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#### 14. Magnetic Field III

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Lecture slides 14 for Elementary Physics II (PHY 204), taught by Gerhard Müller at the University of Rhode Island.

Some of the slides contain figures from the textbook, Paul A. Tipler and Gene Mosca. Physics

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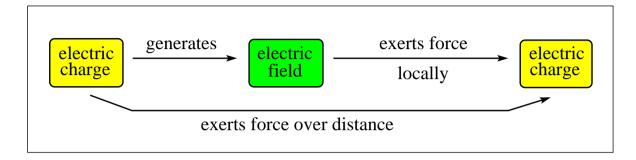
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# **Electric Field of a Point Charge**

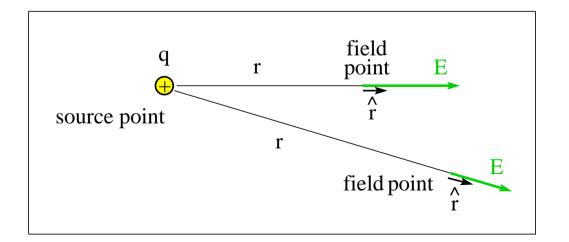




- (1) Electric field  $\vec{E}$  generated by point charge q:  $\vec{E} = k \frac{q}{r^2} \hat{r}$
- (2) Force  $\vec{F}_1$  exerted by field  $\vec{E}$  on point charge  $q_1$ :  $\vec{F}_1 = q_1 \vec{E}$

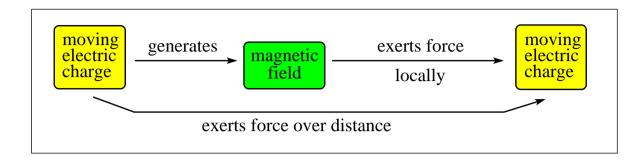
(1+2) Force  $\vec{F_1}$  exerted by charge q on charge  $q_1$ :  $\vec{F_1} = k \frac{qq_1}{r^2} \hat{r}$  (static conditions)

• 
$$\epsilon_0 = 8.854 \times 10^{-12} \text{C}^2 \text{N}^{-1} \text{m}^{-2}$$
  
•  $k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{Nm}^2 \text{C}^{-2}$ 



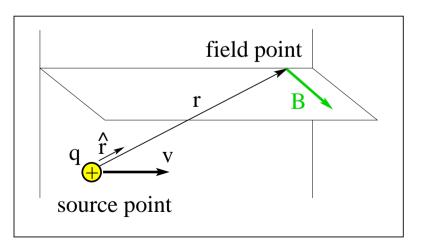
# **Magnetic Field of a Moving Point Charge**





- (1) Magnetic field  $\vec{B}$  generated by point charge q:  $\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$
- (2) Force  $\vec{F_1}$  exerted by field  $\vec{B}$  on point charge  $q_1$ :  $\vec{F_1} = q_1 \vec{v_1} \times \vec{B}$
- (1+2) There is a time delay between causally related events over distance.

• Permeability constant  $\mu_0 = 4\pi \times 10^{-7}$ Tm/A



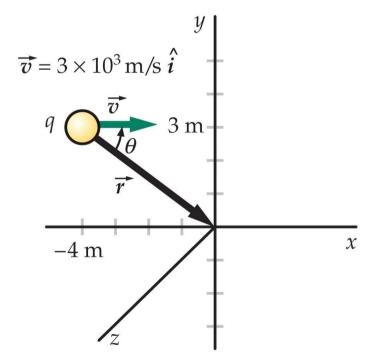
# **Magnetic Field Application (1)**



A particle with charge q = 4.5nC is moving with velocity  $\vec{v} = 3 \times 10^3 \text{m/s}\hat{i}$ . Find the magnetic field generated at the origin of the coordinate system.

- Position of field point relative to particle:  $\vec{r} = 4m\hat{i} 3m\hat{j}$
- Distance between Particle and field point:  $r = \sqrt{(4m)^2 + (3m)^2} = 5m$
- Magnetic field:

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \vec{r}}{r^3}$$
$$= \frac{\mu_0}{4\pi} \frac{q(3 \times 10^3 \,\mathrm{m/s}\hat{i}) \times (4\mathrm{m}\hat{i} - 3\mathrm{m}\hat{j})}{(5\mathrm{m})^3}$$
$$= -\frac{\mu_0}{4\pi} \frac{q(3 \times 10^3 \,\mathrm{m/s}\hat{i}) \times (3\mathrm{m}\hat{j})}{(5\mathrm{m})^3}$$
$$= -3.24 \times 10^{-14} \,\mathrm{T}\hat{k}.$$

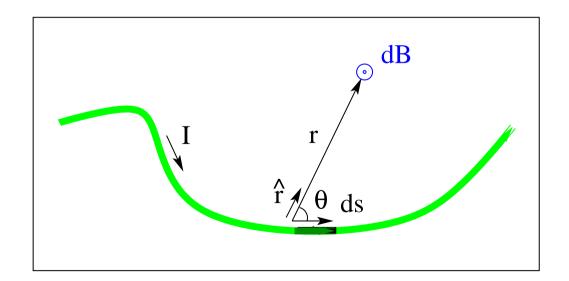


#### Law of Biot and Savart



- Current element:  $Id\vec{s} = dq\vec{v}$  [1Am = 1Cm/s]
- Magnetic field of current element:  $dB = \frac{\mu_0}{4\pi} \frac{dqv \sin \theta}{r^2} = \frac{\mu_0}{4\pi} \frac{Ids \sin \theta}{r^2}$
- Vector relation:  $d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{s} \times \hat{r}}{r^2}$
- Magnetic field generated by current of arbitrary shape:

$$\vec{B} = \frac{\mu_0}{4\pi} \int \frac{Id\vec{s} \times \hat{r}}{r^2}$$
 (Law of Biot and Savart)



# **Magnetic Field of Circular Current**

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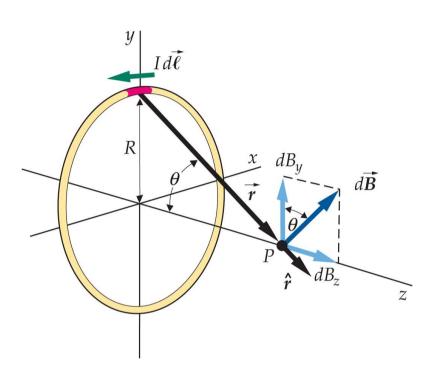


• Law of Biot and Savart: 
$$dB = \frac{\mu_0}{4\pi} \frac{Id\ell}{z^2 + R^2}$$
  
•  $dB_z = dB \sin \theta = dB \frac{R}{\sqrt{z^2 + R^2}}$   
 $\Rightarrow dB_z = \frac{\mu_0 I}{4\pi} \frac{Rd\ell}{(z^2 + R^2)^{3/2}}$   
•  $B_z = \frac{\mu_0 I}{4\pi} \frac{R}{(z^2 + R^2)^{3/2}} \int_0^{2\pi R} d\ell$   
 $\Rightarrow B_z = \frac{\mu_0 I}{2} \frac{R^2}{(z^2 + R^2)^{3/2}}$ 

• Field at center of ring (z = 0):  $B_z = \frac{\mu_0 I}{2R}$ 

• Magnetic moment:  $\mu = I\pi R^2$ 

• Field at large distance 
$$(z \gg R)$$
 :  $B_z \simeq \frac{\mu_0}{2\pi} \frac{\mu}{z^3}$ 



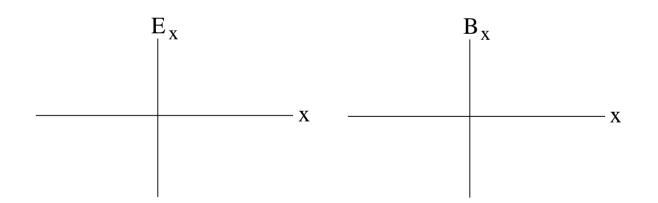
# **Magnetic Field Application (11)**



The electric field  $E_x$  along the axis of a charged ring and the magnetic field  $B_x$  along the axis of a circular current loop are

$$E_x = \frac{Q}{4\pi\epsilon_0} \frac{x}{(x^2 + R^2)^{3/2}}, \qquad B_x = \frac{\mu_0 I}{2} \frac{R^2}{(x^2 + R^2)^{3/2}}$$

- (a) Simplify both expressions for x = 0.
- (b) Simplify both expressions for  $x \gg R$ .
- (c) Sketch graphs of  $E_x(x)$  and  $B_x(x)$ .

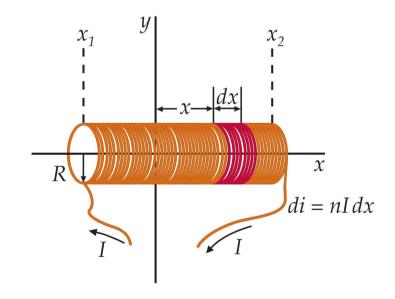


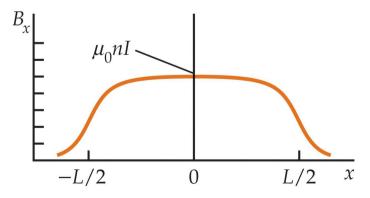
#### **Magnetic Field on the Axis of a Solenoid**

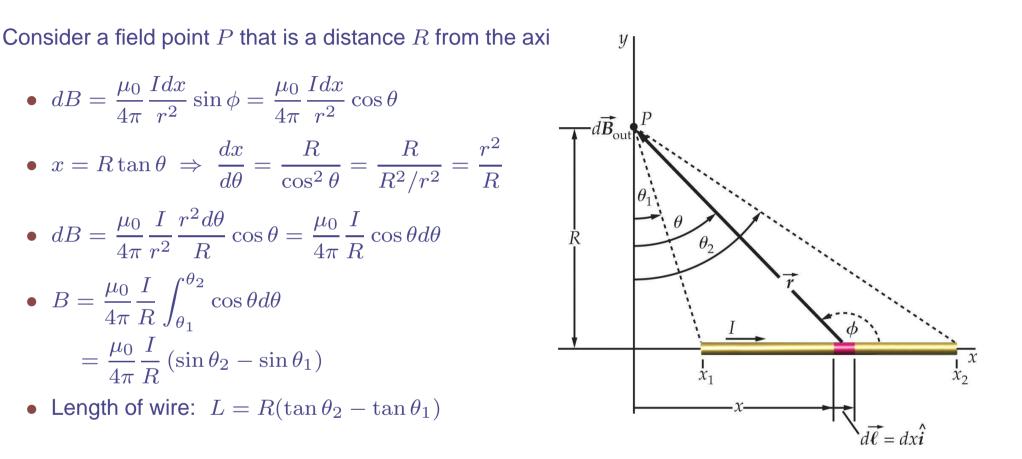


- Number of turns per unit length: n = N/L
- Current circulating in ring of width dx': nIdx'
- Magnetic field on axis of ring:  $dB_x = \frac{\mu_0(nIdx')}{2} \frac{R^2}{[(x-x')^2 + R^2]^{3/2}}$
- Magnetic field on axis of solenoid:

$$B_x = \frac{\mu_0 nI}{2} R^2 \int_{x_1}^{x_2} \frac{dx'}{[(x-x')^2 + R^2]^{3/2}} = \frac{\mu_0 nI}{2} \left( \frac{x-x_1}{\sqrt{(x-x_1)^2 + R^2}} - \frac{x-x_2}{\sqrt{(x-x_2)^2 + R^2}} \right)$$







Wire of infinite length: 
$$\theta_1 = -90^\circ$$
,  $\theta_2 = 90^\circ \Rightarrow B = \frac{\mu_0 I}{2\pi R}$ 

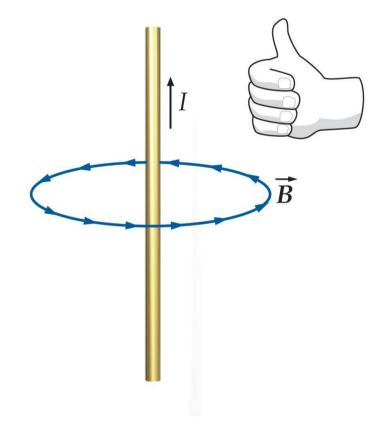


**Magnetic Field Generated by Current in Straight Wire (2)** 

Consider a current *I* in a straight wire of infinite length.

- The magnetic field lines are concentric circles in planes prependicular to the wire.
- The magnitude of the magnetic field at distance *R* from the center of the wire is  $B = \frac{\mu_0 I}{2\pi R}$ .
- The magnetic field strength is proportional to the current *I* and inversely proportional to the distance *R* from the center of the wire.
- The magnetic field vector is tangential to the circular field lines and directed according to the right-hand rule.







Consider the magnetic field  $\vec{B}$  in the limit  $R \rightarrow 0$ .

• 
$$B = \frac{\mu_0}{4\pi} \frac{I}{R} (\sin \theta_2 - \sin \theta_1)$$
  
•  $\sin \theta_1 = \frac{a}{\sqrt{a^2 + R^2}} = \frac{1}{\sqrt{1 + \frac{R^2}{a^2}}} \simeq 1 - \frac{1}{2} \frac{R^2}{a^2}$   
•  $\sin \theta_2 = \frac{2a}{\sqrt{4a^2 + R^2}} = \frac{1}{\sqrt{1 + \frac{R^2}{4a^2}}} \simeq 1 - \frac{1}{2} \frac{R^2}{4a^2}$   
•  $B \simeq \frac{\mu_0}{4\pi} \frac{I}{R} \left(1 - \frac{1}{2} \frac{R^2}{4a^2} - 1 + \frac{1}{2} \frac{R^2}{a^2}\right)$   
 $= \frac{\mu_0 I}{4\pi} \frac{3R}{8a^2} \xrightarrow{R \to 0} 0$ 

a

a

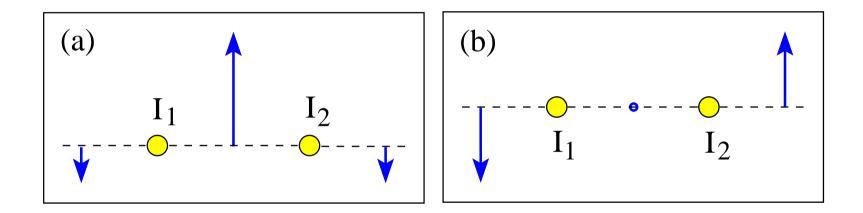
 $\theta_1$ 

# **Magnetic Field Application (2)**



The currents  $I_1, I_2$  in two long straight wires have equal magnitude and generate a magnetic field  $\vec{B}$  as shown at three points in space.

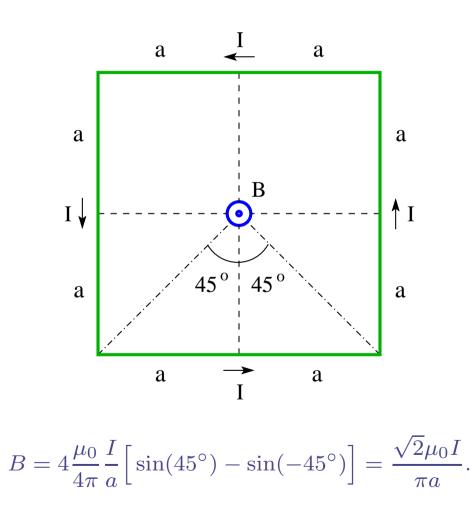
• Find the directions  $(\odot, \bigotimes)$  for  $I_1, I_2$  in configurations (a) and (b).



# **Magnetic Field at Center of Square-Shaped Wire**



Consider a current-carrying wire bent into the shape of a square with side 2a. Find direction and magnitude of the magnetic field generated at the center of the square.

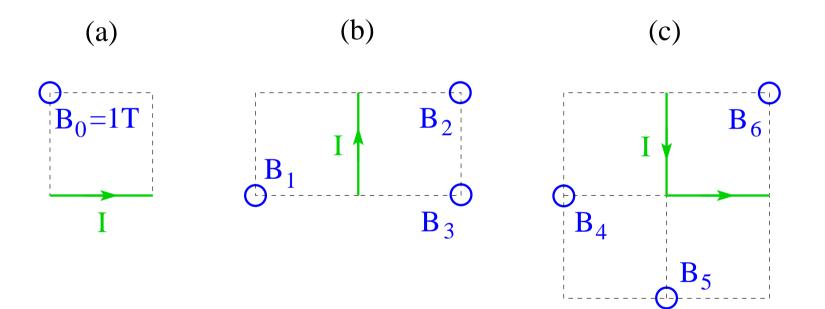


# **Magnetic Field Application (5)**



If the current I in (a) generates a magnetic field  $B_0 = 1T$  pointing out of the plane

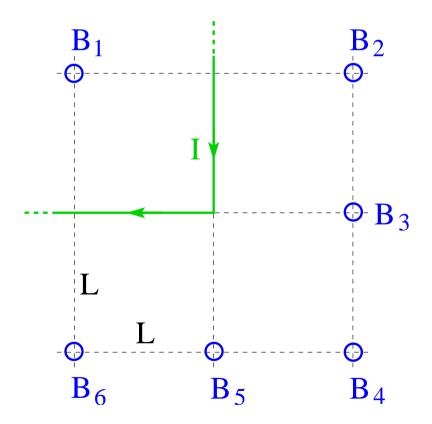
- find magnitude and direction of the fields  $B_1, B_2, B_3$  generated by I in (b),
- find magnitude and direction of the fields  $B_4, B_5, B_6$  generated by I in (c).





A current-carrying wire is bent into two semi-infinite straight segments at right angles.

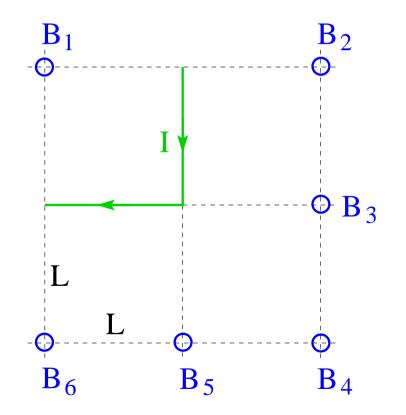
- (a) Find the direction  $(\odot, \bigotimes)$  of the magnetic fields  $B_1, \ldots, B_6$ .
- (b) Name the strongest and the weakest fields among them.
- (c) Name all pairs of fields that have equal strength.





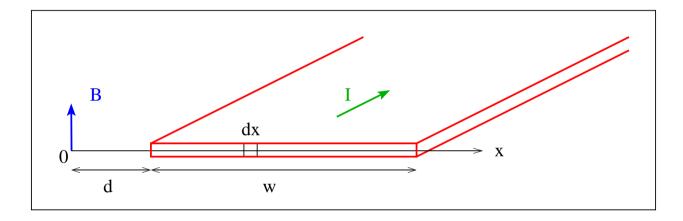
A current-carrying wire is bent into two straight segments of length L at right angles.

- (a) Find the direction  $(\odot, \bigotimes)$  of the magnetic fields  $B_1, \ldots, B_6$ .
- (b) Name the strongest and the weakest fields among them.
- (c) Name all pairs of fields that have equal strength.



Consider a very long ribbon of width w carrying a current I in the direction shown. The current density is assumed to be uniform.

Find the magnetic field B generated a distance d from the ribbon as shown.



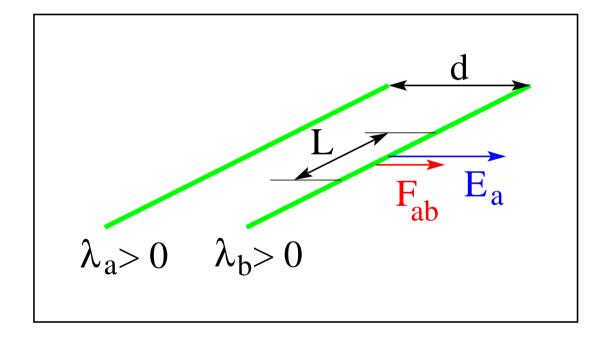
Divide the ribbon into thin strips of width dx. Treat each strip as a wire with current dI = I dx/w. Sum up the field contributions from parallel wires.

$$dB = \frac{\mu_0}{2\pi} \frac{dI}{x} = \frac{\mu_0 I}{2\pi w} \frac{dx}{x}$$
$$B = \frac{\mu_0 I}{2\pi w} \int_d^{d+w} \frac{dx}{x} = \frac{\mu_0 I}{2\pi w} \ln\left(1 + \frac{w}{d}\right)$$

#### **Force Between Parallel Lines of Electric Charge**



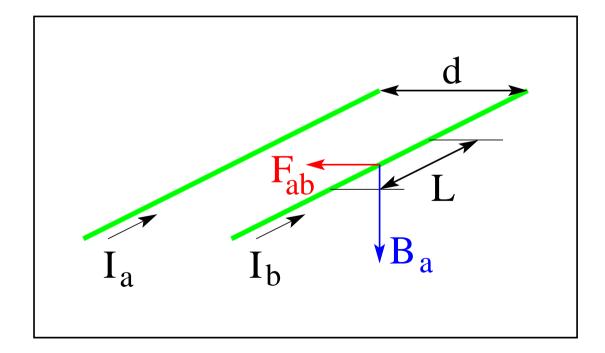
- Electric charge densities:  $\lambda_a, \lambda_b$
- Electric field generated by line *a*:  $E_a = \frac{1}{2\pi\epsilon_0} \frac{\lambda_a}{d}$
- Electric force on segment of line b:  $F_{ab} = \lambda_b L E_a$
- Electric force per unit length (repulsive):  $\frac{F_{ab}}{L} = \frac{1}{2\pi\epsilon_0} \frac{\lambda_a \lambda_b}{d}$



#### **Force Between Parallel Lines of Electric Current**



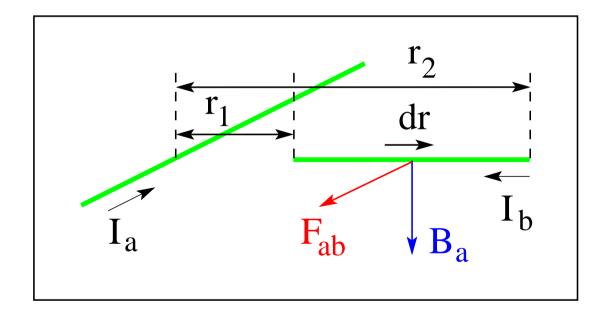
- Electric currents:  $I_a, I_b$
- Magnetic field generated by line *a*:  $B_a = \frac{\mu_0}{2\pi} \frac{I_a}{d}$
- Magnetic force on segment of line b:  $F_{ab} = I_b L B_a$
- Magnetic force per unit length (attractive):  $\frac{F_{ab}}{L} = \frac{\mu_0}{2\pi} \frac{I_a I_b}{d}$



#### **Force Between Perpendicular Lines of Electric Current**



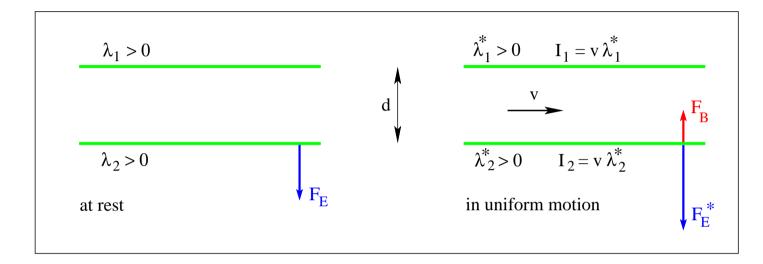
- Electric currents:  $I_a, I_b$
- Magnetic field generated by line *a*:  $B_a = \frac{\mu_0}{2\pi} \frac{I_a}{r}$
- Magnetic force on segment dr of line b:  $dF_{ab} = I_b B_a dr$
- Magnetic force on line *b*:  $F_{ab} = \frac{\mu_0}{2\pi} I_a I_b \int_{r_1}^{r_2} \frac{dr}{r} = \frac{\mu_0}{2\pi} I_a I_b \ln \frac{r_2}{r_1}$



# **Is There Absolute Motion?**



#### Forces between two long, parallel, charged rods



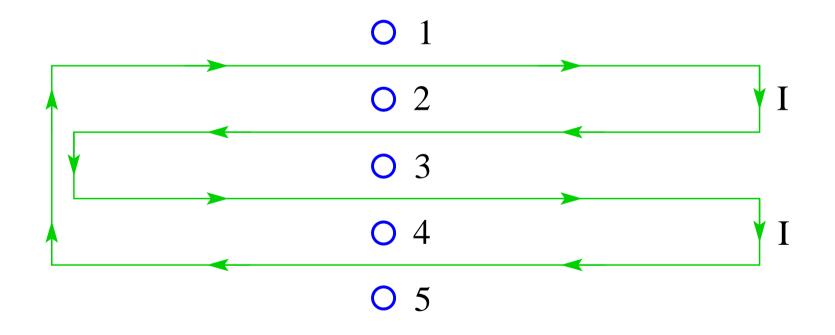
• 
$$\frac{F_E}{L} = \frac{1}{2\pi\epsilon_0} \frac{\lambda_1 \lambda_2}{d} \quad \text{(left)}, \qquad \frac{F_E^*}{L} = \frac{1}{2\pi\epsilon_0} \frac{\lambda_1^* \lambda_2^*}{d}, \quad \frac{F_B}{L} = \frac{\mu_0}{2\pi} \frac{I_1 I_2}{d}, \quad \text{(right)}$$
• 
$$\frac{F_E^* - F_B}{L} = \frac{1}{2\pi\epsilon_0} \frac{\lambda_1^* \lambda_2^*}{d} \left(1 - \frac{v^2}{c^2}\right) = \frac{1}{2\pi\epsilon_0} \frac{\lambda_1 \lambda_2}{d}$$
• 
$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = 2.998 \times 10^8 \text{ ms}^{-1} \quad \text{(speed of light)}$$
• 
$$\lambda_1^* = \frac{\lambda_1}{\sqrt{1 - v^2/c^2}}, \quad \lambda_2^* = \frac{\lambda_2}{\sqrt{1 - v^2/c^2}} \quad \text{(due to length contraction)}$$

# **Magnetic Field Application (4)**



An electric current I flows through the wire as indicated by arrows.

- (a) Find the direction  $(\odot, \bigotimes)$  of the magnetic field generated by the current at the points  $1, \ldots, 5$ .
- (b) At which points do we observe the strongest and weakest magnetic fields?

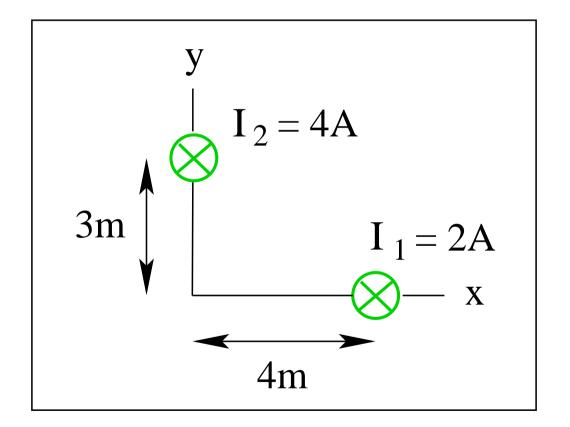


# **Magnetic Field Application (12)**



Consider two infinitely long straight currents  $I_1$  and  $I_2$  as shown.

• Find the components  $B_x$  and  $B_y$  of the magnetic field at the origin of the coordinate system.

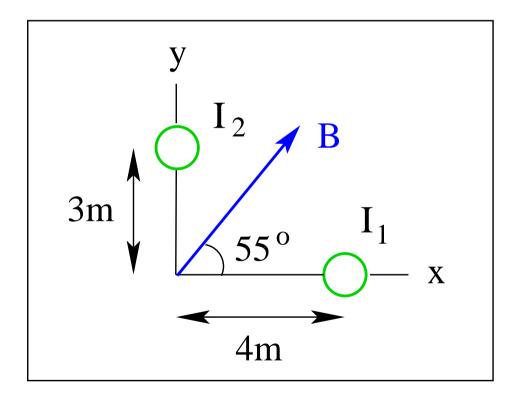


# **Magnetic Field Application (13)**



Two straight electric currents  $I_1$  and  $I_2$  of infinite length directed perpendicular to the *xy*-plane generate a magnetic field of magnitude  $B = 6.4 \times 10^{-7}$ T in the direction shown.

• Find the magnitude and direction  $(\odot, \otimes)$  of each current.

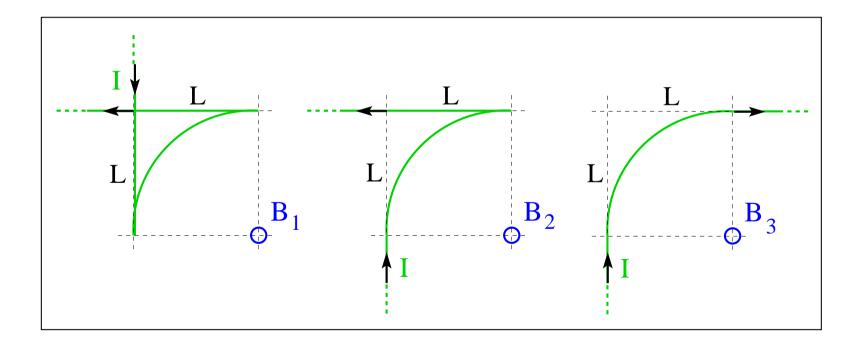


# **Magnetic Field Application (3)**



Two semi-infinite straight wires are connected to a segment of circular wire in three different ways. A current *I* flows in the direction indicated.

- (a) Find the direction  $(\odot, \bigotimes)$  of the magnetic fields  $\vec{B}_1, \vec{B}_1, \vec{B}_3$ .
- (b) Rank the magnetic fields according to strength.

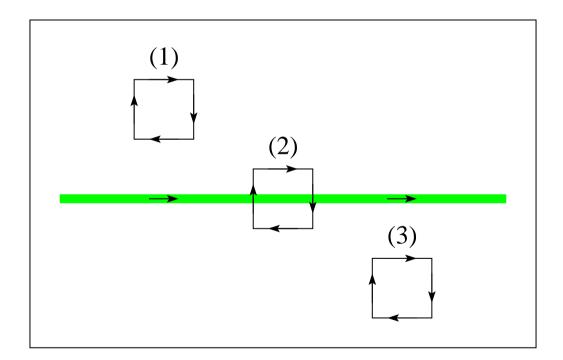


# **Magnetic Field Application (8)**



Three squares with equal clockwise currents are placed in the magnetic field of a straight wire with a current flowing to the right.

• Find the direction ( $\uparrow$ ,  $\downarrow$ , zero) of the magnetic force acting on each square.

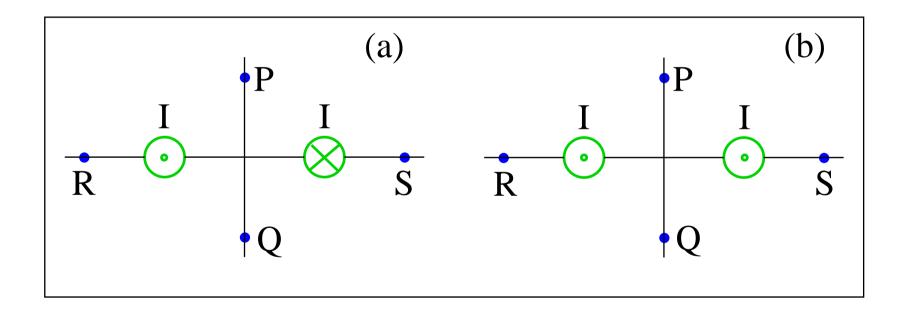


# **Magnetic Field Application (10)**



Consider two currents of equal magnitude in straight wires flowing perpendicular to the plane.

 In configurations (a) and (b), find the direction (→, ←, ↑, ↓) of the magnetic field generated by the two currents at points P, Q, R, S

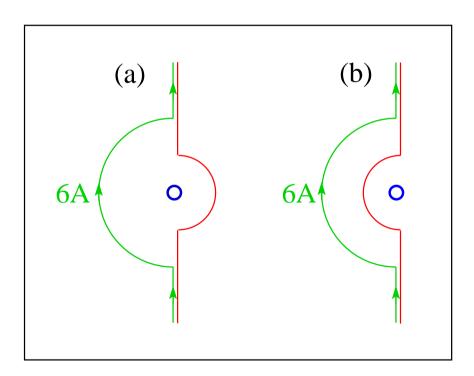


# **Magnetic Field Application (9)**



Two wires of infinite length contain concentric semicircular segments of radii 1m and 2m, respectively.

If one of the wires carries a 6A current in the direction indicated, what must be the direction
 (↑,↓) and magnitude of the current in the other wire such that the magnetic field at the center
 of the semicircles vanishes?

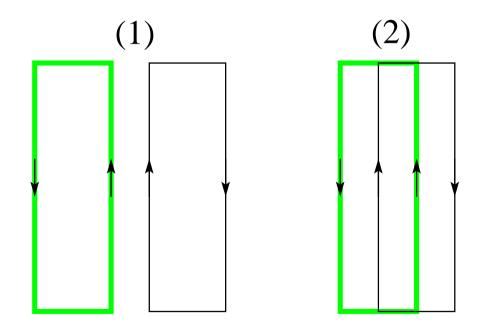


# **Magnetic Field Application (14)**



Consider two pairs of rectangular electric currents flowing in the directions indicated.

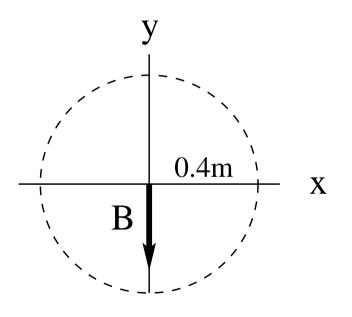
- (a) What is the direction  $(\rightarrow, \leftarrow)$  of the magnetic force experienced by the black rectangle in each case?
- (b) Which black rectangle experiences the stronger magnetic force?



mini

An infinitely long straight current of magnitude I = 6A is directed into the plane ( $\otimes$ ) and located a distance d = 0.4m from the coordinate origin (somewhere on the dashed circle). The magnetic field  $\vec{B}$  generated by this current is in the negative *y*-direction as shown.

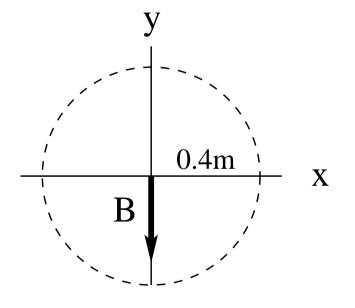
- (a) Find the magnitude B of the magnetic field.
- (b) Mark the location of the position of the current  $\otimes$  on the dashed circle.



An infinitely long straight current of magnitude I = 6A is directed into the plane ( $\otimes$ ) and located a distance d = 0.4m from the coordinate origin (somewhere on the dashed circle). The magnetic field  $\vec{B}$  generated by this current is in the negative *y*-direction as shown.

- (a) Find the magnitude *B* of the magnetic field.
- (b) Mark the location of the position of the current  $\otimes$  on the dashed circle.

(a) 
$$B = \frac{\mu_0}{2\pi} \frac{I}{d} = 3\mu T.$$





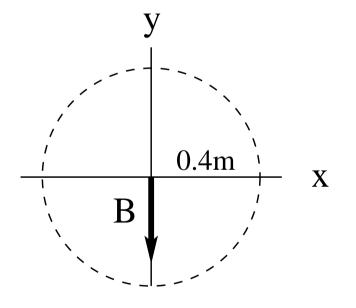
An infinitely long straight current of magnitude I = 6A is directed into the plane ( $\otimes$ ) and located a distance d = 0.4m from the coordinate origin (somewhere on the dashed circle). The magnetic field  $\vec{B}$  generated by this current is in the negative *y*-direction as shown.

- (a) Find the magnitude B of the magnetic field.
- (b) Mark the location of the position of the current  $\otimes$  on the dashed circle.

Solution:

(a) 
$$B = \frac{\mu_0}{2\pi} \frac{I}{d} = 3\mu T.$$

(b) Position of current  $\otimes$  is at y = 0, x = -0.4m.

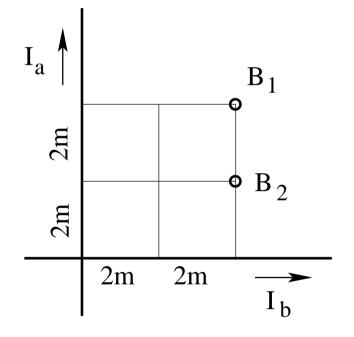


Consider two infinitely long, straight wires with currents of equal magnitude  $I_1 = I_2 = 5$ A in the directions shown. Find the direction (in/out) and the magnitude of the magnetic fields  $B_1$  and  $B_2$  at the points marked in the graph.

 $\begin{array}{c|c}
I_a & & & & & & & & & \\
\hline B_2 & & & & & & & \\
\hline B_2 & & & & & & & \\
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Consider two infinitely long, straight wires with currents of equal magnitude  $I_1 = I_2 = 5$ A in the directions shown.

Find the direction (in/out) and the magnitude of the magnetic fields  $B_1$  and  $B_2$  at the points marked in the graph.

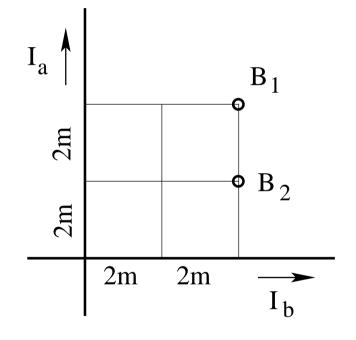


• 
$$B_1 = \frac{\mu_0}{2\pi} \left( \frac{5A}{4m} - \frac{5A}{4m} \right) = 0$$
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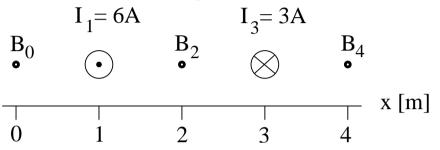


• 
$$B_1 = \frac{\mu_0}{2\pi} \left( \frac{5A}{4m} - \frac{5A}{4m} \right) = 0$$
 (no direction).  
•  $B_2 = \frac{\mu_0}{2\pi} \left( \frac{5A}{2m} - \frac{5A}{4m} \right) = 0.25\mu T$  (out of plane).



Consider two very long, straight wires with currents  $I_1 = 6A$  at x = 1m and  $I_3 = 3A$  at x = 3m in the directions shown. Find magnitude and direction (up/down) of the magnetic field (a)  $B_0$  at x = 0,  $I_1 = 6A$   $I_3 = 3A$ (b)  $B_2$  at x = 2m,  $B_0$  G  $B_2$  G  $B_4$ 

(c)  $B_4$  at x = 4m.



Consider two very long, straight wires with currents  $I_1 = 6A$  at x = 1m and  $I_3 = 3A$  at x = 3m in the directions shown. Find magnitude and direction (up/down) of the magnetic field  $I_{1} = 6A$ (a)  $B_0$  at x = 0,  $I_3 = 3A$ (b)  $B_2$  at x = 2m,  $B_2$  $B_0$  $B_4$ 0 (c)  $B_4$  at x = 4m. 0 • x [m] 0 3 2 1 4

(a) 
$$B_0 = -\frac{\mu_0(6A)}{2\pi(1m)} + \frac{\mu_0(3A)}{2\pi(3m)} = -1.2\mu T + 0.2\mu T = -1.0\mu T$$
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 (down),  
(b)  $B_2 = \frac{\mu_0(6A)}{2\pi(1m)} + \frac{\mu_0(3A)}{2\pi(1m)} = 1.2\mu T + 0.6\mu T = 1.8\mu T$  (up),

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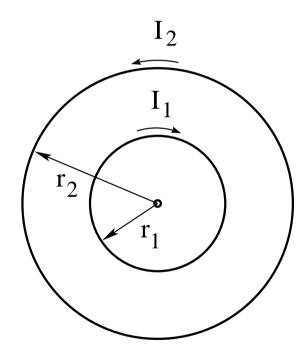
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(c)  $B_4 = \frac{\mu_0(6A)}{2\pi(3m)} - \frac{\mu_0(3A)}{2\pi(1m)} = 0.4\mu T - 0.6\mu T = -0.2\mu T$  (down).



Consider two circular currents  $I_1 = 3A$  at radius  $r_1 = 2m$  and  $I_2 = 5A$  at radius  $r_2 = 4m$  in the directions shown.

(a) Find magnitude B and direction  $(\odot, \otimes)$  of the resultant magnetic field at the center.

(b) Find magnitude  $\mu$  and direction  $(\odot, \otimes)$  of the magnetic dipole moment generated by the two currents.



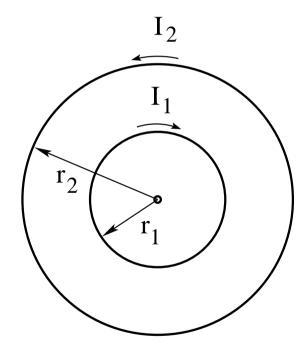


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(a) 
$$B = \frac{\mu_0(3A)}{2(2m)} - \frac{\mu_0(5A)}{2(4m)} = (9.42 - 7.85) \times 10^{-7} T$$
  
 $\Rightarrow B = 1.57 \times 10^{-7} T \otimes$ 



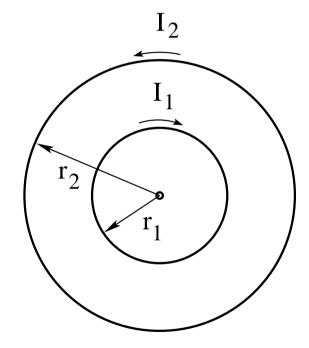


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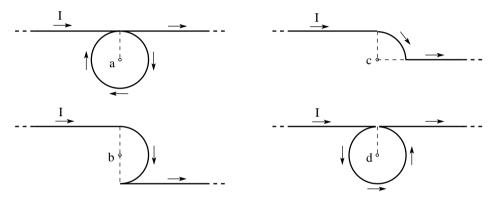
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 $\Rightarrow B = 1.57 \times 10^{-7} T \otimes$   
(b)  $\mu = \pi (4m)^2 (5A) - \pi (2m)^2 (3A) = (251 - 38) Am^2$   
 $\Rightarrow \mu = 213 Am^2 \odot$ 



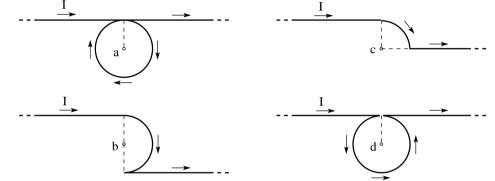


Two semi-infinite straight wires are connected to a curved wire in the form of a full circle, quarter circle, or half circle of radius R = 1m in four different configurations. A current I = 1A flows in the directions shown. Find magnitude  $B_a, B_b, B_c, B_d$  and direction  $(\odot/\otimes)$  of the magnetic field thus generated at the points a, b, c, d.





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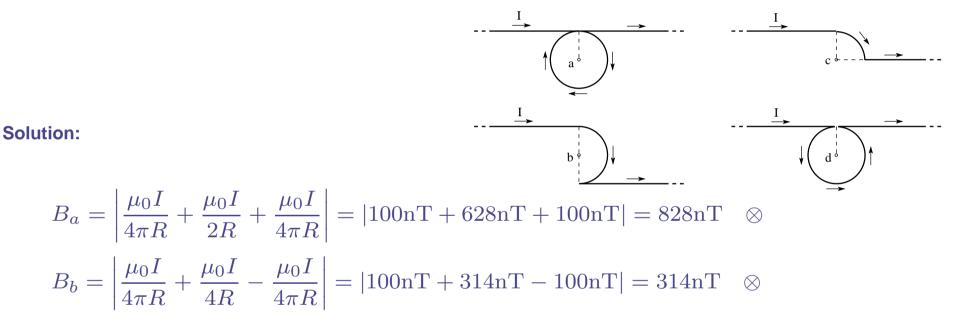


**Solution:** 

 $B_a = \left| \frac{\mu_0 I}{4\pi R} + \frac{\mu_0 I}{2R} + \frac{\mu_0 I}{4\pi R} \right| = |100\text{nT} + 628\text{nT} + 100\text{nT}| = 828\text{nT} \quad \otimes$ 



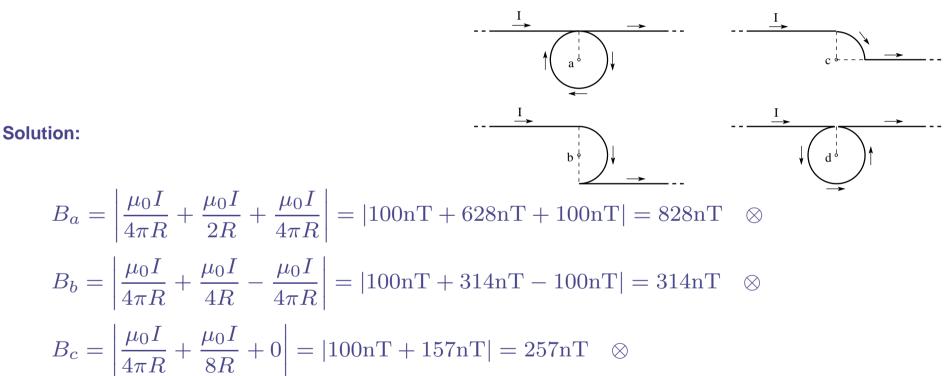
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