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Emerging investigator series: moving beyond resilience by considering antifragility in potable water systems

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1 **EMERGING INVESTIGATOR SERIES: MOVING BEYOND RESILIENCE BY**
2 **CONSIDERING ANTIFRAGILITY IN POTABLE WATER SYSTEMS**

3
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12
13 **Abstract**

14
15 It is inherently difficult to plan water systems for a future that is non-predictive. This paper
16 introduces a novel perspective for the design and operation of potable water systems under
17 increasing water quality volatility (e.g., a relatively rapid and unpredicted deviation from
18 baseline water quality). Increased water quality volatility and deep uncertainty stress water
19 systems, confound design decisions, and increase the risk of decreased water system
20 performance. Recent emphasis on resilience in drinking water treatment has partly addressed this
21 issue, but still establishes an adversarial relationship with change. An antifragile system benefits
22 from volatile change. By incorporating antifragility, water systems may move beyond resilience
23 and improve performance with extreme events and other changes, rather than survive, or fail and
24 quickly recover. Using examples of algal blooms, wildfires, and the COVID-19 pandemic, this
25 work illustrates examples of fragility, resilience, and antifragility within physicochemical
26 process design including clarification, adsorption and disinfection. Methods for increasing
27 antifragility—both individual process options and new system design tools—are discussed. Novel
28 physicochemical processes with antifragile characteristics include ferrate preoxidation and
29 magnetic iron (nano)particles. New design tools that allow for systematic evaluation of
30 antifragile opportunities include artificial neural networks and virtual jar or pilot “stress testing”.
31 Incorporating antifragile characteristics represents a trade-off with capital and/or operating cost.
32 We present a real options analysis approach to considering costs in the context of antifragile
33 design decisions. Adopting this antifragile perspective will help ensure water system improved
34 performance during extreme events and a general increase in volatility.

35
36 **Water Impact Statement**

37
38 Raw water quality volatility driven by extreme events presents a grand challenge to potable
39 water systems. This work describes a new perspective of antifragility that allows water systems
40 to thrive despite an uncertain future. Individual processes that have antifragile characteristics are
41 introduced and discussed, as well as new tools for water system design that allow for
42 considerations of antifragility. Incorporation of the antifragile paradigm developed here will
43 enable a shift towards more sustainable water systems less reliant on stationarity and prediction
44 of future conditions.

45
46 **Introduction**

47
48 Engineered systems that produce and distribute potable water are critically important to public
49 health. Potable water systems (PWS) have led to dramatic decreases in waterborne diseases,¹ at a
50 low cost relative to public value.² PWS face challenges, especially related to uncertainty and
51 volatility. For example, source water quality and quantity may be affected by extreme events and
52 phenomena such as chemical spills,³ harmful algal blooms,⁴ hurricanes,^{5,6} and wildfires.^{7,8} Some
53 water changes may be driven by climate change, although predictive modeling of this
54 relationship is difficult at the watershed spatial scale.⁹ PWS may also be impacted by complex
55 socioeconomic processes such as economic globalism, leading to population loss (e.g. “shrinking
56 cities”) and corresponding water age increases,¹⁰ and possible water quality problems.¹¹ These
57 processes generally contribute to volatility, uncertainty, complexity and ambiguity (VUCA).
58 This combination of stressors contributes to a “deep uncertainty” that confounds the design and
59 planning of water systems.¹²

60
61 Water treatment processes have historically been designed using a deterministic approach.^{13,14} In
62 the deterministic approach, modeling efforts intended to assist in process optimization have
63 tended to assume that the influent water quality conditions, water demands, and model
64 parameters are fixed and known. This assumption has proven dubious as new types of
65 contamination (e.g. perfluorinated compounds, pharmaceuticals) have emerged, and surface
66 water quality variability has increased.¹⁵ More recently, researchers have advocated for the
67 incorporation of variability and uncertainty of source water quality in water treatment plant
68 design and operation, but have continued an optimality paradigm with regard to water treatment
69 plant effluent.¹⁶⁻¹⁸ The deterministic approach remains the current dominant paradigm in water
70 treatment process design and operation, and is enshrined in published process selection guidance
71 (see [13] as an example).

72
73 An example consequence of the optimality paradigm is the exclusion of clarification from some
74 PWS treatment trains (e.g., direct filtration). Given source water of sufficient average historical
75 quality (i.e., the constraint), water treatment plants have been designed to minimize lifetime
76 construction and operation costs (i.e., the objective). This model has been generally successful;
77 however, a loss of (perceived) stationarity undermines the optimality paradigm, with accelerating
78 rates of change and more numerous extreme events projected.^{19,20} The optimality paradigm is
79 highly constrained and fragile to baseline water quality deviations, and is not appropriate for
80 cases of deep uncertainty, as is now faced by water treatment plant operators and planners.²¹
81 Also, it is highly dependent upon the quality of simulation models representing the water
82 treatment system; unfortunately, we know the quality of the available models to be relatively
83 poor.^{16,22} Further, common physical models such as jar testing and pilot testing informing PWS
84 decision making provide no information about future water conditions or performance. Elements
85 of the outcome for the optimality paradigm approach therefore contain stochastic elements,
86 making the outcomes also inherently stochastic.²³ An alternative decision making analytical
87 approach is needed.

88
89 PWS decision making has been shifting to the incorporation of robustness, resilience and
90 adaptation.^{24,25} In the United States, The National Infrastructure Advisory Council (NIAC)
91 defined resilient infrastructure as able to anticipate, adsorb or adapt to, and/or recover from a
92 disruptive event, and encourages planners and designers to aim for resilience in designs for

93 infrastructure.^{26,27} Similarly, America’s Water Infrastructure Act requires most PWS to conduct a
94 risk and resilience assessment by the end of 2021.²⁸ Common design changes to increase
95 resilience in PWS include additional redundancy and capacity.²¹ These changes have decreased
96 risk of water system failure; however, this approach is still somewhat dependent on prediction of
97 future events, and limiting service disruptions, not improving service in the face of volatility. If
98 volatility is increasing, then the adversarial relationship with it inherent in resilience is
99 unsustainable.

100

101 This paper describes a novel perspective for achieving an antifragility paradigm in PWS design
102 and operation, including cost trade-offs. The antifragile concept was popularized in the financial
103 domain,²⁹ but has been applied in other fields, such as computer science and transportation
104 planning,³⁰ as an approach to risk. In the antifragility paradigm, a system benefits from volatility,
105 rather than being harmed by it.²⁹ In this way, antifragility extends resilience/robustness
106 frameworks. Robust infrastructure resists failure, often through the adoption of conservative
107 designs that include excess capacity. Resilient infrastructure systems fail, but not
108 catastrophically, and recover somewhat quickly. The key benefit of antifragility is that
109 performance actually improves in volatile periods. It also is less reliant on prediction of the
110 future. The overarching objective of this paper is to introduce the antifragility paradigm across
111 domains into PWS, and frame raw water quality volatility and extreme (e.g., “black swan”)
112 events in the water supply sector that may be better managed with *via* antifragility. We also
113 include examples of novel physicochemical processes that have antifragile characteristics and
114 summarize new design tools that allow for systematic consideration of antifragility in the field of
115 water treatment.

116

117 **Black Swan Events**

118

119 We define volatility as the (relatively) rapid and unpredicted deviation from a baseline (i.e.,
120 “normal”). Specific instances of volatility can be labeled as a Black Swan Event. The term Black
121 Swan Event (BSE) was also popularized in the financial domain, and is generally taken to mean
122 a low probability event, with casual opacity, that is difficult to predict.³¹ Quantitatively, this can be
123 summarized as an event more than a few standard deviations away from the mean of prior data;
124 an outlier. Casual opacity may also be a characteristic, leading to uncertainty in what initiated the
125 low probability event. These characteristics of BSEs ultimately make them impossible to predict
126 with confidence. Often, insufficient data (e.g. sample size) make the nature of the event
127 probability unknowable, and leave it unclear if a system follows as Gaussian distribution, or
128 another distribution with skewness (e.g. gamma family), or fat tails (e.g. Cauchy).^{32,33}

129

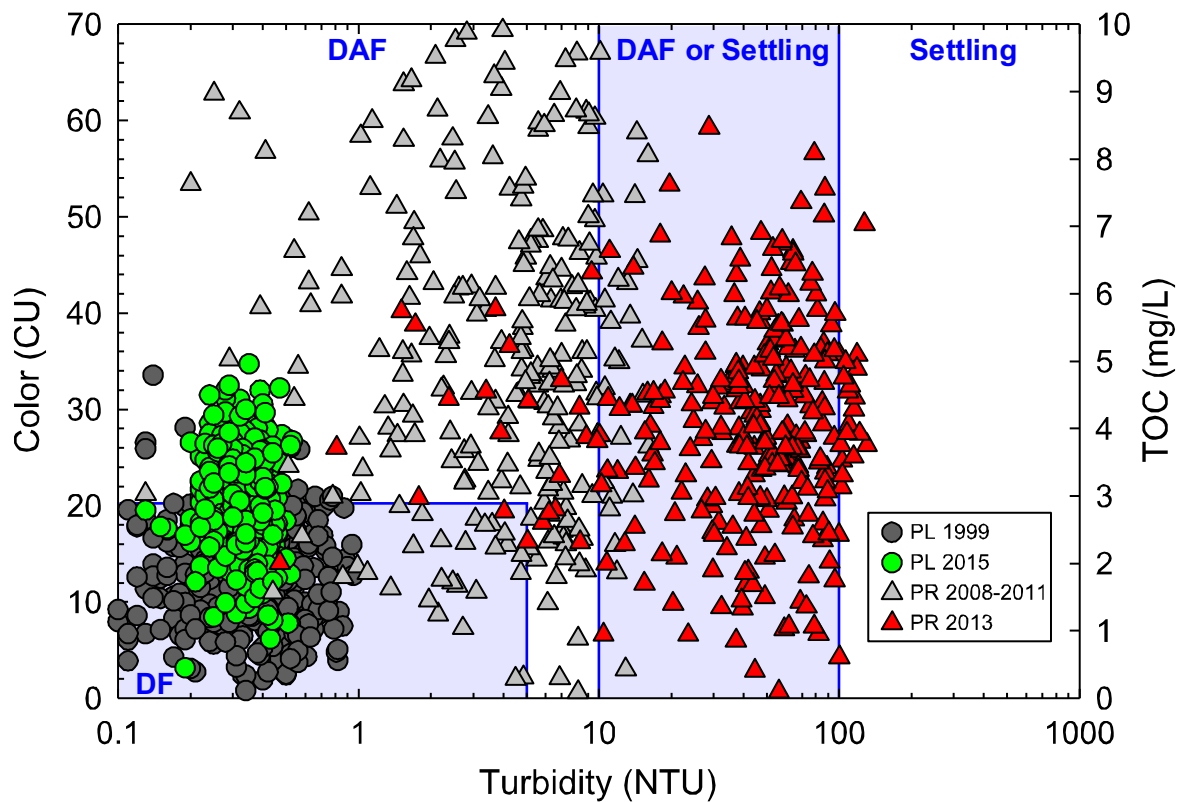
130 Here, we take this concept cross domain into the environmental engineering context, focused on
131 PWS. Water systems are exposed to BSEs. Examples receiving recent attention include lake
132 recovery,³⁴ and forest fires.³⁵ Both of these BSE examples have impacts to source water quality
133 that are an extreme departure from historical averages.³⁶ Also, the cause of these events is
134 difficult to determine. Lake recovery is a relatively rapid increase in organic productivity or
135 “browning” of a surface water driven by a complex combination of nutrient loadings, warming
136 air temperatures (e.g. climate change),³⁷ and decreases in sulfur deposition from upwind
137 sources.³⁸ In Atlantic Canada, decreases in sulfur deposition followed the amendments of the US
138 Clean Air Act, illustrating the causal opacity and deep complexity of secondary effects in PWS

139 design. Similarly, large-scale forest fires may form via anthropogenic or natural phenomena and
140 are likely exasperated by climate change, invasive insect activity, and forest management
141 policies. The total annual acreage burned by wildfires in the US more than tripled from 1983 to
142 2016.³⁵ Wildfires are known to cause changes in watersheds that impact water quality including
143 increases in turbidity, nitrate, phosphate, and disinfection byproduct precursors that may persist
144 for several years postfire.^{39,40}

145

146 The problem caused by exposure to a BSE by a PWS often presents in difficulty achieving
147 treatment goals following dramatic changes in raw water quality. These source water shifts may
148 exceed the design capacity of any physicochemical process that comprises a given drinking
149 water treatment plant. Two examples of this situation are presented in Figure 1, which includes
150 raw water organics (color or total organic carbon) and turbidity for two different source waters:
151 (1) A reservoir before and after lake recovery—Pockwock Lake,³⁴ and (2) a river draining an
152 alpine forest before and after a major wildfire—Poudre River.⁸ Figure 1 also includes regions of
153 recommended clarification design from Valade et al., 2009 based primarily on American Water
154 Works Association survey of utilities.⁴¹ Gaussian distributions were assumed for both organics
155 and turbidity.

156



157

158

159 **Figure 1.** Results of 365 statistical resamplings of distributions based on average raw water
160 quality from Pockwock Lake (PL) in 1999 (gray circle) and 2015 (green circle) and from the
161 Poudre River (PR) from 2008-2011 (gray triangle) and 2013 (red triangle). PL plots are Color vs.
162 Turbidity; PR plots are TOC vs. Turbidity. Regions of typical particle removal designs include
163 direct filtration (DF), dissolved air flotation (DAF) and conventional sedimentation from Valade
164 et al., 2009. Relative scaling of color and TOC within design regions also taken from Valade et

165 al., 2009. Raw water quality statistical information from PL and PR taken from Anderson et al.,
166 2017 and Hohner et al., 2016, respectively.

167
168 Figure 1 demonstrates that shifts in raw water quality from BSEs can change the optimal design
169 of a DWTP. Optimal clarification design guidance is summarized in Valade et al., 2009 and
170 Gregory and Edzwald, 2011 (see Table 9.9 in that work).⁴² Utilizing raw quality data from
171 Pockwock Lake (PL) in 1999, a designer using the optimality paradigm may recommended
172 direct filtration (DF) to save costs by excluding any clarification step.¹³ Similarly, an optimality-
173 based designer presented with PR data in 2011 may consider DAF clarification in an attempt to
174 save space and capital costs. DAF systems can be operated at a loading rate 10-20 times greater
175 than conventional gravity sedimentation.⁴³ However, a DAF design may struggle post wildfire,
176 as resampled turbidities are significantly greater than the pre-fire condition. The J.D. Kline
177 Water Supply Plant (JDKWSP) utilizing PL was designed as a direct filtration facility. This
178 design was optimal at the time; in 1999 water quality was within the DF design region in 92% of
179 simulations. However, JDKWSP is now straining to meet treatment goals due to lake recovery as
180 the raw water typically exceeds the recommended limits for a DF facility. Figure 1 shows raw
181 water quality exceeding the recommended color limit of the DF design region 58% of
182 simulations. As a DF facility, few mitigative options are available. For the first time in 35 years,
183 the JDKWSP recently increased its coagulation (alum) dose by 50%,⁴⁴ which may have negative
184 higher-order effects associated with increased levels of effluent aluminum and subsequent
185 changes on distribution system corrosion.⁴⁵ Recent pilot-scale research at JDKWSP has also
186 examined cationic polymers, and larger filter media. Neither mitigation approach was completely
187 successful and now physical plant upgrades are being considered. To what conditions the plant
188 might be optimized in the future remains unclear.⁴⁴ The situation at JDKWSP exemplifies
189 difficulties presented by BSEs to drinking water systems. The Fort Collins Water Treatment
190 Facility, which treats surface water from the Poudre River watershed, rapidly constructed a
191 presedimentation basin as a response to observed turbidity volatility following a major wildfire.³⁹

192 193 **Fragile, Resilient, and Antifragile**

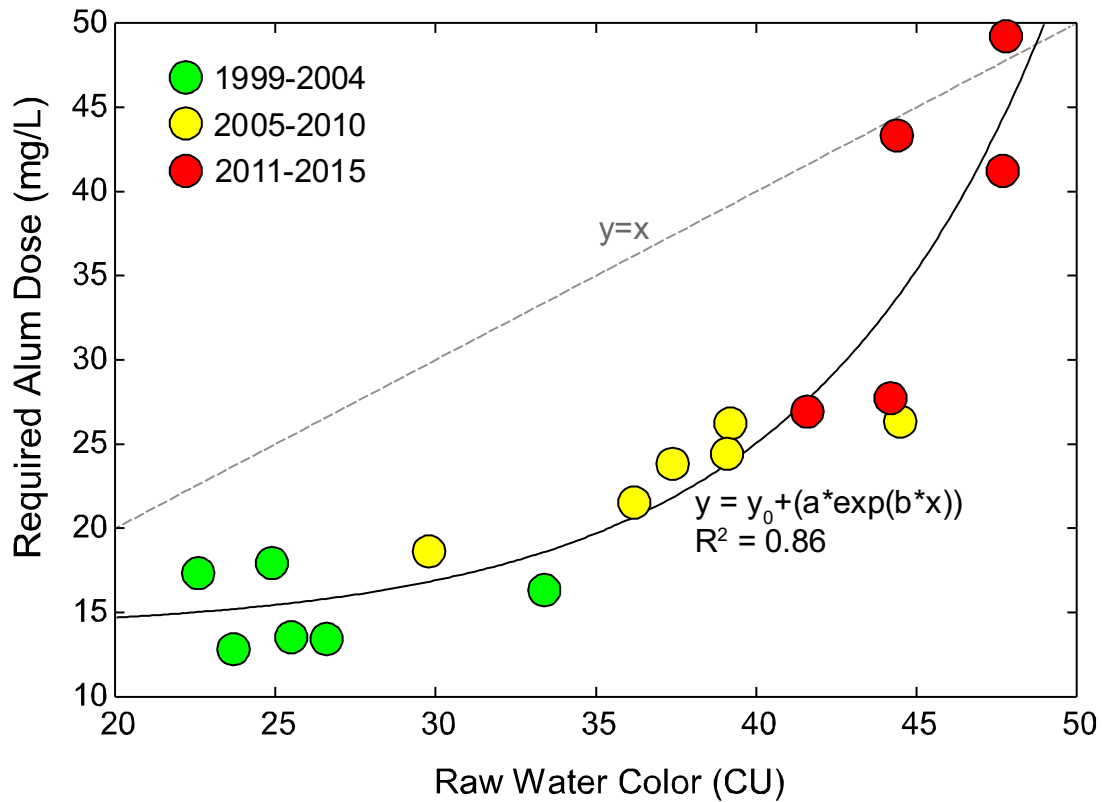
194
195 Future BSEs and general volatility are difficult to predict, so it is more profitable to define a
196 system based on relative impact from stress. This approach has again been popularized in
197 financial markets through stress testing.⁴⁶ The three primary relationships to stress may be
198 described as fragile, resilient, and antifragile. A fragile system has severe negative outcomes
199 from volatility, a resilient system has minor negative outcomes from volatility with relatively
200 quick recovery, while an antifragile system has positive outcomes from volatility. Mathematical
201 expressions of all three terms exist;⁴⁷ however, model-free and probability-free heuristics can
202 also be used to assess fragility, resilience, and antifragility based on a convex relationship to
203 volatility.⁴⁸ Fragile and antifragile systems have negative and positive convex relationships with
204 volatility, respectively, while resilience has a linear relationship with volatility. Here, we apply a
205 heuristic approach to identifying fragile, resilient, and antifragile PWS based on convexity using
206 data from full-scale DWTPs,

207
208 Fragility, resilience/robustness, and antifragility are currently present in contemporary full-scale
209 DWTPs. Examples of each include the Lake Major Water Supply Plant (#1 Fragile); the
210 Providence Water System (#2 Resilient) and for two surface water sourced DWTPs in New

211 England (#3 Antifragile). The Lake Major Water Supply Plant and the Providence Water System
212 are also both surface water sourced systems.

213
214 **Fragile.** The Lake Major Water Supply Plant (LMWSP) was commissioned in 1999 as a
215 conventional sedimentation facility treating a high-quality source, Lake Major (LM). The
216 LMWSP serves the same general population as JDKWSP: Halifax, Canada. Similar to Pockwock
217 Lake, Lake Major has also experienced lake recovery since commission, resulting in an increase
218 in raw water algal organics, as noted by color measurements, shown in Figure 2. Algae challenge
219 conventional sedimentation-based DWT plants in two ways: the algal organic matter exhibits an
220 increased coagulant demand, and algal particles settle quite slowly due to specific gravities ≤ 1 .⁴⁹
221 The LMWSP has few mitigative operational controls, and has increased alum dosing in response
222 to increased water color. Figure 2 shows an exponential (e.g., convex) relationship between raw
223 water color and required alum dose. This indicates accelerating problematic fragility to further
224 increases in water color. For example, an increase in color 5 units from 25 to 30 resulted in an
225 alum increase of 20%, while the same 5 unit increase from 42 to 47 resulted in an alum increase
226 of almost 50%. Results indicate accelerating problems and risk of system failure with further
227 increase in raw water color, even if only incremental. Significant increases in alum dose carry
228 the potential for numerous negative second-order effects, such as increased chemical costs,
229 decreased filter run times, increased solids handling stress, and increased distribution system
230 corrosion.⁴⁴

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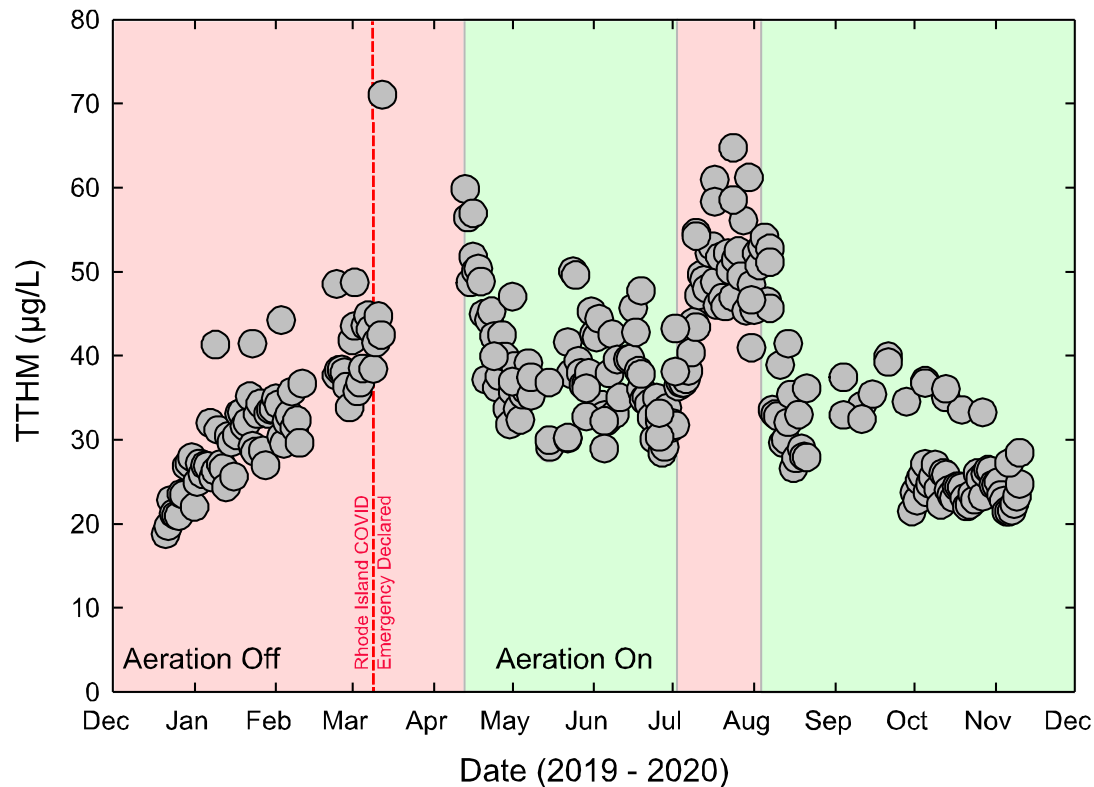
235 **Figure 2.** Yearly mean raw water color and corresponding coagulant dose at the Lake Major
236 Water Supply Plant from 1999 through 2015. Data from Anderson et al., 2017. Note the non-

237 linear (e.g., convex) relationship between color and required alum dose demonstrating fragility.
238 Incremental increases in color above 40 CU led to exponential increases in alum dose.

239
240 **Resilient.** The Providence Water Supply Board (PW) operates the largest conventional DWTP in
241 the Northeast USA. PW has a history of providing safe water service but recent, occasional
242 issues with disinfection byproducts (DBPs), especially total trihalomethanes (TTHMs), have
243 occurred including an maximum contaminant limit (MCL) violation in 2018.⁵⁰ One particular
244 DBP monitoring site tends to control MCL compliance; a large elevated storage tank in a remote
245 part of the system. PW had recently installed a THM-stripping aeration system in the tank, just
246 prior to the BSE of the COVID-19 pandemic. Changes in commuting and other behavioral
247 patterns led to changes in water usage within the service area's urban core. Water ages increased,
248 and thus the THM formation also increased. Trihalomethane formation potential (THMFP) is a
249 function of several drivers including precursory organic carbon, residual chlorine concentrations,
250 temperature, and water age.⁵¹ Methods exist for estimating site-specific THMFP based on
251 dissolved organic carbon (DOC), UV absorbance, and other water quality parameters.^{52,53} Using
252 an approach outlined in [52] the THMFP for PW effluent is estimated to range from 100 to 150
253 $\mu\text{g/L}$, significantly greater than the 80 $\mu\text{g/L}$ MCL for TTHMs.

254
255 The increase in water age created stress on the PW system to meet the MCL. Results in Figure 3
256 show rapidly increasing THMs in March 2020, with one sample above 70 $\mu\text{g/L}$. Aeration was
257 initiated in April. Aeration within the storage tank was effective at decreasing THMs in the
258 delivered water, and THM values decreased to well below the MCL. The impact of aeration is
259 also noted in July 2020 when aeration was temporarily ceased. The use of aeration represents a
260 form of resilience for PW. Given serious stress from the COVID-19 BSE (increase in THMs),
261 the system was able to mitigate the damage, and continue to meet treatment goals, after a
262 temporary increase in delivered water THMs. There is a linear (non-convex) relationship
263 between volatility and THMs as the presence of aerators provides a switch-on recovery option
264 that can be utilized as needed. This THM mitigative approach generally meets the NIAC
265 definition of resilience: "the ability to reduce the magnitude and/or duration of disruptive events
266 through the ability to anticipate, absorb, adapt to, and/or rapidly recover."²⁷

267



268
269

270 **Figure 3.** Total trihalomethane (TTHM) concentrations measured as at an elevated storage tank
271 within a problematic water age area of the Providence Water (PW) system from December 2019
272 through November 2020. Shaded regions represent periods when an aeration system inside the
273 elevated storage tank was in operation. PW THM formation potential estimated to be 100 to 140
274 µg/L.

275

276 Resilience may also be considered at the system level. In general, the more diverse a system is
277 (e.g. multiple sources and/or production) the more resilient it is to a particular disruption; while a
278 highly centralized system is more fragile.²⁹ The relationship between centralization and fragility
279 has been commonly explored in a financial context (e.g. “a diversified portfolio”), however,
280 recent work has advocated for water supply systems to not be reliant upon a single source of
281 water.⁵⁴ A comparison between the water systems of Rhode Island, USA and Singapore
282 demonstrates this difference. The PW system, consisting of one conventional water treatment
283 plant, provides water to approximately two-thirds of Rhode Island residents, as many
284 communities outside of Providence are wholesale customers through interconnections. While
285 this is efficient, it also fragile as any BSE or other disruption at the PW treatment plant would
286 impact potable water access to much of the state. Contrastingly, the Singapore Four National
287 Taps approach includes water imports, direct potable reuse (i.e., NEWater), desalination, and
288 runoff from local catchments. These four sources, each with different treatment processes,
289 represents a semi-decentralized system with much less fragility from a BSE that might disrupt an
290 individual component of the PWS. Decentralized water infrastructure has been described as a
291 distinguishing characteristic of the “Water Sensitive City”,⁵⁵ with the aim of reducing the harm
292 from extreme events and ensuring service security for residents.⁵⁶

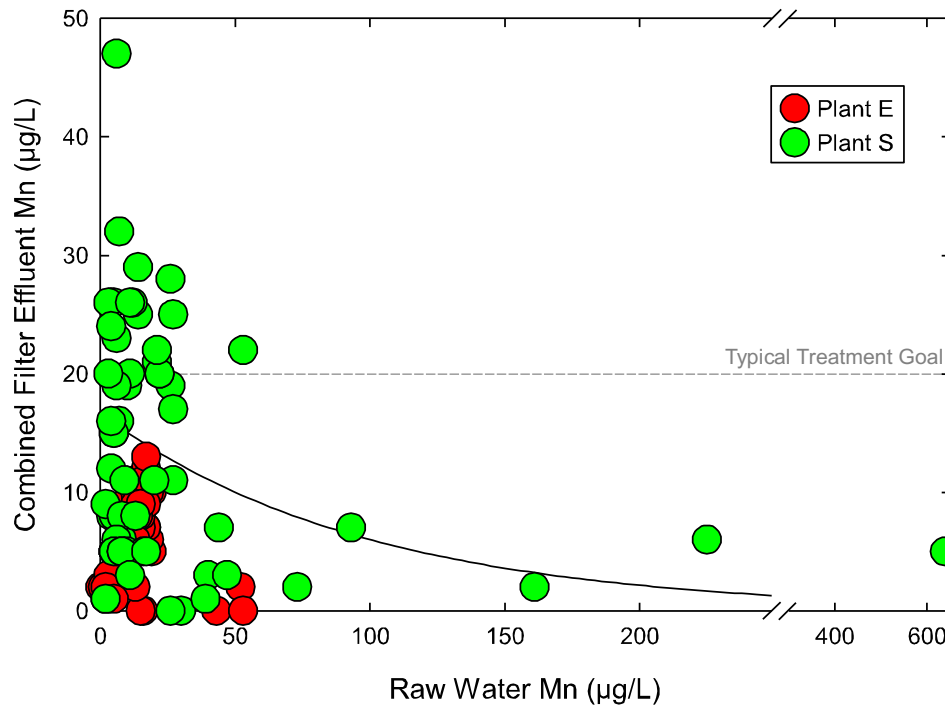
293

294 Decentralized systems also support intergenerational equality and environmental justice.⁵⁶ In the
295 electricity planning field, one tool to accomplish this is “islanding”, whereby decentralized
296 energy suppliers are managed in a way to protect consumers from blackouts, ensuring the
297 security of supply.^{57–59} Within water networks, infrastructure that can be disconnected from the
298 main centralized water system if it is compromised would continue as a source of clean water
299 when in island mode, promoting public health and safety, supply security, and overall regional
300 livability.⁵⁵

301
302 **Antifragile.** Options for incorporating antifragility in PWS are available. For example,
303 Manganese (Mn) is a contaminant of concern in the drinking water field, based on emerging
304 health risks, aesthetic concerns, and recent regulation by Health Canada.⁶⁰ Current USEPA non-
305 enforceable guidance on Mn is through a secondary maximum contaminant level (SMCL) of 50
306 µg/L, although there is no scientific basis for this SMCL, and aesthetic concerns still commonly
307 occur at this level.⁶¹ The typical treatment goal for finished water Mn is 20 µg/L.⁶² Mn presents
308 challenges to surface water systems, as raw water Mn concentrations can be highly variable;
309 changing an order of magnitude or more within days.⁶³ This volatility challenges chemical
310 oxidation treatment, such as meeting stoichiometry.⁶⁴ However, auto-catalytic Mn(II) (e.g.
311 “greensand”) adsorption and subsequent free chlorine regeneration has been successful Mn
312 removal approach. This auto-catalytic process exhibits antifragile characteristics, as the adsorbed
313 Mn from the source water is rapidly converted by free chlorine to MnO_x sites for additional
314 Mn(II) adsorption.⁶⁵ Thus, increases in raw water Mn produce increased adsorption capacity of
315 subsequent raw water Mn(II), creating a positive, reinforcing cycle.

316
317 Figure 4 includes raw and combined filter effluent (CFE) Mn concentrations for two surface
318 water sourced DWTPs in New England. For both facilities, CFE Mn levels were lower as raw
319 water Mn increased. In other words, treatment improved as contaminant concentrations
320 increased. There is a positive convex relationship between raw water Mn and CFE Mn. Plant S
321 more consistently achieved CFE Mn treatment goals when influent Mn was ≥ 50 µg/L, and met
322 the treatment goal despite raw water Mn far exceeding 100 µg/L. This process is clearly beyond
323 resilient and improves as raw water conditions deteriorate. Adequate Mn treatment does not
324 require precise prediction or measurement of raw water Mn, nor a full understanding of the
325 causes of raw water Mn fluctuations. Loss of MnO_x coating from media surfaces is a likely cause
326 of CFE Mn exceeding raw water Mn in the case of both facilities in Figure 4. This coating loss is
327 a function several parameters including free chlorine residual across the media, backwashing
328 practices, and filter run times.⁶⁶ MnO_x coating loss can be controlled by balancing these
329 operational parameters with other water quality objectives on a case-by-case basis.⁶²

330



331
 332
 333 **Figure 4.** Combined filter effluent manganese (Mn) concentrations as a function of influent raw
 334 water Mn concentration for two surface water treatment plants with seasonal manganese
 335 problems. Data from Goodwill, 2006.
 336

337 The use of coagulation for the removal of DBP precursors (e.g., “enhanced coagulation” but
 338 perhaps best called “multi-objective coagulation”)⁶⁷ is another example of an antifragile process
 339 common in water treatment systems. Aromatic, hydrophobic, higher molecular weight (MW)
 340 carbon compounds are more preferentially addressed by coagulation with metal salts due to
 341 charge interactions between cationic metal hydrolysis products and anionic humic
 342 macromolecules with carboxyl and phenolic groups.^{68,69} This is fortunate, as these same fractions
 343 of NOM also tend to have higher halogenated DBP yields due to the same unsaturated and
 344 aromatic moieties that have relatively high electron-donating capability.^{70,71} Therefore, as
 345 concentrations of higher DBP-forming compounds in raw water increases greater removals *via*
 346 enhanced coagulation are expected. This antifragile characteristic is acknowledged in The
 347 USEPA Stage 1 D/DBP Rule which requires higher removals of organic matter as aromatic and
 348 hydrophobic portion increases, as quantified by specific ultra-violet absorbance (SUVA).⁶⁷
 349

350 **Incorporating the Antifragility Paradigm into Potable Water Systems**

351
 352 Antifragility can be incorporated into a PWS by applying physicochemical processes that are
 353 known to do well under a given set of raw water quality volatility. This process requires two
 354 general steps: (1) knowledge of individual processes that increase antifragility and (2) a design
 355 evaluation approach that enable antifragile process selection under a given volatility parameter
 356 (e.g., what processes have positive convexity to this volatility parameter?). We present two
 357 examples of emerging antifragile treatment processes and describe new design tools and how
 358 they may be used. Diverging from the optimality paradigm will inherently lead to increased

359 costs, and we also present opportunities to include real options analysis for the assessment of
360 antifragile and financial trade-offs.

361
362 **Individual Processes.** Two examples of emerging, individual processes that may increase
363 antifragility of PWS include: (1) ferrate (Fe(VI)) preoxidation and (2) magnetic (nano)particulate
364 iron oxides.

365
366 Fe(VI), a high-valent oxo-anion of iron,⁷² has been considered and evaluated as a potential
367 preoxidant (i.e. occurring before the primary particle removal step) in DWT.⁷³ Preoxidation is
368 sometimes utilized as a response to BSEs, such as chemical spills,⁷⁴ wildfires,⁷⁵ and algal
369 blooms⁷⁶ to mitigate organic contaminants and/or improve downstream performance. Fe(VI) has
370 a high reduction potential that is comparable to other strong oxidants in DWT such ozone (O₃)
371 and chlorine dioxide (ClO₂).⁷⁷ Similar performance in oxidative transformation of organic and
372 inorganic targets between Fe(VI) and O₃ has been noted, including DBP precursors,⁷⁸
373 manganese,⁷⁹ arsenic,⁸⁰ and algal toxins.⁸¹ Unlike O₃ and ClO₂, however, Fe(VI) does not require
374 on-site generation. A production method for stable, high-purity K₂FeO₄(s) salts has been
375 developed,⁸² which forms the basis for recent commercial applications. Also Fe(VI) generally
376 leads to lower yields of active bromide and bromate than O₃,⁸³ due to the simultaneous *in situ*
377 formation of H₂O₂ during Fe(VI) decay,⁸⁴ which reduces HOBr to Br⁻.⁸⁵ Fe(VI) does not form
378 chlorite or chlorate, unlike ClO₂, and is not known to directly from any other regulated
379 byproducts.⁷²

380
381 This difference in generation between O₃/ClO₂ (on-site) and K₂FeO₄ (off-site) makes Fe(VI) a
382 way for increasing antifragility of a water system. K₂FeO₄ can be acquired as needed, stored
383 onsite as a stable salt, and added as conditions dictate. In this way, use of K₂FeO₄ is similar to
384 powdered activated carbon usage for managing urgent events. However, Fe(VI) leads to benefits
385 to multiple water treatment physicochemical processes including (pre)oxidation, coagulation,
386 clarification, and disinfection.^{73,86} These multimodal benefits enable production of water quality
387 better than baseline, in spite of a sudden deterioration in raw water quality. For example, bench-
388 scale testing has demonstrated lower post-clarification water turbidities following an algae spike
389 than was otherwise achievable.⁸⁷ Similar results related to ferrate use in natural disaster
390 emergency contexts have been noted at the point-of-use (POU) scale.^{88,89}

391
392 K₂FeO₄ dissolves in water to produce Fe(VI) which is a relatively strong oxidant, leading to the
393 transformation of various reduced targets stemming from a BSE including algae and algal toxins,
394 ^{90,91} chemical spills (e.g. Methyl tert-Butyl Ether).⁹² This Fe(VI) can also be activated using
395 common shelf-stable reductants, such as sulfite, forming radicals Fe(V) and SO₄⁻ *in situ* that are
396 capable of transforming recalcitrant organics.^{93,94} Following oxidation, Fe(VI/V) is reduced to
397 Fe(III) which is insoluble in most water treatment contexts. These *in situ* formed iron particles
398 have unique characteristics including polydisperse diameters,⁹⁵ magnetism,⁹⁶ and core-shell
399 architecture.⁹⁷ Ferrate resultant particles then participate in coagulation,⁹⁸ flocculation,⁹¹
400 clarification, and adsorption processes.^{97,99} This multimodal action enables antifragility in
401 response to volatility. For example, a water utility experiencing an unforeseen chemical spill
402 could deploy ferrate as needed to oxidize the pollutant, while simultaneously decreasing
403 disinfection byproducts, and improving coagulation beyond typical baseline operations. Thus,
404 the as needed deployment of shelf stable K₂FeO₄ as represents a step towards antifragility. In

405 contrast to MnO_x, Fe(VI)-derived benefits are from the use of the technology itself, not a
406 synergistic effect of the degraded water quality. Fe(VI), in several forms, could also be
407 conducive to consistent use as part of baseline operations.

408
409 Iron oxide nanoparticles (IONPs), exclusive of the ferrate context, also provide antifragility to
410 PWS through the combination of adsorption and magnetic separation.¹⁰⁰ Iron oxide nanoparticles
411 comprised of magnetite (Fe₃O₄) or maghemite (γ-Fe₂O₃) exhibit superparamagnetic properties
412 and relatively high adsorption capacities for various drinking water contaminants. These IONPs
413 can be synthesized off site, stored and used as needed by a PWS, like powdered activated carbon.
414 However, unlike PAC, IONPs can be selectively recovered via magnetic separation, and
415 reused.¹⁰¹ IONPs were found to decrease the concentration Rhodamine B dye in aqueous solution
416 by > 60% with no significant decrease in adsorption capacity after five cycles of magnetic
417 separation and chemical regeneration. Magnetic-based separations have demonstrated
418 effectiveness of > 95%, using commercially available permanent magnet systems.^{101,102} The use
419 of magnets may also improve flocculation and separation of non-magnetic particles assuming
420 attachment to an IONP. Magnetic attraction between superparamagnetic IONPs in a magnetic
421 field would serve to increase aggregation rate, from a DLVO perspective. Therefore, addition of
422 IONPs in response to an algal bloom, forest fire, or chemical spill could enable improved water
423 quality more than if the BSE had not occurred. For example, modeling magnetic filtration of
424 activated sludge particles comprised of 10% IONPs by volume with stainless steel wool (M =
425 0.2T) indicate filtration performance 100-times more effective than a conventional gravity filter
426 with media collectors.¹⁰³ In this way, IONPs represent a “switch on” method for achieving
427 antifragility (similar to K₂FeO₄); however, they may also be used outside of periods of volatile
428 water quality and provide benefits during more typical periods.

429
430 **Design Tools.** A water system designer interested in incorporating antifragile processes into a
431 drinking water plant requires new tools for guidance and evaluation. Current and historical
432 process design under the optimality paradigm follows a multistep deterministic approach: (1)
433 characterization of raw water quality and establishment of treatment goals; (2) jar testing and
434 pilot studies and (3) selection of treatment processes optimized to conditions during jar testing
435 and piloting. This approach produces treatment facilities that are generally minimized for cost
436 given a required baseline performance. However, a six-month pilot test has a low probability of
437 evaluating a BSE, and the system design has opacity to what future conditions a particular
438 process might need to be antifragile to. In other words, incorporation of antifragile processes
439 requires a lens to systematically evaluate weakness prior to picking antifragile processes. This
440 establishes a potentially beneficial relationship with future volatility that is a key characteristic of
441 an antifragile system.²⁹

442
443 Artificial neural networks (ANNs) are a biologically-inspired computational model generally
444 consisting of an input layer, hidden layer(s), and an output layer.¹⁰⁴ There are many different
445 forms of ANNs and their corresponding models are trained and built using multiple methods and
446 calibrated using large data sets such that the weights between different neurons and hidden layers
447 can be estimated.¹⁰⁵ ANNs offer several advantages over traditional modeling approaches and
448 are well-suited for drinking water treatment applications because: (1) associations between
449 inputs and outputs are “learned” from historical data without having to specify the form of the
450 model; (2) results of ANN runs are robust to noisy or discontinuous data; (3) a detailed

451 understanding of the processes (i.e. treatment process) is not necessary, only an understanding of
452 the factors that influence the processes; and (4) they are fast (increases in computer processing
453 speeds have reduced the time needed to train and evaluate these models).^{106,107} For example,
454 Shariff et al. 2004 used an ANN for modelling a full-scale drinking water treatment facility lime
455 clarification process and reported r-squared value of 0.92 for the ANN model versus 0.41 for the
456 USEPA Water Treatment Plant Model. ANNs have been used for simultaneous prediction of
457 turbidity and DOC removal for a conventional surface water treatment plant configuration as a
458 function of source water quality parameters and chemical use.¹⁰⁸ Results from Kennedy et al.,
459 2015 indicate that ANNs can be used to provide an evaluation of the impact on DOC changes (as
460 measured by individual parallel factor analysis components) on the coagulation process and
461 turbidity removal. This enables virtual jar testing of future water quality scenarios that were not
462 present during the original experiments. Coagulation of the turbidity and/or DOC event caused
463 by a BSE (e.g., wildfire, accelerating lake recovery, or hurricane) can be evaluated prior to
464 occurrence, allowing for development of antifragile elements into the physicochemical
465 processes. In other words, shifts in water quality presented in Figure 1 could be simulated to
466 “stress test” and assess impact on coagulation/clarification performance before they occur, and
467 identify potential chemical combinations and operational settings that perform better as the same
468 shifts occur.

469
470 Beyond bench-scale, pilot testing can also be improved with digital tools to achieve antifragility,
471 primarily by simulating performance during extreme events prior to their occurrence.
472 Developments in pilot-testing have led to the development of “proven perfect” pilot-scale
473 systems that closely replicate their full-scale counterparts, as demonstrated by paired *t* tests to
474 confirm the production of statistically equivalent water quality.¹⁰⁹ Knowles et al., 2012 describes
475 this process for the JDKWSP. This particular pilot system has been used to established possible
476 physicochemical solutions to lake recovery, albeit after the negative impacts from lake recovery
477 were realized.⁴⁴ Pilot-scale systems that are proven to represent full-scale performance can be
478 combined with digital twins to “stress test” a proposed process system design before problems
479 arise, and proactively select and incorporate antifragile processes. A digital twin is a dynamic
480 simulation model that visually integrates system components, and can be combined with data
481 variations to understand the sensitivity of a physical system to input perturbation.¹¹⁰

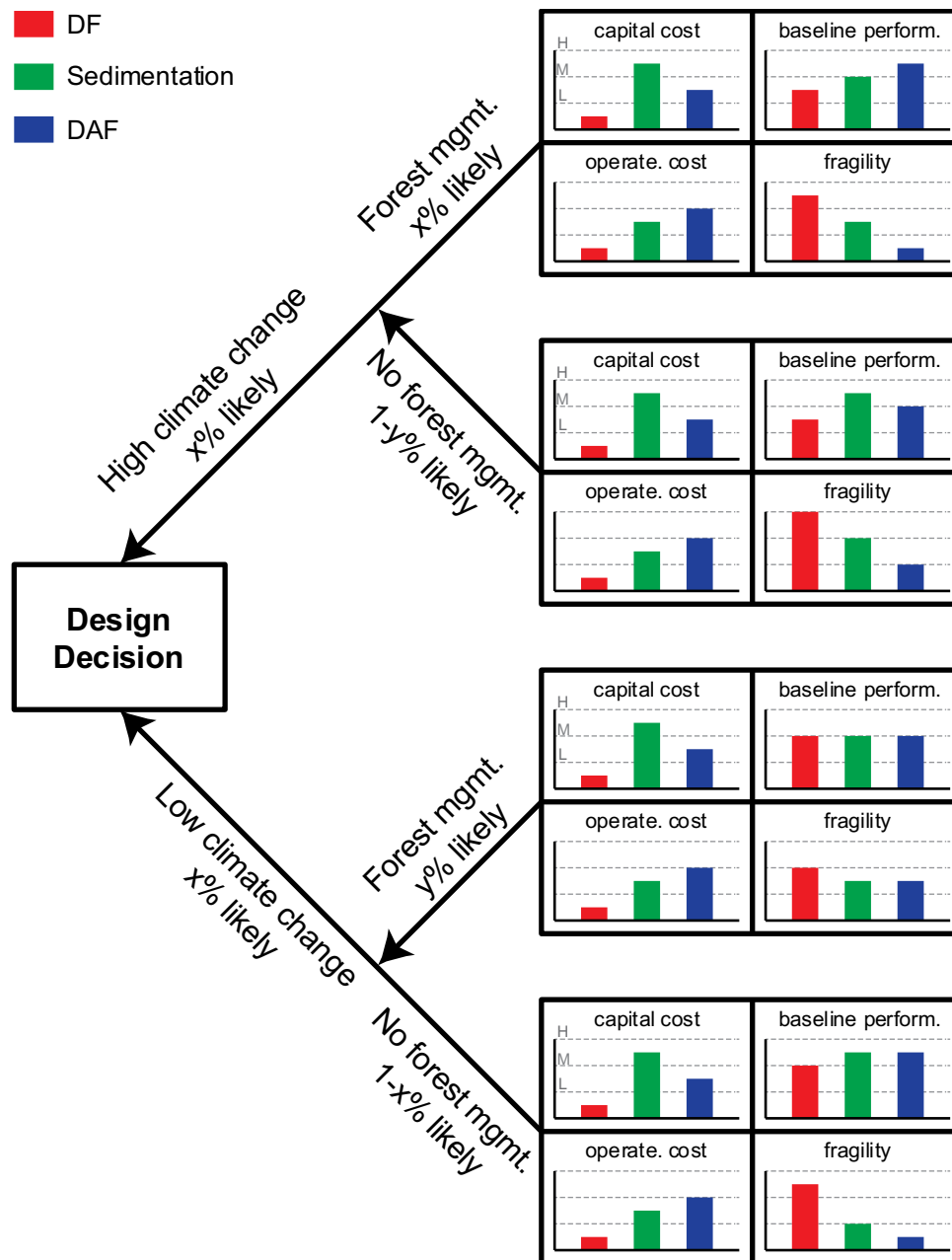
482
483 Essentially, these digital twins enable the typical process design question to be flipped: what
484 types of future BSEs is the system fragile (e.g., negative convexity)? Curl et al. 2020 refers to
485 this approach as “failure analysis”. In this application the failure is virtual, and information
486 generated can be used to select processes that would perform better when the same BSE occurs
487 (e.g., positive convexity). In this way the designer is empowered to systematically increase the
488 antifragility of a water treatment system. The drinking water treatment space is currently
489 experiencing early adoption of digital twins. For example, the City of San Diego (California,
490 USA) is developing a digital twin of its North City Pure Water Facility, a component of their
491 water reuse program.¹¹⁰ This digital twin operates via one-second time steps, and fully replicates
492 system hydraulics and process performance. The city intends to employ the digital twin to
493 improve future performance to operational challenges.

494
495 **Investment Considerations.** Investments in antifragility may require capital cost outlays,
496 behavioral changes and localized downtime or inconvenience as systems are altered from the

497 original deterministic designs. Investment in antifragility therefore requires demonstration of
498 benefits that outweigh the costs – benefits such as improved performance, increased long-term
499 (i.e., intergenerational) water security. Tradeoff analysis such as this is the realm of decision
500 science, and the application to antifragility investment follows.

501
502 Tradeoff analysis is the analytical core of Decision Making under Deep Uncertainty.¹¹¹ Figure 5
503 summarizes one approach. For the sake of illustration, we select four desired attributes of the
504 proposed water treatment system: 1) low capital cost; 2) low operating costs; 3) high baseline
505 performance; and 4) low fragility. The three design options in this case, as presented in Figure 1,
506 are direct filtration (DF), sedimentation (Sed.), and dissolved air flotation (DAF). In the
507 illustration, DF has the lowest capital costs and sedimentation has the highest capital costs. Why,
508 then, would one choose to build sedimentation over DF? One motivating factor might be the
509 higher baseline performance offered by sedimentation. But that baseline performance is
510 calculated, as discussed in the Design Considerations section above, with reference to the
511 particular raw water characteristics observed in the historical case, and it changes depending on
512 whether the designer believes that those historical raw water characteristics will continue into the
513 future or shift in some anticipatable fashion. Shifts in raw water characteristics will affect
514 estimates of operating costs, and the system fragility.

515
516



517
518

519 **Figure 5.** Real options analysis decision tree framework for the comparison of three clarification
520 designs: Direct filtration (DF), gravity sedimentation (e.g., conventional settling), and dissolved
521 air flotation (DAF). Capital and operational costs, and baseline performance taken from Gregory
522 and Edzwald, 2011.

523

524 One method for navigating uncertainty in future raw water characteristics when designing a
525 water system is to enumerate a decision tree.¹¹² This approach, sometimes referred to (especially
526 in applications to financial decision making) as real options analysis (ROA, see for example
527 Ranger et al. (2010)),¹¹³ involves stepping through branches of distinct uncertainties. Each
528 uncertainty is discretized into easily understood categories of exogenous variable such as “high”,
529 “medium”, or “low”. Endogenous variables (such as “build this” or “build X amount of that” or

530 “don’t build”) are decision points at the left-hand side of decision trees. In higher-order complex
 531 decision trees, endogenous decision points can be interspersed throughout the branches of the
 532 tree to represent decision staging and adaptive design. Figure 5 includes only a single
 533 endogenous decision point (build DF or Sedimentation or DAF), and two exogenous variables to
 534 which the performance of the treatment plant is sensitive: climate change, discretized into
 535 “high”, signifying rapid global warming over the treatment plant’s design life, and “low”
 536 signifying less rapid global warming; and forest management, discretized into “yes” or “no”.
 537 Climate change increases ambient air temperatures and speeds the hydrologic cycle, resulting in
 538 lower base flows during dry periods and higher velocity flow during wet periods. Each condition
 539 creates raw water quality challenges, as described in the introduction. Forest management is
 540 costly (and controversial), but has potential to reduce evapotranspiration, reduce forest fire risks,
 541 and improve soil retention. Forest management also benefits source water protection,¹¹⁴ which
 542 can be considered the first step in water treatment,¹¹⁵ from a multiple barrier perspective by
 543 decreasing contaminant load in source waters. For the sake of illustration, these two variables are
 544 presented as independent, i.e., forest management policy has no bearing on climate change
 545 magnitude, and climate change magnitude has no bearing on forest management policy.

546
 547 Scenarios are formulated as combinations of the fully enumerated decision tree, in this case: high
 548 climate change and forest management, high climate change without forest management, low
 549 climate change and forest management, low climate change without forest management. Once
 550 the scenarios are enumerated, variable values (e.g., water temperature, sediment load) are
 551 assigned to represent each condition, and the performance of each treatment option is simulated
 552 for each variable setting. Simulations might be accomplished with an ANN, a physically based
 553 model, or a “digital twin”, as discussed earlier. As shown in Figure 5, the baseline performance
 554 of each treatment option is differently responsive to the altered conditions. In the case of low
 555 climate change and forest management, DF might be the preferred choice as it is lowest in cost
 556 with comparable baseline performance, and only slightly elevated fragility. However, in the case
 557 of high climate change and no forest management, sedimentation might be the preferred choice,
 558 with its high baseline performance and relatively low fragility. DAF appears the best option in
 559 the case of low climate change without forest management, with its moderate costs, high baseline
 560 performance and very low fragility. Probabilistic weighting and risk hedging is needed before a
 561 final decision can be made.

562
 563 Climate change carries deep uncertainty. The Intergovernmental Panel on Climate Change
 564 (IPCC) Sixth Assessment Report presents possible climate futures as a function of potential
 565 reductions in carbon dioxide and other greenhouse gas emissions. The extent of realized global
 566 warming will affect the climate system in numerous ways, including precipitation extremes, and
 567 more intense tropic cyclones.¹¹⁶ It is impossible to know whether “high” climate change or “low”
 568 will occur, and it is impossible to know whether the next set of politicians will opt for forest
 569 management or not. However, in order to overcome the paralysis created by the uncertainty
 570 regarding future watershed conditions, we weight possible future conditions by likelihood of
 571 occurrence and calculate the expected value of each performance metric across the uncertainty
 572 space as shown in Equation 1.

$$573 \quad \xi = \sum_{s \in \Omega} p_s \xi_s \quad \forall s \quad \text{(Equation 1)}$$

574
 575

576 Where ξ_s is the value of the realization of the particular performance metric under consideration
577 in some future aggregate scenario (climate change level and forest management condition) s , and
578 p is the probability of that aggregate scenario. ξ is the expected value of the performance metric
579 across the likelihood-weighted future conditions.

580

581 Expected values are not the only metrics of interest and depending on the risk aversion (or
582 relative optimism) of the particular decision maker, there might be more or less focus placed on
583 extreme values – best-case and worst-case performance of each water treatment plant design
584 option. Finally, likelihoods could be assigned in this case, for example, by consulting the most
585 up-to-date science on global climate change produced by the Intergovernmental Panel on
586 Climate Change, and local experts on the history and likely future management of local forests.
587 The process of likelihood weighting is inexact, and best subjected to sensitivity analysis (i.e.,
588 repeated evaluation changing likelihoods and re-determining the preferred decision). See Ray et
589 al. (2012) for an example exploration of the sensitivity of staged climate change adaptation
590 decisions to changes in scenario likelihoods.¹¹⁷

591

592 **Conclusion**

593 The deterministic approach to drinking water system design has served society well and led to
594 safe supplies of water at low costs; however, these optimized water systems carry the indirect
595 cost of fragility. This fragility has become increasingly problematic as source water volatility and
596 other extreme events have increased. This increased variability makes reliance on stationarity
597 unsustainable. Water system design has begun to increase emphasis on resilience, although this
598 paradigm still has an adversarial relationship with volatility. Pursuing antifragility in water
599 systems creates a different relationship with change, whereby system processes are placed in a
600 position to perform better as conditions change with less reliance on future forecasts. Processes
601 conveying antifragility can be included into PWS designs by new tools powered by ANNs,
602 including virtual jar and pilot testing, that allow for systematic evaluation of convexity.
603 Including antifragile components into a PWS will inherently cost more than an option optimized
604 for lowest cost. Therefore, developing antifragile characteristics represents a trade-off between
605 performance and cost. Real options analysis is one way for water system designers to consider
606 this trade-off. Ultimately, more research on antifragile designs and costs is required to ensure
607 long-term performance and sustainability of public water systems in an era of increasing
608 volatility.

609

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611

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