard deviation of the observed POC flux. Symbols within the circle indicate that the parameterization captures the observed POC flux more accurately than using the mean of the observed data (modeling efficiency > 0) at each region.

Figure 3. Simulated POC flux (black) with standard deviation (gray) compared with observed POC flux (blue) for the Martin curve (column 1), exponential model (column 2), and ballast model (column 3) at four provinces (SANT, PEQD, PSAE, NADR). Depth is relative to the surface. Twilight zone extends from 100m – 1000m and midnight zone is >1000m.

Figure 4. Cross plot of simulated POC flux versus observed POC flux for the Martin curve, exponential model, and ballast model at four provinces (SANT, PEQD, PSAE, NADR). Colors represent depth below surface: the upper twilight zone (100-500m), lower twilight zone (500-1000m), upper midnight zone (1000-2500m), and lower midnight zone (2500-4000m). The reliability index (RI) for each zone is indicated at top left in each panel.

Figure 5. Box and whisker plots of summary statistics in the twilight zone (red) and midnight zone (blue) for each parameterization (Exponential, Ballast, Martin et al. [1987] global b value, Henson et al. [2012] regional b values, and Guidi et al. [2015] regional b values). These box and whisker plots account for all simulated provinces (11 total).

Figure 6. Target diagrams displaying average model skill at each region (SANT, PEQD, PSAE, NADR) for the exponential model, Martin curve, and ballast model in the twilight zone (red) and midnight zone (blue). The black circle is the normalized standard deviation of the observed POC flux. Symbols within the circle indicate that the parameterization captures the observed POC flux more accurately than using the mean of the observed data (Modeling Efficiency (ME) > 0) at each region.

Figure 7. Simulated POC flux (black) with standard deviation (gray) compared with observed POC flux (blue) using the global b value of Martin et al. [1987] (column 1), regional b value of Henson et al. [2012] (column 2), and regional b values of Guidi et al. [2015] (column 3) at four provinces (SANT, PEQD, PSAE, NADR). Depth is relative to the surface. Twilight zone extends from 100m – 1000m and midnight zone is >1000m.

Figure 8. Cross plot of simulated POC flux versus observed POC flux using the global b value of Martin et al. [1987], Henson et al. [2012] regional b values, and Guidi et al. [2015] regional b values at four provinces (SANT, PEQD, PSAE, NADR). Colors represent depth below surface: the upper twilight zone (100-500m),
lower twilight zone (500-1000m), upper midnight zone (1000-2500m), and lower
midnight zone (2500-4000m). The reliability index (RI) for each zone is indicated at
top left in each panel.

Figure 9. A: Range of $b$ values for each province. Light gray bar uses data in the
twilight and midnight zone while dark bars only use data in the midnight zone. B:
percentage of observations in the midnight zone for each province. C: Histogram of
normalized occurrence of $b$ values fit to observations in the twilight and midnight
zone. D: Histogram of normalized occurrence of $b$ values fit to observations in the
twilight and midnight zone. Red line is at Martin et al. [1987] global $b$ value of 0.858.
Dotted lines are the 25th percentile and 75th percentile. Solid black line is the median.

$\Delta$pCO$_2$ is relative to pCO$_2$ with $b=0.858$ [Kwon et al., 2009].