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#### 09. Resistors I

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Lecture slides 9 for Elementary Physics II (PHY 204), taught by Gerhard Müller at the University of Rhode Island.

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# **Equilibrium**:

 $\vec{E}$  $= 0$  inside conductor. Mobile charge carriers undergo random motion.

## **Nonequilibrium**:

 $\vec{E}\neq 0$  inside conductor. Mobile charge carriers undergo random motion and drift. Positive charge carriers drift from high toward low electric potential and negative charge carriers from low towardhigh electric potential.

## **Electric current**:

• Net charge flowing through given cross-sectional area per unit time.

• 
$$
I = \frac{dQ}{dt}.
$$

• SI unit: 1C/s <sup>=</sup> 1A (one Ampère)



#### **Current and Current Density**

Consider drift of Na $^+$  and Cl $^-$  ions in a plastic pipe filled with salt water.

- $\bullet \;\; v_1>0, \; v_2<0{:} \;\;$  drift velocities
- $\bullet$   $\,q_1>0,\ q_2<0\mathrm{:}\,$  charge on ions
- $\bullet$   $\left\lceil n_1,\; n_2\right\rceil$  number of charge carriers per unit volume



- Net charge flowing through area A in time  $dt$ :  $dQ=n_1q_1v_1Adt+n_2q_2v_2Adt$  [C]
- Electric current through area A: I ≡ $dQ$  $\frac{d\mathbf{v}}{dt}=A(n_1q_1v)$  $v_1 + n_2 q_2 v$  $v_2)$  [A]
- Current density:  $\vec{J} = n_1q_1\vec{v_1} + n_2q_2\vec{v_2}$  [A/m<sup>2</sup>  $^2]$
- Current equals flux of current density:  $I$ = $\int \vec{J} \cdot d$  $\vec{A}$

### **Current Direction**





positive charge carriers

#### negative charge carriers



current  $I$  flowing toward left in both cases

#### **Resistance and Resistivity**



- •**Resistor**: device (material object with two terminals)
- •**Resistance**: attribute of device
- $\bullet$ **Resistivity**: attribute of conducting material

A voltage  $V$  provided by some source is applied to the terminals of a resistor and a current  $I$  is observed flowing through the resistor.

• Resistance: 
$$
R = \frac{V}{I}
$$
 [1Ω=1V/A] (1 Ohm)

The current density  $\vec{J}$  in a resistor depends on the local electric field  $\vec{E}$  and on the resistivity  $\rho$  of the resistor material.

• **Resistivity:** 
$$
\rho = \frac{E}{J} \left[ \frac{1 \text{V/m}}{1 \text{A/m}^2} = 1 \Omega \text{m} \right]
$$

- Conductivity:  $\sigma = \frac{1}{\rho}$  $[1(\Omega \mathrm{m})^{-1}]$
- Vector relations:  $\vec{E}$  $= \rho \vec{J}, \quad \vec{J}$  $=\sigma \vec{E}$



#### **TABLE 25-1**

#### **Resistivities and Temperature Coefficients**



$$
\bullet \ \alpha = \frac{(\rho - \rho_{20})/\rho_{20}}{t_C - 20^{\circ}\text{C}}
$$

- $\alpha$ : temperature coefficient at  $20^{\circ}$ C in K $^{-1}$
- $\rho$ : resistivity near  $20^{\circ}$ C
- $\rho_{20}$ : resistivity at 20 $\rm ^{\circ}$ C
- $t_C$ : temperature in  $\circ$ C

**Ohm's Law**







RESISTOR - WW



 $DIODE - M$ 







#### **Uniform cross section**

- Length of wire:  $L$
- Area of cross section:  $A$ •
- Resistivity of material:  $\rho$
- Current density: J = $\boldsymbol{E}$  ρ[A/  $\mathrm{m}^2$  $\sim$ ]<br>]
- Current:  $I = JA$  [A]
- Voltage:  $V = EL$  [V]
- Resistance:  $R \equiv$  $\,V\,$  $\frac{V}{I}=\frac{\rho L}{A}$  A $\frac{1}{A}$  [Ω]

## **Variable cross section**

- Cross-sectional profile:  $A(x)$
- Resistance of slice:  $dR = \frac{\rho dx}{A(x)}$
- Resistance of wire:  $R = \rho \int_0^L$ 0 $dx \$  $\overline{A(x)}$



### **Radial Current in Coaxial Cable**





$$
dR = \frac{\rho dr}{A}, \quad A = 2\pi rL
$$

$$
R = \frac{\rho}{2\pi L} \int_{a}^{b} \frac{dr}{r} = \frac{\rho}{2\pi L} \ln \frac{b}{a}
$$

### **Electric Current Application (1)**



A steady current  $I$  is flowing through a wire from left to right. The wire first doubles its diameter and then splits into two wires of the original diameter. Both branches on the right carry the same current.



Rank the current densities  $J_1, J_2, J_3=J_4$  in the three segments.



Two wires are formed into

- (a) an equilateral triangle,
- (b) <sup>a</sup> regular pentagon.

A voltage between points <sup>1</sup> and <sup>2</sup> produces <sup>a</sup> current of 12mA along the shorter path.



What is the current along the longer path in each case?



Consider three wires made of the same material.

Wire 1 of length 2m and diameter 2mm has a resistance  $18\Omega.$ 

- (a) What resistance does wire <sup>2</sup> of length 4m and diameter 4mm have?
- (b) How long is wire 3 of diameter 6mm with a resistance of  $18\Omega?$

#### **Resistor: Material and Device Perspectives**



•  $\vec{E}$ : electric field

### **Material**

- $\vec{J}$ : current density
- $\bullet\,$   $\rho\!$ : resistivity
- $\sigma = 1/\rho$ : conductivity
- $\bullet~~ \vec{E}=\rho \vec{J}, ~~~\vec{J}=\sigma \vec{E}$



## **Device**

- $\bullet\,$   $V$ : voltage
- $\bullet$  *I*: electric current
- $\bullet$   $R$ : resistance
- $V = RI$

Current from current density:  $\,I\,$ = $\int \vec{J} \cdot d$  $\vec{A}$ Voltage from electric field:  $\ V= \int_a^b \vec{E} \cdot d\vec{s}$  $\it a$ 





Consider <sup>a</sup> resistor in the form of <sup>a</sup> uniform wire.

- Voltage between ends:  $V \equiv V_a V_b = E(x_b x_a)$
- Displaced charge:  $\Delta q = I \Delta t$ •





• Work done by electric field  $\vec{E}$  on displaced charge  $\Delta q$ :

 $W_E = F(x_b - x_a) = E \Delta q (x_b - x_a) = V \Delta q = VI \Delta t$ 

- Power dissipated in resistor:  $P = \frac{W_E}{\Delta t}$  $\Delta t$  $= VI = I$ 2 ${}^2R=$  $\,V\,$ 2 $\, R$
- SI unit:  $1V·1A = (1J/C)·(1C/s) = 1J/s = 1W$  (Watt)

#### **Electric Heating Element**





#### **Incandescent Light Bulb**





- voltage drives electric current throughfilament
- •electric current heats up filament
- •hot filament emits radiation
- • radiation has significant intensity in visiblerange around 4000 degrees Fahrenheit.
- $\bullet$  most energy is emitted in the form of heat (infrared radiation)
- inert gas (e.g. argon) regulates heat transport and prevents oxidation
- tungsten has high melting point

## **Resistor Problem (1)**



A heating element is made of a wire with a cross-sectional area  $A = 2.60 \times 10^{-6} \text{m}^2$  and a mosisticity for  $200 \times 10^{-7}$ resistivity  $\rho = 5.00 \times 10^{-7} \Omega \text{m}$ .

- (a) If the element dissipates  $5000W$  when operating at a voltage  $V_1 = 75.0V$ , what is its length  $L_{1},$  its resistance  $R_{1},$  and the current  $I_{1}$  running through it?
- (b) What must be the voltage  $V_2$ , the resistance  $R_2$ , and the length  $L_2$  of a heating element made of the same wire if the same power should be generated with half the current?

### **Resistor Problem (2)**



A  $1250{\rm W}$  radiant heater is constructed to operate at  $115{\rm V}$ .

- (a) What will be the current in the heater?
- (b) What is the resistance of the heating coil?
- (c) How much thermal energy is generated in one hour by the heater?