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"$^{1}S_{0} \rightarrow ^{3}S_{1}$ Radiative Transition" in Thermal $n-p$ Capture

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Possible Tests on the Verification of and Departure from \(^{1}\text{S}_0 \rightarrow ^{3}\text{S}_1\) Radiative Transition in Thermal \(n-p\) Capture

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Tests are suggested to verify the hypothesis that thermal \(n-p\) capture proceeds via the transition \(^{1}\text{S}_0 \rightarrow ^{3}\text{S}_1\) and that approximately 10\% of the observed capture cross section is due to interaction effects. It is shown that measurements of the \(\gamma\) polarization effect using polarized neutrons and protons are capable of testing the predictions of the hypothesis to within 1\%.

The nuclear two-body problem illustrates perhaps in the most direct way the complexity of nuclear forces. At small values of the relative momenta between the nucleons, the two-body interaction is assumed to be rather insensitive to the detailed nature of the nucleon-nucleon interaction. Such an assumption has been the basis of treating the low-energy \(n-p\) capture and its counterpart, the photodisintegration of the deuteron in the so-called zero-range approximation. (The approximation implies the use of the asymptotic values of the initial- and final-state wave function.) Noyes\(^1\) has analyzed the present status. The conclusion persists that the theoretical calculations are approximately 10\% lower than the measured value of the thermal \(n-p\) capture cross section \(\sigma_n\) of 334 mb.\(^2\) A possible explanation first suggested by Austern and Rost\(^3\) in terms of certain unaccounted-for elementary-particle currents and labeled as "interaction effect" is assumed to be the cause of the discrepancy.

Briefly the customary view point is to assume \(S\)-wave neutron capture and that the capture proceeds via the transition \(^{1}\text{S}_0 \rightarrow ^{3}\text{S}_1\). The transition is characterized as a magnetic dipole isospin-flip and even-\(G\)-parity transition. The operator responsible for the transition is the isovector nucleon magnetic-moment operator. Theoretical calculations using the Bethe-Longmire\(^4\) approximation yield a value of 305 mb. Various efforts have been made to include contributions due to possible \(\pi-\pi\), \(w+\rho\), and \(\eta-\pi\) vertices. The net result of such calculations is an increase of 10 mb with most of it resulting from the \(\pi-\pi\) vertex.\(^5\)

In a recent article Noyes\(^6\) concludes that the nucleon-nucleon scattering experiments below 10 MeV are consistent with an \(n-p\) effective range \(r_{np} = 2.73 \pm 0.03\) F. If the discrepancy between the observed and calculated value of \(\sigma_n\) were to be explained by a downward revision of \(r_{np}\), then its value must be less than 2.4 F.\(^7\) (A decrease in \(r_{np}\) increases the value of \(\sigma_n\).) Noyes' analysis indicates such a possibility to be highly unlikely.

Lately it has been suggested by Malik and Sailor\(^8\) and independently by Breit and Rustgi\(^9\) that a \(^3\text{S}_1 \rightarrow ^{3}\text{S}_1\) transition may be the source of discrepancy. It was further suggested that observations of polarization of the \(\gamma\) rays produced in the capture of polarized neutrons by polarized protons can test the presence of such a transition. Breit and Rustgi, using density-matrix description of the beam and target, examine in detail the asymmetry in the angular distribution and the degree of polarization of the capture \(\gamma\) rays. Their calculations show that for a geometric-mean target-beam polarization \(f = (f_n f_p)^{1/2}\), where \(f_n\) and \(f_p\) are the neutron and proton polarization, respectively, \(f\) can range from 0.954 to 0.577, and that asymmetries in the angular distribution ranging from 34 to 1.96\% may be found. These results are obtained on the assumption that 9\% of the capture occurs via the transition \(^5\text{S}_1 \rightarrow ^{3}\text{S}_1\). In terms of practical possibilities, even the lower value of \(f\) is difficult to achieve except in the case of dynamic polarization. The targets used for dynamic polarization include nuclei with large absorption cross sections, making the observation more difficult.

The purpose of this comment is to suggest a means of establishing departures from the basic underlying hypothesis of the capture process; namely, that the capture occurs solely via the transition \(^{1}\text{S}_0 \rightarrow ^{3}\text{S}_1\). The essential content of the proposed method is a measurement of the spin dependence of the capture \(\gamma\) intensities. It amounts to testing whether the assumed orthogonality of \(^5\text{S}_1\) continuum and the \(^3\text{S}_1\) part of the ground state of deuteron is strictly valid and/or \(p\)-wave capture is likely. Presented below are the theoretical estimates of spin-dependent cross sections to-
gather with the possibility of their observation.

Assume that the neutron beam of polarization \( f_N \) is incident on a proton target of polarization \( f_p \). The quantities \( f_N \) and \( f_p \) are defined as

\[
f_n = \frac{w_1 - w_2}{w_1 + w_2},
\]

where \( w_1 \) are the beam intensities corresponding to the neutrons with magnetic quantum number \( \pm \frac{1}{2} \), respectively, and

\[
f_n = \frac{v_1 - v_2}{v_1 + v_2},
\]

where \( v_1 \) are the target nuclei with magnetic quantum numbers \( \pm \frac{3}{2} \), respectively, in the case of protons. The extent of nuclear polarization is determined by the hyperfine constant via the expression

\[
f_n = \frac{2I+1}{2I} \coth \left( \frac{2I+1}{2I} \mu \right) - \coth \left( \frac{\mu}{2I} \right),
\]

where \( \mu = \mu_f H/kT > \mu_1 \) is the ground-state magnetic moment of the target nuclei at the temperature \( T \) in the field of \( H \) gauss, and \( k \) is the Boltzmann constant.

The capture cross section \( \sigma_+(\tau \tau) \) and \( \sigma_-(\tau \tau) \) for neutrons polarized parallel and antiparallel to the proton polarization, respectively, can be obtained and for \( f_n = 1 \) are given by

\[
\sigma_+(\tau \tau) = \frac{I+1}{2I+1} \sigma_+^{1/2} + \frac{I}{2I+1} \sigma_+^{0/1} + \frac{I}{2I+1} f_n (\sigma_+^{0/1} - \sigma_+^{0/0}),
\]

\[
\sigma_-(\tau \tau) = \frac{I+1}{2I+1} \sigma_-^{1/2} + \frac{I}{2I+1} \sigma_-^{0/1} - \frac{I}{2I+1} f_n (\sigma_-^{0/1} - \sigma_-^{0/0}),
\]

where \( \sigma_+^{a/1} \) and \( \sigma_-^{a/1} \) are the capture cross sections corresponding to the compound state \( J = I + \frac{1}{2} \) and \( J = I - \frac{1}{2} \), respectively. The corresponding total cross sections \( \sigma_+ \) are

\[
\sigma_+ = \sigma_+(1 + \rho f_n)
\]

and

\[
\sigma_- = \sigma_+(1 - \rho f_n),
\]

where \( \rho = [I/(2I+1)](\sigma_+ - \sigma_-)/\sigma_+ \), with \( \sigma_+ \) and \( \sigma_- \) values of the total cross sections corresponding to the compound state \( J = I + \frac{1}{2} \), respectively.

Having given the expressions for all the necessary cross sections we proceed to evaluate the difference in the intensity of the 2.24-MeV \( \gamma \) ray (produced as a result of neutron capture) for parallel and antiparallel spin orientation of the neutrons and protons. In the evaluation of these intensities account must be taken of the variations in the beam intensities \( w_1 \) at different depths inside the sample. It is easily shown that \( w_1 \) satisfy the following differential equations:

\[
d w_1 = [-w_x \sigma_+(1 + p f_n) + D_+ w_+ + D_- w_+] dx,
\]

\[
d w_+ = [-w_x \sigma_-(1 - p f_n) + D_+ w_+ + D_- w_-] dx.
\]

The Eqs. (7a) and (7b) take into account the different values of the incoherent scattering cross sections for the parallel and antiparallel neutron-proton spin orientations and leading to the neutron spin-flip in the zero-magnetic-moment quantum number substate of the triplet state. The spin-flip probability thus depends upon the value \( \sigma_+ - \sigma_- \), where 1 and 0 refer to the scattering lengths for the triplet and the single state. The factors \( D_+ \) and \( D_- \) are the values of the depolarization factors corresponding to the parallel and antiparallel spin orientations. The Eqs. (7a) and (7b) require numerical integration. If, however, we assume that \( D_+ \) can be replaced by the average value \( D = \frac{1}{2}(D_+ - D_-) \) and that the target is thin (i.e., the neutrons scattered more than once, escape the target, and do not

FIG. 1. Differences in the values of the variations of the \( \nu \) polarization effect corresponding to proton polarizations \( f_N = 0.125 \) and \( f_N = 0.275 \) as a function of \( \xi \sigma_+^{0/0} \) and the ZrH\(_{1.85} \) target thickness. All differences are measured from the value of \( \Delta \xi \) for \( \xi = 0 \).
possibility of testing...  

Contribute appreciably to the observed $\gamma$-ray intensities Eqs. (7a) and (7b) can be solved. The result is

$$w_0^\alpha = e^{-\alpha[x_0 \cosh(\kappa x) \pm \tau \sinh(\kappa x)]}$$

$$+ w_0^\alpha \nu \sinh(\kappa x),$$

where

$$\alpha = n \sigma_T + D, \quad \kappa = (n \sigma_T \nu^2 + D^2)^{1/2},$$

$$\tau = n \sigma_T \nu \kappa, \quad \nu = D \kappa, \quad \rho = \rho f_n.$$

The intensities of the two components of the incident neutron beam are $w_0^\alpha$ and $w_0^\beta$, and $n$ is the number of target nuclei per cm$^3$.

The intensity of $\gamma$ rays (2.224-MeV photons) by a strip of thickness $dx$ located at distance $x$ from the entrance surface of the sample can be expressed as

$$dN_\gamma = n dx [w_+ (1 + f_n) + w_- (1 - f_n)]$$

$$+ \frac{1}{2} w_+ [(1 - f_n) + (1 + f_n) + w_+]$$

$$- \frac{1}{2} w_- [(1 - f_n) + (1 + f_n) - w_-].$$

After inserting values of $w_+$, $w_-$ and after somewhat lengthy operations, Eq. (10) can be integrated to yield

$$N_\gamma = \frac{1}{2} \left( N + \tau f_0^n G_1 \right)$$

$$+ f_0^n \left( (\nu - \tau f_0^n G_2) (1 - \xi) \right)$$

$$- f_0^n \left( (\tau + \nu f_0^n G_2) (1 - \xi) \right).$$

(11)

where

$$G_1 \equiv f_1 + f_2, \quad G_2 \equiv f_1 - f_2, \quad \xi = \sigma_1^0 / \sigma_0^0,$$

and

$$f_1 = \int_0^\infty e^{(\kappa + \alpha t) \zeta} dt, \quad f_2 = \int_0^\infty e^{(\kappa - \alpha t) \zeta} dt.$$

$f_0^n = (w_0^\alpha - w_0^\beta) / (w_0^\alpha + w_0^\beta)$ is the incident-neutron beam polarization. If now the incident-beam-neutron spins are flipped with a flipping efficiency $\phi$, an equation similar to Eq. (11) can be obtained. The result is

$$N'_\gamma = \frac{1}{2} \left( N + \tau f_0^n G_1 \right)$$

$$+ f_0^n \left( (\nu - \tau f_0^n G_2) (1 - \xi) \right)$$

$$- f_0^n \left( (\tau + \nu f_0^n G_2) (1 - \xi) \right).$$

(12)

A quantity $\epsilon$, which we designate as the "$\gamma$ polarization effect," similar to the definition of polarization can then be defined as

$$\epsilon = \frac{N_\gamma - N'_\gamma}{N_\gamma + N'_\gamma}.$$

Using Eqs. (11) and (12), we obtain the following

expression for $\epsilon$:

$$\epsilon = \frac{1}{2} \left( \frac{1 + \phi}{2} \right) f_0^n \left( \frac{(3 \xi + 1) \tau G_2 + (1 - \xi) f_0^n G_1 - (\nu G_2)}{(1 - \phi) / 2} \right)$$

$$- f_0^n (1 - \xi) \left[ (\nu G_1 + \nu G_2 - \tau G_2) \right].$$

(13)

We note that $\epsilon \to 0$ as $f_0^n$ and/or $f_0^n$ goes to zero. However, for nonzero values of $f_0^n$ and $f_0^n$, $\epsilon$ does not become zero even when $\xi = 0$. This residual effect is due to the difference in the available neutrons with proper spin orientations for capture in the singlet state. One would therefore measure $\Delta \epsilon$ (variation of $\epsilon$) as a function of nuclear (proton) polarization.

In Fig. 1, the differences of $\Delta \epsilon$ calculated for the two values of $f_0^n = 0.125$ and $0.275$ have been plotted as a function of target thickness for various values of $\epsilon$, starting from $\Delta \epsilon$ for $\xi = 0$ as the base. We have taken for the present purposes a target of ZrH$_2$. Cross-section measurements indicate that the hydrogen in the compound remains atomic and can therefore be polarized because of the proton magnetic moment. A number of other hydrogen compounds also appear promising. The decrease in $\Delta \epsilon$'s versus $t$ corresponds to the fact that depolarization reduces the size of the effect. For an actual experimental circumstance the competing requirement of a statistically significant number of photons must balance the obvious conclusion of Fig. 1 that the thinnest possible sample yields the maximum effect.

The neutron flux available at the High Flux Beam Reactor and the techniques of nuclear polarization (either static or dynamic) make such an experiment a practical possibility. Calculations show that measurements corresponding to $\xi = 0.01$ (2.3 mb) are possible.

We conclude this note by reemphasizing that an observation of nonzero effect implies two possible causes. They are: (1) possible capture via the transition $^3S_1 \to ^3S_2$, and (2) $P$-wave capture from continuum $p$ state to the deuteron ground state.

To distinguish between the two possibilities, measurements of $\gamma$-ray polarization and angular distribution can be made. The capture in the $^3S_1$ con-
Summing-Energy Spectrum of the Beta Particles Plus Emitted K Electrons
in the K-Shell Internal Ionization Accompanying the Beta Decay of $^{63}$Ni

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Through a new type of experiment to obtain information on the K-shell internal ionization in $\beta$ decay, the summing-energy spectrum of electrons ($\beta$ particles plus emitted K-shell electrons) in coincidence with emitted K x rays in the $\beta$ decay of $^{63}$Ni has been observed directly using two proportional counters. The procedure and results are discussed.

This brief note on the direct observation of the spectrum of electrons emitted in the K-shell internal ionization during $\beta$ decay of $^{63}$Ni is an addendum to a recent work by the present authors.\textsuperscript{1} In the previous work, the K x rays from the $\beta$ source mounted inside the electron counter were measured in coincidence with emitted electrons, for seven segments of the $\beta$ spectrum. From the coincidence x-ray counts, the energy-dependent K-shell internal-ionization probability per $\beta$ decay, $P_E(E_0)$, could be obtained as a function of $E_0$, which is defined as the sum of kinetic energies of the $\beta$ particle, $E_\beta$, and the emitted K electron, $E_K$, plus the K-shell binding energy of the daughter atom, $B_K$. In the present work, a summing-energy spectrum of $E_\beta+E_K$ has been measured directly in order to obtain more-refined data on the energy-dependent probability $P_E(E_0)$.

The technique used to prepare the source mounted inside the electron counter is described in the previous paper.\textsuperscript{1} The source solution ($^{63}$NiCl\textsubscript{2} in HCl obtained from the Oak Ridge National Laboratory) was purified using a cation-exchange resin column to remove unfavorable trace ions com-