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IES Calibration for Main Thermocline Depth: A Method Using Integrated XBT Temperature Profiles

Diagram of Moored IES

S.D. Howden, E. Fields, X. Qian, K. Tracey, and D.R. Watts GSO Technical Report No. 93-3

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Abstract

A new method of calibrating Inverted Echo Sounder (IES) travel time measurements to main thermocline depths is described. Unlike the traditional method in which the thermocline is defined by a point measurement, such as the depth of the 12°C isotherm depth as measured with an XBT, this technique utilizes the full temperature profile of XBT casts. The advantage of this method is that the vertical integral of temperature, $Q_T = \int T dz$ is conceptually and empirically very closely correlated with the acoustic travel time measured by the IES, $\tau = 2 \int c^{-1} dz$. Comparisons of the new method with the more traditional point method show that the root-mean-square error in the calibration (11 m standard deviation) is $\frac{1}{3}$ as large as before, and outlier values are significantly reduced. The final coefficients used to calibrate the SYNOP Central and Inlet Array IESs are tabulated.

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Introduction $\mathbf{1}$

An IES measures the time it takes for an emitted acoustic pulse to travel to the sea surface, be reflected and return to the instrument on the ocean floor. From hydrographic data Rossby (1969) showed that, in an appropriate region, the round-trip travel time (τ) measured by an IES is linearly related to the depth of the main thermocline.

Although the main thermocline is defined by a region in the vertical, it is useful for various analyses to characterize it by a single criterion. The most intuitive characterizations are perhaps the depth where the temperature gradient is largest or the midpoint of a depth range defined by a certain value of the gradient. However, these characterizations are not the most convenient ones to implement. We have chosen, for our work in the Gulf Stream, to characterize the thermocline depth as the depth of the 12°C isotherm (Z_{12}) (Friedlander et al., 1986 and Watts et al., 1989), since it is always found in the high gradient region of the Gulf Stream thermal front and does not normally rise to the sea surface at the northern side, even in winter.

In order to convert the round-trip travel time into a thermocline depth a calibration is necessary. As previously mentioned, τ and the main thermocline depth are linearly related. Insofar as Z_{12} represents the main thermocline depth, τ and Z_{12} are also linearly related. The calibration then consists in determining the coefficients $(A \text{ and } B)$ in the equation

$$
Z_{12} = A \cdot \tau + B. \tag{1}
$$

In a geographic area where the above linear relation holds, the slope A will have a fixed value for all IESs while the coefficient B will vary depending upon how deep an IES is moored.

In the past, the calibration of an IES had been accomplished by using Z_{12} s measured from XBT casts (calibration XBTs) over the IES site in conjunction with the τ values from the recovered IES data tape. The τ values chosen were the ones which were most nearly coincident in time with the launch of the XBT. Once the slope A of the relationship between Z_{12} and τ had been found, the calibration of each IES was determined by calculating its unique B-intercept (hereafter BINT) which was taken to be the average of the N BINTs calculated from the N XBT casts and coincident τs at that IES site. Thus, for the ith IES:

Old Method :
$$
BINT_i = N^{-1} \cdot \sum_{j=1}^{N} (Z_{12j} - A \cdot \tau_j)
$$
 (2)

Figure 1a is a flow chart of this process.

Within the main thermocline region the vertical distances between isotherms are compressed or expanded by small scale or high frequency processes such as internal waves. In general, these isotherm depth changes in the thermocline are of small vertical scale. Thus, the individual isotherms can be perturbed in the vertical without a corresponding perturbation of the depth of the thermocline. It is evident that a point measurement, such as the depth of Z_{12} as measured from an XBT cast, is a poorer measure of the thermocline depth: than a measurement which uses the full thermal structure of the thermocline. A better characterization of the depth of the main thermocline is then "the average Z_{12} " (Z_{12}^*) for a given value of a water-column integrated quantity which is sensitive to thermocline depth changes. In this way small vertical scale processes are averaged out. Indeed, the Z_{12} value converted from an IES τ record is a sort of Z_{12}^* for the given τ value, because the sound travels through the whole water column. In the past a possible random offset had been introduced for each XBT by using Z_{12} instead of Z_{12}^* in the calibration process. In order to use Z_{12}^* for IES calibrations, we needed to develop a method to estimate it from an XBT cast.

Watts and Rossby (1977) showed that the heat content of a column of water (Q_h) was linearly related to the depth of the main thermocline. Although Q_h cannot be measured with an XBT, the vertically integrated temperature (Q_T) can be measured. If the heat capacity of the column of water is roughly constant, then Q_T is proportional to Q_h and hence should also vary linearly with the thermocline depth. The main subject of this report is a method devised whereby Q_T calculated from an XBT cast can be related to Z_{12}^* . The Q_T used is not linearly related to the depth of the main thermocline since the integration is not done over the entire water column, but rather it is done over a more limited range of depth as dictated by the use of depth limited XBTs. The relationship between Q_T and Z_{12}^* is, however, monotonic so that each Q_T defines a unique Z_{12}^* . Thus, from an XBT cast we can calculate Q_T and convert it into a characteristic depth Z_{12}^* .

The new method was put into practice in a series of steps. The first step was to determine the functional relationship between the thermocline depth and heat content. To do this, the two quantities Z_{12} and Q_T were calculated from a large set of XBT casts in our study region. The limits of integration for Q_T were chosen so that the shallow limit (200 m) would exclude effects in the seasonally forced upper layer and the deep limit (750 m) would include

calibrating IESs.

Figure 1a: Flow chart of old method of Figure 1b: Flow chart of new method of calibrating IESs.

typical XBT cast depths. From this large set of data, a functional relationship between Z_{12}^* and Q_T could be determined. The value calculated from this function should then be the desired Z_{12}^* for the water column. In this way Z_{12}^* rather than Z_{12} could be used in the calibration. Thus, with the new method:

$$
New Method: \quad BINT_i^* = N^{-1} \cdot \sum_{j=1}^{N} (Z_{12\ j}^* - A \cdot \tau_j)
$$
 (3)

Figure 1b is a flow chart of the new calibration process.

$\overline{2}$ Data Set

The data used in this study were all collected from XBT casts and IES records from the Central and Inlet Array regions of the SYNOP (Synoptic Ocean Prediction) program. The IES data are described in Qian et al. (1990), Fields and Watts (1990), and Fields and Watts (1991). The times and dates, as well as the locations, of the XBT casts are documented in the SYNOP cruise reports (Friedlander, 1987; Kim, 1988; Fields, 1989; Kim, 1989; Cronin, 1990). The data were used in two different ways. 739 XBT casts, taken in the vicinity of the SYNOP Central Array, were used to determine the functional relationship between Z_{12}^* and Q_T in our region of interest. The XBT drop locations are shown in Figure 2. The IES records and all of the calibration XBT casts (those XBT casts taken near the IES sites) were then used to calibrate the IESs.

There were 9 IES sites in the SYNOP Inlet Array. The sites were arranged in three lines set perpendicular to the mean Gulf Stream path. The SYNOP Central Array consisted of 24 IES sites arranged in 5 lines, again set perpendicular to the mean Gulf Stream path. Figure 3 shows the deployment positions of the IESs in both arrays. Over the three year period 1987–90 IESs were deployed and recovered on an annual basis at up to 33 sites (there was one exception when an IES was not recovered for approximately two years).

Altogether there were 88 IES records for the three deployments. During the three SYNOP IES deployments, a total of 355 calibration XBTs with usable records were dropped at the IES sites.

Figure 2: Geographic coverage of XBT casts in the SYNOP Central and Inlet Arrays. Each Δ denotes a cast.

 Z_{12}^* from Q_T^+ 3

 Q_T was defined as

$$
Q_T = \int_{200m}^{750m} T dz
$$
 (4)

 $\mathbf 5$

Excluding the upper 200 m effectively eliminated variability due to the seasonal signal, and the 750 m limit ensured that most T7 XBTs could be used as calibration XBTs. Figure 4 shows the scatter plot of Z_{12} versus Q_T for the SYNOP XBTs.

Superimposed on this plot is the best fit curve to the data, defined as:

$$
Z_{12}^* = \underbrace{A1 * exp\{(Q_T - Q_1)/\lambda_1\} + A2 * exp\{(Q_2 - Q_T)/\lambda_2\}}_{A}
$$

$$
+ a * Q_T + b
$$
 (5)

The linear part of equation 5 (B) was first determined by fitting a cubic polynomial, using least-squares criteria, to the total SYNOP Central and Inlet Arrays XBT data and then determining the tangent line with the smallest slope. The exponential part of equation 5 (A) was fit to the data after the linear trend was removed. Q1 and Q2 were fixed and the other coefficients were found by a least-squares fit of the function to the detrended data.

(Note that a different choice of $Q1$ and $Q2$ can be exactly compensated by coefficients $A1$ and $A2$ for the same λs .) The scatter about this curve should be due primarily to variations of the point values of Z_{12} for a particular thermocline depth. Equation 5 has the following coefficients:

$$
Q1 = 9998
$$

\n
$$
Q2 = 2912
$$

\n
$$
A1 = 246.8
$$

\n
$$
A2 = -107.2
$$

\n
$$
\lambda_1 = 918.5
$$

\n
$$
\lambda_2 = 904.5
$$

\n
$$
a = 0.0788
$$

\n
$$
b = -65.93
$$

Figure 3: Geographic locations and site names of IESs in the SYNOP Central and Inlet arrays. The dashed line indicates the 12 year mean Gulf Stream sea-surface temperature front (provided by Cornillon, personal communication)

 $\overline{7}$

Figure 4: Z_{12} versus $Q_T = \int T dz$ from the SYNOP XBT casts. Superimposed is the best fit curve defined in equation 5.

Best Slope 4

 Z_{12}^* still has a linear relationship with travel time τ , but we will see there is less scatter because they are both integral measurements. In order to determine the slope of the 'best straight line' relationship between Z_{12}^* and τ , the sets of $\{Z_{12}^*, \tau\}$ (one set for each IES), from the calibration XBTs and the IESs respectively, were translated to the same line. This was accomplished by subtracting the average Z_{12}^* and τ for each set from the individual values of Z_{12}^* and τ values of the same set. The residual Z_{12}^* s and τ s all lie on a straight line which passes through the origin. The residual Z_{12}^* s and τ s are defined as:

Residual
$$
Z_{12}^*
$$
 $i,j = Z_{12}^*$ $i,j - N_j^{-1} \cdot \sum_{i=1}^{N_j} Z_{12}^*$ i,j (6)

Residual
$$
\tau_{i,j} = \tau_{i,j} - N_j^{-1} \cdot \sum_{i=1}^{N_j} \tau_{i,j}
$$
 (7)

where $i = 1, N_j$ refers to the *i*th calibration XBT at the *j*th IES site. This process allowed a best fit to the entire SYNOP data set, to refine our value of the slope A in Equation 1. The same process was carried out for the sets of $\{Z_{12},\tau\}$ (the old method) for comparison. Figure 5 shows the scatter plots of both the residual Z_{12}^* and residual Z_{12} versus residual τ

Figure 5: The top panel is a scatter plot of residual Z_{12} versus residual τ (see text for explaination). Also shown is the slope of the linear least-squares best fit to the data. The bottom panel is the same as the top with Z_{12}^* replacing Z_{12} .

and Table 1 lists the results from the linear regressions.

5 **B**-intercepts

B-intercepts from Calibration XBTs Only 5.1

Tables 2-4 contain the \overline{BINTs} and $\overline{BINT*}s$ for all the IESs in the SYNOP Central and Inlet Arrays. Each value is an average over the number of calibration XBTs at that particular site and has an associated standard deviation which is also listed in the tables.

	Old Method	New Method
Slope (ms^{-1})	-19291	-20256
rms error (m)	33	20
St.Dev. (ms^{-1})	238.4	145
R^2 (adj)	95.1	98.3

Table 1: Comparison of calibration slope calculated by the old and new methods.

Table 2: BINTs and BINT*s, and corresponding standard deviations for the IESs in the 1989-90 SYNOP Central and Inlet Arrays. The \dagger indicates that the standard deviation was undefined because only one calibration XBT was available.

 $\boldsymbol{9}$

1988-89 Inlet Array						
IES	\overline{BINT}	STDEV	$\overline{BINT^*}$	STDEV*	FINAL BINT	
B1	4679	20	4665	18	4665	
B ₂ B3	7547 8394	35 19	7567 8414	28 16	7567 8414	
B41 B42	1733 1804	41 9	1733 1803	31	1733	
B51	1943	44	1952	$\boldsymbol{2}$ 37	1803 1952	
B52 C ₁	1862 4278	20 34	1861 4293	8 7	1861 4293	
C ₂	4629		4639	6	4639	

Table 3: BINTs and BINT*s, and corresponding standard deviations for the IESs in the 1988-89 SYNOP Central and Inlet Arrays.

Table 4: BINTs and BINT*s, and corresponding standard deviations for the IESs in the 1987-88 SYNOP Central and Inlet Arrays.

Figures 6 and \overline{y} show histograms of the standard deviations. For comparison, Figure 6 is a histogram of the standard deviations of the BINTs, the B-intercepts calculated using the old calibration method, whereas Figure ∇ shows those obtained with the new method. Note that the center of the distribution for the old method has a greater value than that of the new method. Also, using the old method results in both a greater occurrence and magnitude of outlier values. Table 5 shows the average and standard deviations for the two distributions.

Figure 6: Histogram of the standard deviations for all BINTs. Each "count" is the standard deviation of the set of BINTs for a particular IES.

Figure 7: Histogram of the standard deviations for all BINT*s. Each "count" is the standard deviation of the set of BINT*s for a particular IES.

	New Method	Old Method
Average (m)	19.7	30.9
σ (m)	10.7	26.5

Table 5: Standard deviations and averages of the sets of standard deviations for the BINTs and BINT*s.

5.2 Final B-intercepts for SYNOP Central and Inlet Array IESs

The preceeding sections described the new method used to determine the calibration coefficients for IESs. In this section we document how the SYNOP IES calibrations were further improved by taking into account additional measurements of the thermocline depth obtained from other data sources in the study region. These sources included (i) all XBTs taken on the IES deployment and recovery cruises but were not located right at the instrument sites, (ii) all XBTs located within the Central Array that were dropped as part of the Gulf Stream Anatomy experiment (Hummon et al., 1991), and (iii) twelve current meter moorings located in the Central Array. The adjusted BINT*s, tabulated below, were used in the final calibration of the SYNOP IES.

XBTs. For each XBT, we determined Z_{12}^* using the method described previously. However, because these XBTs were not dropped directly over the IES sites, their Z_{12}^* values could not be used in conjunction with coincident τ measurements to determine BINT*s. Therefore, an alternate approach was developed in order to incorporate these XBTs into the calibration process. The first step was to calibrate the IES τ measurements into Z_{12}^* using the BINTs listed in Tables 2-4. Then, objective maps of these Z_{12}^* estimates were made using the techniques described in Tracey and Watts (1991). The second step was to interpolate the maps to find the Z_{12}^* value at the position and time of each XBT drop. Subsequently the differences ΔZ_{12}^* between the IES-derived and XBT Z_{12}^* estimates were calculated.

Current Meters. The moorings in the SYNOP Central Array consisted of 4 current meters at nominal depths of 400, 700, 1000, and 3500 m. Because these tall moorings were pulled over by the drag of the current, the temperature and velocity measurements were corrected for mooring motion as described in Cronin et al. (1992). A by-product of this motion compensation procedure was a time series of the pressure of the 12°C isotherm at each site. These pressures in decibars were scaled by 1.01 to obtain records of depth in

meters, which are identical to the IES Z_{12}^* measurements. The current meter and IES Z_{12}^* values were compared by first interpolating the IES-derived objective maps to each current meter site and then calculating the record-long averages of the differences (ΔZ_{12}^*) .

Adjustment of BINT*. We used the XBT and current meter ΔZ_{12}^* values to adjust the BINT*s of the IESs. This was accomplished by treating each ΔZ_{12}^* as a supplementary calibration XBT; thus the BINTs listed in Tables 2-4 were adjusted either upwards or downwards by weighting each ΔZ_{12}^* according to the total number of calibration XBTs at each IES. The final BINT^{*}s used to calibrate the SYNOP IESs are listed in Tables 6 and 7.

6 Summary

From a relatively large and well scrutinized data set (over 700 XBTs), a functional relationship between the temperature integrated over standard depth limits Q_T and the depth of the 12^oC isotherm was found. The scatter about this best fit curve is primarily due to the scatter of the point measurement of Z_{12} about a given thermocline depth. This function then allows a quantity Z_{12}^* , with a tighter linear relation to the thermocline depth than Z_{12} , to be calculated from an XBT cast via the Q_T calculation.

The use of Z_{12}^* , rather than Z_{12} , improves the calibration of IESs in two ways. It improves both the relative measure of the thermocline depth, i.e., the measurement at one time relative to that at another at each IES site, and the absolute value of the thermocline depth. The improvement in the relative measure of the thermocline depth is due to the factor of two improvement in the standard deviation of the determination of the slope A. The improvement in the absolute measure of the thermocline depth is indicated by the reduction by a factor of four of the standard deviation of the distribution of standard deviations for the BINT*s versus that of the BINTs.

 $\hat{\mathcal{I}}$

Table 6: Final BINT*s used to calibrate the SYNOP Central Array IESs for the three deployment periods spanning 1987-1990.

Table 7: Final BINT*s used to calibrate the SYNOP Inlet Array IESs for three deployment periods spanning 1987-1990.

 \bar{z}

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